A fault tolerant Neuro-Fuzzy Inference system: using Coarse-coded Distributed Representations

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Abstract: - In this paper, we describe a fault-tolerant Neuro-Fuzzy inference system for performing fuzzy reasoning using *coarse-coded* distributed representations. The system implements the fuzzy membership functions in a novel way using coarse-coded distributed representations for the inputs and outputs of neural networks. Distributed representations are known to give advantages of fault tolerance, generalization and graceful degradation of performance under noise conditions. Performance of the Neuro-Fuzzy inference system with regard to its ability to exhibit fault tolerance under noise conditions is studied. The system offered very good results of fault tolerance under noise conditions. It has also exhibited good generalization ability on unseen test inputs.

Key-Words: - Coarse-coding, Fuzzy rules, Neural, Reasoning, Fault tolerance, Membership function.

1 Introduction

Traditionally reasoning systems using predicate logic have been implemented using symbolic methods of artificial intelligence. Connectionist or neural network methods of implementation of reasoning systems describe an alternative paradigm. Among the connectionist reasoning systems they use two types of representational schemes. They are 1) localist and 2) distributed representational schemes.

Localist representational schemes represent each concept with an individual unit or neuron. In the distributed representational schemes [5] each unit or neuron is used in representation of multiple concepts and multiple units or neurons are used to represent a single concept. In the literature, some localist methods for predicate logic reasoning using connectionist networks have been described. The connectionist inference system *SHRUTI* [1], [2], [3] described a localist method where temporal synchrony was used to create bindings between variables and entities they represent. A variable x of the predicate give(x, y, z) is getting bound to an entity d if the nodes representing them fire during the same phase of time p1 during the predicate p activation period T. The time period T is divided into three phases p1, p2 and p3 during which synchronous firing of variables x_{i} y and z and entity nodes they bound respectively takes place. This method has used temporal synchrony as a mechanism to create localist representations. CONSYDERR [4,9] described a localist method for variable binding and forward reasoning. It used an assembly or a set of interconnected nodes to represent each predicate $p(x_1, \dots, x_k)$. Each assembly contains one C node for storing the confidence value of the predicate p and k X nodes to store the binding values for k variables of the predicate p. A separate node is allocated for each variable of a predicate. Since, these systems used localist representations. advantages of distributed representations were not obtained

by them. In our previous works [6,7,8] we proposed and described predicate logic reasoning systems using neural networks which used coarse-coded distributed representations to represent instantiated predicates. In these publications we have described the advantages of using the coarse-coded representations along with neural networks for performing predicate logic reasoning. However, the predicate logic reasoning is nonfuzzy and crisp reasoning and hence not suitable for fuzzy reasoning. Here we propose to examine the use of the coarse-coded distributed representations along with the neural networks in the implementation of a Fuzzy-rule-based system. Our motivation is to make available the advantages of distributed coarse-coded representations to the neuro-fuzzy reasoning systems. It is investigated here in this work to examine the advantages gained by the Neuro-Fuzzy reasoning system by using distributed coarse-coded representations.

2 Fuzzy Rule Base

We propose to implement, as an example, the following TSK (Takagi-Sugeno) fuzzy rules in our system.

1. If x is small and y is small, then $z = f_1 = -x + y/4 + 1$ 2. If x is small and y is large, then $z = f_2 = 0.75y + 3$ 3. If x is large and y is small, then $z = f_3 = x + 2$ 4. If x is large and y is large, then $z = f_4 = x + y + 1$ 5. If x is medium and y is large, then $z = f_5 = x/2 + y + 2$ 6. If x is small and y is medium, then $z = f_6 = -x + y/2 + 1$

For given crisp input values for x and y the inferred output *z* is calculated by

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Z = (\mu_1 f_1 + \mu_2 f_2 + \mu_3 f_3 + \mu_4 f_4 + \mu_5 f_5 + \mu_6 f_6) / (\mu_1 + \mu_2 + \mu_3 + \mu_4 + \mu_5 + \mu_6) \qquad (1)
where
\mu_1 = \mu_{small}(X)^* \mu_{small}(Y);
\mu_2 = \mu_{small}(X)^* \mu_{large}(Y);
\mu_3 = \mu_{large}(X)^* \mu_{small}(Y);
\mu_4 = \mu_{large}(X)^* \mu_{large}(Y);
\mu_5 = \mu_{medium}(X)^* \mu_{large}(Y);
\mu_6 = \mu_{small}(X)^* \mu_{medium}(Y)
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where $\mu_{small}(x)$ denotes the membership function for linguistic value *small* of the linguistic variable x,

 $\mu_{medium}(x)$ denotes the membership function for linguistic value *medium* of the linguistic variable x, $\mu_{large}(x)$ denotes the membership function for linguistic value large of the linguistic variable x, $\mu_{small}(y)$ denotes the membership function for linguistic value *small* of the linguistic variable y, $\mu_{medium}(y)$ denotes the membership function for linguistic value *medium* of the linguistic variable y, $\mu_{large}(y)$ denotes the membership function for linguistic value *large* of the linguistic variable y, and '*' denotes the 'Minimum' operation between the indicated fuzzy membership functions. Our task is to start with the above fuzzy rule base and obtain the results of fuzzy inference correctly by our system.



Fig.1. Neural Networks N1 to N6 implement fuzzy membership functions

The architecture for implementing the fuzzy membership functions with neural networks N1 to N6 which use coarse-coded representations at their inputs and outputs is shown in the figure 1 above. Neural networks N1 to N6 implement $\mu_{\text{small}}(\mathbf{X}), \ \mu_{\text{medium}}(\mathbf{X}), \ \mu_{\text{large}}(\mathbf{X}), \ \mu_{\text{small}} \ (\mathbf{y}), \ \mu_{\text{medium}}(\mathbf{y})$ and $\mu_{large}(y)$ respectively. x and y values are coarse-coded before giving them as inputs to the neural networks N1 to N6. Neural networks N1 to N6 generate on their outputs respective membership function values in coarse-coded form. These membership function values after decoding will be in the interval [0, 1]. Each of the six circles at the right side of figure 1 are used to denote the 'minimum' operation performed on its inputs on the decoded

membership function values. They generate on their outputs μ_1 to μ_6 respectively. From these the value of output *z* is computed using formula in equation (1) for a given *x*, *y*.

3 Description of data used by fuzzy membership functions

We show here in the following tables 1 to 6 the samples of the data needed by the fuzzy membership functions $\mu_{small}(x)$, $\mu_{medium}(x)$, $\mu_{large}(x)$, μ_{small} (*y*), $\mu_{medium}(y)$ and $\mu_{large}(y)$ respectively. We assume the data shown in tables 1 to 6 is obtained from the expert knowledge for the efficient performance of our fuzzy system.

Table 1. Shows a sample of data used by membership function $\mu_{small}(x)$

S.No.	Х	μ _{small} (x)
2	6.0	0.98
10	30.0	0.08

Table 2. Shows a sample of data used by membership function $\mu_{medium}(x)$

S.No.	х	μ _{medium} (x)
8	24.0	0.98
14	42.0	0.1

Table 3. Shows a sample of data used by membership function $\mu_{large}(x)$

S.No.	х	$\mu_{large}(x)$
12	36.0	0.3
16	48.0	0.96

Table 4. Shows a sample of data used by membership function $\mu_{small}(y)$

S.No.	у	µ _{small} (y)
3	6.0	0.95
5	10.0	0.6

Table 5. Shows a sample of data used by membership function $\mu_{medium}(y)$

S.No.	у	μ _{medium} (y)
6	12.0	0.3
12	24.0	0.4

Table 6. Shows a sample of data used by membership function $\mu_{large}(y)$

S.No.	у	μ _{large} (y)
11	22.0	0.45
14	28.0	0.95

3.1 Obtaining Coarse-coded Distributed Representations

We describe here how to obtain coarse-coded representations of the data shown in the tables 1 to 6. If the data items to be coarse-coded lie in the interval [R1, R2] where R1 and R2 are real numbers then we divide the interval [a, b] into N sub-intervals, where a = floor(R1) and b = ceiling(R2). Suppose we need to encode the real number R present in the kth sub-interval we proceed as follows. If R is in lower half of the sub-interval k we represent R with a localist pattern having (N+1) bits, with $(k)^{th}$ bit 1 and other bits 'zero'. If R is in upper half of the subinterval k we represent R with a localist pattern having N+1 bits, with $(k+1)^{th}$ bit 1 and other bits zero. We illustrate the coarse-coding process through an example. For coarse-coding output values of membership functions we chose N =40. Consider the 2nd row of table 1. The value of $\mu_{small}(x)$ is 0.08. Since this value belongs to lower half of 4th sub-interval we encode it with a localist pattern of 41 bits with 4th bit 1 and all other bits 'zero'.

'0000000000 00000000 00000000 0000001000'(2)

We are yet to convert this localist pattern into the coarse-coded pattern. We add three leading zeroes to left side of the above pattern for the reason described below to get the following pattern

'0000000000000 00000000 00000000 000001000'.

We illustrate the process of converting the above localist pattern into the coarse-coded pattern. We view the above pattern as being kept in overlapping coarse zones of length of 4 consecutive bits and encode the zone as 1 if there is at least one 1 bit in that zone or else as 0. We then consider next coarse zone and encode it as 1 or 0 following above method. We do this process left to right starting from the left most bit. We do this encoding process for above localist pattern to get the following coarse-coded pattern

'0000000000000 00000000 00000000 0001111000'.

The reason we have added three leading zeros to the localist pattern in (2) is to enable us to coarse-code the pattern even if the 1 bit occurred in the 41st bit (from the right side) of the pattern.

Coarse-coding can be applied when the number of 1's in the original string is sufficiently sparse. If the number of 1's in the original string is not sufficiently sparse then coarse-coded string when decoded will not yield the original string. Coarse-coding increases the information capacity [5] by increasing the number of units active at a time compared to localist codes which have sparsely populated 1's. The amount of information conveyed by a unit that has a probability p of being '1' is

-plog(p) - (1 - p) log(1 - p).

The coarse-coding process involves making an approximation and hence an error. To decrease the error to the desired limits, we choose an appropriate value of 'N'. 'x' and 'y' values used by our fuzzy system are real numbers in the range 0 to 60.0, 0 to 40.0 respectively. The N values for coarse-coding them were chosen to be 60 and 40 respectively. Using the technique described the above we obtain coarse-coded representations of patterns for all the fuzzy membership function inputs and outputs in our system. We show here a sample of coarsecoded representations of the patterns for the various membership functions in tables 7 to 12.

Table 7. Shows a sample of coarse-coded data used by membership function $\mu_{small}(x)$

S.No.	Х	µ _{small} (X)
6	00000000	00000000
	00000 00	000000 11
	00000000	11000000
	00000000	0000000000
	00 00000	0 0000000
	00001 11	000
	10000000	
	00000000	
	00	

Table 8. Shows a sample of coarse-coded data used by membership function $\mu_{medium}(x)$

S.No	Х	μ _{medium} (X)
8	0000000000	0011110
	0000 0000	0000000
	000000 00	00000000

00000000	00 00000
000111100	0000000
0 0000000	00000000
000 00000	
00000	

Table 9. Shows a sample of coarse-coded data used by membership function $\mu_{large}(x)$

S.No.	Х	μ _{large} (x)
9	00000000	0000000
	00000 00	0000000
	00000000	0000000
	01111000	000 0000
	00 00000	011110 0
	00000000	0000000
	00000000	00
	00000000	
	00	

Table	e 10. Shows a sample of coarse-coo	bet
data	used by membership function μ_{small}	(y)

S.No.	Y	µ _{small} (y)
3	00000000	0001111
	00000 00	0000000
	00000000	0000000
	00000000	000 000
	00 011110	0000000
	0000	0000000
		000

Table	e 11. Shows a sar	mple of coars	e-coded
data	used by member	ship function	μ _{medium} (y)

S.No.	у	μ _{medium} (y)
6	0000000	00000000
	000000	000000 0
	0001111	00000000
	000 0000	0 011110
	000000 0	0000 000
	0000000	0000000
	00	

Table 12. Shows a san	nple of coarse-coded
data used by members	ship function $\mu_{large}(y)$

У	μ _{large} (y)
000000000	0000000
00000 00	0000000
00011110	0000000
00000000	001 1110
00 00000	000000 0
00000	0000000
	00
	y 000000000 00011110 00000000 00000000 000000

4 Testing

Following are the details of neural networks used in our work shown in table 13. The neural networks N1 to N6 in figure 1 are feed forward neural networks using back-propagation algorithm.

Table 13. Shows the details of neural networks used

Neural Network	No. of input units	No.of hidden units	No.of output units
N1	63	52	44
N2	63	52	44
N3	63	52	44
N4	43	32	44
N5	43	32	44
N6	43	32	44

The fuzzy reasoning task was successfully accomplished by using the system to give the expected results. The value of system output z obtained for two values of (x, y) are shown in table 14.

Table 14. Shows the details of inputs (x,y) andcorresponding z values

Sr.no	1	2
Х	16	33
у	11	20
μ1	0.6	0
μ2	0	0.05
μ3	0	0
μ4	0	0.05
μ5	0	0.2
μ6	0.05	0.05
Z	-12.04	29.14

 Table 15. Shows the details of tests for faulttolerance

Neural Network	No. of Training Patterns	No. of Test Patterns	No. of Patterns Corrected	No. of Patterns not Corrected
N1	20	20	20	0
N2	20	20	19	1

N3	20	20	19	1
N4	20	20	20	0
N5	20	20	20	0
N6	20	20	20	0

Secondly, the performance of the above coarse-coded Neuro-Fuzzy reasoning system was tested for fault tolerance under noise conditions for each of the neural networks N1 to N6. In the tests, neural networks N1 to N6 are trained with 20 patterns each. These training patterns were made test patterns after introducing 1 bit error at a random location in each of these patterns. These artificially simulating introduced errors are noise conditions. Results are as shown in table 15. The coarse-coded Fuzzy reasoning system was found to be highly fault tolerant to errors as was indicated by the test results.

In the second set of tests conducted, the performance of Coarse-coded fuzzy reasoning system was checked for its generalization ability on unseen test patterns. The system has displayed good generalization ability on unseen test patterns. Results are shown in table 16.

Table 16.	Shows	the	details	of tests	s for
	gene	eraliz	ation		

Neural	No. of	No. of	No. of	No. of
Network	Training	unseen	Patterns	Patterns
	Patterns	Test	Correctly	not
		Patterns	generalized	Correctly
				generalized
N1	20	20	14	6
N2	20	20	16	4
N3	20	20	17	3
N4	20	20	16	4
N5	20	20	14	6
N6	20	20	13	7

5 Conclusions

We have designed and tested a Neuro-Fuzzy reasoning system which uses distributed coarse-coded representations with the neural networks. The system implements in a novel way the fuzzy membership functions for its linguistic terms using neural networks with coarse-coded distributed representations at their inputs and outputs. The system has successfully performed the fuzzy reasoning. The coarse-coded fuzzy reasoning system exhibited good generalization ability on unseen test patterns thereby displaying learning ability. The coarse-coded fuzzy reasoning system exhibited very good fault tolerance under simulated noise conditions as indicated by the tests.

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