# **Platform Independent Neural Semi-Inverse Controller**

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*Abstract:* – The neural network based semi-inverse controller is similar to an inverse controller. An inverse controller uses an inverse model of the controlled plant. On the other hand, the semi-inverse controller is based on a forward model of the plant. This avoids some of the problems of inversion. The algorithm is suitable for implementation in a PLC. For maximum portability of the algorithm between the development environment and its final implementation in the PLC, the algorithm is implemented on top of an abstract object-oriented layer, which provides platform independency.

Key-Words: - Neural network, Semi-inverse controller, Portable implementation, Real time

## 1 Introduction

Ever since neural networks began to be used in controller algorithms, the designs of the algorithms were often based on the ability of a neural network to approximate the inverse dynamics of the controlled plant. Serial connection of this inverse model with the plant then theoretically suffices to respond well to the desired value.

Unfortunately the inversion approach has several problems. The inverse model can be hard or even impossible to obtain. Other problems arise from the fact that the inverse controller is a dead-beat controller. This leads to high sensitivity to the precise learning of the model. When working with short sampling periods, it also produces extreme control actions. These problems are highlighted when noise is present. They can be mitigated with filtration, but it worsens the dynamics of the control system.

The semi-inverse controller [1] attempts to avoid the problem of the inverse model learning by basing itself on a forward model instead.

The control algorithm is first developed in a simulation environment. However, the goal is to implement it win a PLC. In order to simplify the final porting, the implementation of the algorithm uses a portability layer.

### 2 The semi-inverse controller

#### 2.1 The inverse controller in a closed loop

Let's suppose the plant is approximated by an ARMA model:

$$F_{\rm M}(z) = \frac{b_0 + b_1 z^{-1} + b_2 z^{-2} + \dots + b_m z^{-m}}{1 + a_1 z^{-1} + a_2 z^{-2} + \dots + a_n z^{-n}}$$
(1)

An inverse controller would have a transfer function:

$$F_{\rm C}(z) = \frac{1 + a_1 z^{-1} + a_2 z^{-2} + \dots + a_n z^{-n}}{b_0 + b_1 z^{-1} + b_2 z^{-2} + \dots + b_m z^{-m}}$$
(2)

The inverse controller is normally used in an open loop, without a real feedback. This is undesirable because it doesn't eliminate disturbance. Therefore when used in a closed control loop, it computes the action as:

$$u_{k} = \frac{1}{\underline{b_{0}}} (e_{k} + a_{1}e_{k-1} + a_{2}e_{k-2}... + a_{n}e_{k-n} - b_{1}u_{k-1} - b_{2}u_{k-2} - ... - b_{m}u_{k-m})$$
(3)

where: 
$$k \dots$$
 discrete time step  
 $u_k \dots$  control action in step  $k$   
 $e_k \dots$  control error in step  $k$ 

The big sensitivity of the controller on the model accuracy comes mainly from the parameter  $b_0$ , especially when its value is close to zero.

After the finish of a transient response, the control action will be:

$$u_{\rm S} = \frac{1}{b_0} [e_{\rm S}(1 + a_1 + a_2 + \dots + a_n) - u_{\rm S}(b_1 + b_2 + \dots + b_m)]$$
(4)

It is clear that in the steady state (indicated by the index S) the control error  $e_{\rm S}$  would be non-zero. Let's introduce a modified control error:

$$e_{M,k} = w_k + e_k = 2w_k - y_k \tag{5}$$

where:  $e_{M,k}$  ..... modified control error in step k $w_k$  ..... desired value in step k $y_k$  ..... system output in step k

This is implemented by a filter  $F_k(z)$ . If the controller operates on the modified control error, it will remain non-zero in the steady state but the real error will be able to reach zero. In order for this to work as expected, the gain of the open loop must be 1.

#### 2.2 Modification for a semi-inverse controller

Let's start from the inverse controller operating on the modified error. In a steady state, its action will be:

$$u_{\rm S} = \frac{1}{b_0} [e_{\rm M,S}(1 + a_1 + a_2 + \dots + a_n) - u_{\rm S}(b_1 + b_2 + \dots + b_m)]$$
(6)

In order to simplify the situation, let's assume that the gain of the plant model is  $A_{\rm M} = 1$ . We'll generalize this assumption away later. For now let's also assume that the desired value is  $w_k = 1$ . Under these simplifying conditions we can write:

$$u_{\rm S} = y_{\rm S} = e_{\rm M,S} = w_{\rm S} = 1$$
 (7)

Therefore some of the members in the equation (6) can be cancelled, resulting in:

$$1 = \frac{(1 + a_1 + a_2 + \dots + a_n) - (b_1 + b_2 + \dots + b_m)}{b_0}$$
(8)

Thus it holds that:

 $1 = b_0 - a_1 - a_2 - \dots - a_n + b_1 + b_2 + \dots + b_m$ (9)

At this point we'll modify the inverse controller and rewrite the action of the semi-inverse controller in the steady state as:

$$1 = u_{\rm S} = e_{\rm M,S}(b_0 - a_1 - a_2 - \dots - a_n) + + u_{\rm S}(b_1 + b_2 + \dots + b_m) = = 1 \cdot (b_0 - a_1 - a_2 - \dots - a_n) + + 1 \cdot (b_1 + b_2 + \dots + b_m)$$
(10)

The idea behind this modification is that the parameter  $b_0$  is transferred instead of constant 1 in the inverse controller. In the non-steady case the action is computed as:

$$u_{k} = b_{0}e_{\mathrm{M},k} - a_{1}e_{\mathrm{M},k-1} - a_{2}e_{\mathrm{M},k-2} - \dots$$
$$-a_{n}e_{\mathrm{M},k-n} + b_{1}u_{k-1} + b_{2}u_{k-2} + \dots + b_{m}u_{k-m}$$
(11)

The corresponding transfer function of the semi-inverse (SI) controller is:

$$F_{\rm SI}(z) = \frac{b_0 - a_1 z^{-1} - \dots - a_n z^{-n}}{1 - b_1 z^{-1} - \dots - b_m z^{-m}}$$
(12)

#### 2.3 Normalization of gain

The total gain of the serial connection of the semiinverse controller and the plant is:

$$A = A_{\rm SI}A_{\rm M} = \frac{b_0 - a_1 - a_2 \dots - a_n}{1 - b_1 - b_2 - \dots - b_m} \cdot \frac{b_0 + b_1 + b_2 + \dots + b_m}{1 + a_1 + a_2 + \dots + a_n}$$
(13)

To fulfil the requirement that the gain of the open loop is equal to 1, it's necessary to add a multiplication by  $\frac{1}{A}$ to the open loop.

## **3** Implementation

The algorithm was originally implemented in ANSI C as an S-function in Matlab Simulink. Thanks to the availability of ANSI C development environment in the B&R PLC the final porting was therefore simplified. To make porting completely seamless, an abstract interface was developed for control algorithms. It allows to transfer the source code of control algorithms between Matlab S-functions and B&R PLCs without changes (Fig. 4).



Fig. 1: Control loop with a semi-inverse controller



Fig. 2: The model can be linear ARMA or non-linear neural network (NN) model



Fig. 3: The semi-inverse controller is based on the model, only its inputs are reconfigured



Fig. 4: Transfer of the control algorithm using the abstract interface



Fig. 5: Test of the semi-inverse controller on a physical model with approximate transfer  $F_{\rm M}(s) = \frac{1}{(5s+1)(s+1)^2}$ 

It also theoretically enables the transfer of compiled binaries of control algorithms between these platforms, because they are based on the same CPU architecture (Intel x86). Only the skeleton parts of the interface had to be implemented separately on both platforms. Not having to change the source code of the algorithm decreases the probability of introducing new bugs during porting.

The portability interface is object-oriented. Although ANSI C is a classical procedural programming language with no object-oriented elements, it is still possible to use an object-oriented design in it, including properties such as inheritance and partially even encapsulation. An abstract base class is defined of which classes of control algorithms are descended. It describes virtual methods, which the control algorithm classes redefine.

### 4 Testing the controller

The semi-inverse controller was implemented and tested in simulations and on physical models. An example of testing with a physical model can be seen on Fig. 5.

## 5 Conclusion

The semi-inverse controller is computationally simple and suitable for real-time control. It is highly adaptable. It also works with short sampling periods, which is an advantage for disturbance cancellation. It performed well in testing on simulations and on physical models.

The abstract object-oriented interface for control algorithms proved useful in porting of the semi-inverse controller to the PLC. Using this interface, the source code of the algorithm is identical in the Matlab Sfunction and in the PLC. The encapsulation of the control algorithm into an object class allows easy parallel operation of multiple controllers in a single program. Control algorithms providing this interface are modular and interchangable to a large degree.

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