

## Rainfall Estimation from Convective Storms Using the Hydro-Estimator and NEXRAD

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*Abstract* - Validation of the Hydro-Estimator (HE) and the Next Generation Radar (NEXRAD) during heavy storms over Puerto Rico (PR) is reported. The HE is a high resolution rainfall retrieval algorithm based on satellite and numerical weather prediction model data. The accuracy of the HE and the NEXRAD rainfall estimates can be measured by decomposing the rainfall process into sequences of discrete (rain / no rain) and continuous (rainfall rate) random variables. Validation results are based on five heavy storms that seriously impacted human life and the economy of PR during the period 2003 to 2005. The average discrete validation results indicate acceptable hit rate values for both the HE and NEXRAD (0.76 vs. 0.87) and reasonable discrete bias ratios (1.04 vs. 0.73) but a very low of probability of detection of rain for both the HE and NEXRAD (0.36 vs. 0.52). The HE shows an overestimation on average whereas the NEXRAD exhibits underestimation in the continuous validation results (continuous bias ratio of 1.14 vs 0.70 for NEXRAD), which contributes to moderate overall errors for the HE and NEXRAD in terms of root mean squared error (2.14 mm vs. 1.66 mm) and mean absolute error (0.96 mm vs. 0.77 mm).

The HE algorithm was designed to operate over US continental areas and satisfactory results have been reported. However, over tropical regions it was determined that warm clouds can generate substantial rainfall amounts that are not detected by the HE algorithm. It is known that precipitation processes in clouds with warm tops are very sensitive to the microphysical structure of their tops. Specifically, precipitation processes are more efficient when water droplets or/and ice particles grow to larger sizes. It has been shown that the uses of the reflected portion of the near-infrared during the daytime indicates the presence large cloud-top particles and suggest rain in warm-top clouds. It has been used the effective radius of clouds particles to detect raining clouds. However, the available algorithms to estimate the effective radius are designed to operate over ice clouds. We are in the process of developing an algorithm to extract the microphysical structure for rainy warm top clouds, and the first step of this algorithm is to estimate the emittance of near infrared window, which is described in this paper.

*Key-words* - validation, NEXRAD, Hydro-Estimator, retrieval algorithm, rain rate, GOES, brightness temperature.

## 1. Introduction

Estimation of rainfall amounts is critical for protecting human lives and infrastructure, particularly in the case of heavy rainfall that triggers flash floods or landslides. In Puerto Rico (PR) during 2003 to 2005, five severe storms seriously impacted human lives and the economy. PR has extremely diverse terrain, and during the rainy season severe rainstorms can develop due to complex orographic attributes. Easterly winds come from the eastern Atlantic almost all year and play an important role in bringing humidity into the island and stimulating orographic rainfall over the mountains of PR. Cold fronts dominate the weather pattern during wintertime. Tropical waves occur during the rainy season and frequently generate large amounts of rainfall in the Caribbean basin. These tropical waves are typically the precursor of tropical storms and hurricanes from June to November.

For these types of events, estimates of rainfall from instruments on geostationary platforms such as the Geostationary Operational Environmental Satellite (GOES) are preferred over microwave-based estimates of rainfall from Low-Earth-Orbiting (LEO) platforms because of the rapid refresh (every 15 minutes) over the Continental United States (CONUS) and nearby regions and very short data latency times of GOES data relative to low-Earth orbit data. Numerous algorithms have been developed to estimate precipitation from GOES-based satellite data. The current generation of algorithms produced at the National Oceanic and Atmospheric Administration (NOAA) National Environmental Satellite, Data and Information Service (NESDIS) are the Hydro-Estimator (HE, [1]), GOES Multi-Spectral Rainfall Algorithm (GMSRA, [2]), and the Self-Calibrating Multivariate Precipitation Retrieval (SCaMPR, [3]). The HE relies on GOES data from the infrared (IR) window channel (10.7  $\mu\text{m}$ ) with a fixed relationship to rainfall rates; similarly, Palmeira et al. [4] presented a self-consistent algorithm for rainfall estimation based on GOES data plus lightning data in Brazil. The GMSRA uses additional data from three other GOES channels and updates its calibration in real time based on matches with radar rain rates. SCaMPR calibrates GOES IR parameters against passive microwave rain rates, which is an approach similar to Kidd et al. [5] and the Precipitation Estimation from Remotely Sensed Information using Artificial Neural Network (PERSIANN, [6]) algorithm. PERSIANN uses a combination of geostationary IR and Tropical Rainfall Measuring Mission (TRMM) microwave information to estimate rainfall rate in an hourly basis at spatial resolution of 0.25°. Another algorithm called the CPC Morphing Algorithm (CMORPH, [7]) also combines IR data and microwave rain rates, but uses the IR data as the basis for interpolating the microwave rain rates in time between low-Earth orbit satellite overpasses.

The HE, which will be the focus of this paper, also uses information from numerical weather prediction models to estimate rain rate [1]. Rainfall rates are adjusted upward or downward for moist or dry environments as indicated by National Centers for Environmental Prediction (NCEP) North American Model (NAM) or Global Forecast System (GFS) total column precipitable water and mean-layer relative humidity for the lowest third of the model vertical domain. Another adjustment enhances rainfall rates in regions where the convective equilibrium level temperature is relatively high; i.e., regions where very cold cloud tops are not thermodynamically possible but where strong updrafts and heavy rainfall can still occur. Finally, low-level winds and digital topography are combined to produce enhancements of rainfall rates in upslope regions and reductions in downslope regions, using a technique described in Vicente et al. [8].

The HE has been the operational satellite rainfall algorithm of the National Environmental Satellite, Data, and Information Service (NESDIS) since 2002 and produces rainfall estimates at the full spatial and temporal resolution of GOES over the CONUS and surrounding regions, including PR; real-time estimates are also produced on an experimental basis for the rest of the globe. However, validation of the Hydro-Estimator has generally focused on the CONUS (e.g., [1] and [9]) and has not been performed over Puerto Rico, and given the differences in topography and climate of Puerto Rico relative to the CONUS, previous validation efforts may not necessarily be relevant to users in PR. Furthermore, validation of the HE over PR may illuminate opportunities to enhance the algorithm for application over PR.

Validation of the rainfall retrieval algorithm consists of comparing the rainfall estimates with corresponding observations (rain gauges in this study). The accuracy of rainfall estimates can be measured by decomposing the rainfall process into sequences of discrete and continuous random variables; i.e., the presence or absence of rainfall events (discrete variable) and the amount of rainfall (continuous variable). The occurrence of rainfall events in a given area and at a particular time follows a Bernoulli process and consequently the estimation accuracy of rainfall events can be conducted by analyzing a contingency table. The typical scores that measure the accuracy of categorical forecasts are: hit rate (H), probability of detection (POD), false-alarm rate (FAR), and discrete bias (DB). The continuous validation strategy focuses on the amount of rainfall that occurred at specific area in a particular time and the continuous measurements of accuracy are mean absolute error (MAE), root mean squared error (RMSE), and continuous bias (CB).

The second section of this paper describes the data collection process and sources of information. The third section describes the conventional statistical techniques used to perform validation. The fourth section presents validation results during heavy storms over PR, and includes a comparison for rain gauges versus HE and rain gauges versus NEXRAD. The fifth section presents the NEXRAD bias due to distance from the radar. The sixth outlines some strategies for algorithm improvements. The seventh section presents some conclusions.

## 2. Data collection

Puerto Rico has a rain gauge network that collects rainfall measurements every 5, 10, 15, 30 or 45 minutes and includes 125 rain gauges with data available since January 2000. Since the majority of gauges collect rainfall every 15 minutes a computer program was designed to match these data with HE and NEXRAD data at 15-minute resolution for validation. The data set used for validation includes five heavy storms that have been impacted PR: Three can be characterized as a cold front and two as tropical storms.

NEXRAD data over Puerto Rico come from a WSR-88D unit located in Cayey (18.12°N, 66.08°W, 886.63 m elevation). The radar frequency is 2.7 GHz and the maximum horizontal range is 462.5 km, and the radar scans the entire island every 6 minutes. The NOAA National Severe Storms Laboratory (NSSL) conducted a significant effort to make possible an affordable nationwide operational capture, distribution, and archive of Level II NEXRAD data [10]. Unfortunately, for Puerto Rico the Level II data are available only until 2002 [11]. The NWS did resume archiving level II data for PR during the summer of 2007. On the other hand, Level III data for PR are available continuously since 2000 [12], so the Level III data were selected to perform validation since the most recent and catastrophic floods over PR occurred after 2002. The scanning angle for reflectivity data was selected as 0.5 degrees for this research in order to avoid beam overshoot over western PR. Fig. 1 shows the location of the radar and the spatial distribution of the rain gauges.

As mentioned in the Introduction, the HE uses satellite IR window (10.7- $\mu$ m) data and numerical weather prediction data to estimate rainfall over the CONUS and PR every 15 minutes at 4 km spatial resolution, and they are available for the entire period of interest. In order to ensure consistency among these data sets during the comparison, both the NEXRAD and HE rain rates were aggregated in time over the corresponding 15-minute accumulation period of the gauges.

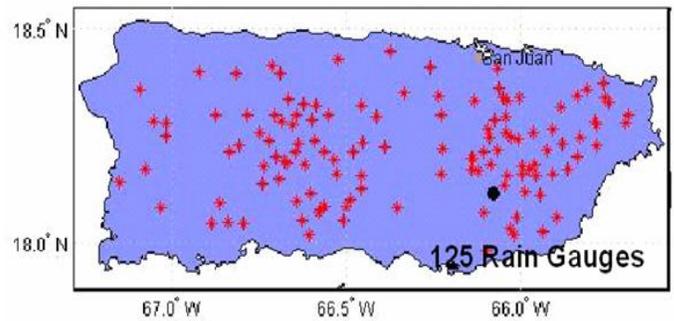


FIG. 1. Location of rain gauges (red stars) and NEXRAD (black dot) in PR.

## 3. Validation techniques

Validation of the rainfall retrieval algorithm consists of comparing the rainfall estimates with observations over the same time and space. The accuracy of rainfall estimates can be measured by decomposing the rainfall process into sequences of discrete and continuous random variables; i.e., the presence or absence of rainfall events and the amounts of rainfall. The occurrence of rainfall events in a given area and at a particular time follows a Bernoulli process and consequently the estimation accuracy of rainfall events can be conducted by analyzing contingency tables and the bivariate probability distribution of rainfall events [13]. Table 1 shows the classical two-way contingency table.

It is assumed that the values provided by the rain gauges are the “ground truth” while the HE and the NEXRAD provide estimated rainfall values. The variable  $a$  in the contingency table is the number of times that the rain gauge identifies a rainfall event and the estimator also correctly identifies a rainfall event at the same time and location. The variable  $d$  represents the number of times the rain gauge does not observe a rainfall event and the estimator correctly determines that there is no rainfall event. The variable  $b$  indicates the number of times the rain gauge does not observe a rainfall event but the estimator incorrectly indicates that there is a rainfall event. The variable  $c$  shows the number of times that the rain gauge detects a rainfall event but the estimator incorrectly does not detect the rainfall event.

TABLE 1. Sample contingency table.

		Observed rainfall (Rain gauge)	
		Yes	No
Estimated rainfall (HE or NEXRAD)	Yes	$a$	$b$
	No	$c$	$d$

The typical scores that measure the accuracy of categorical estimation are:

$$H = \frac{a+d}{n_o}, \quad \text{where } n_o = a+b+c+d \quad (1)$$

$$POD = \frac{a}{a+c} \quad (2)$$

$$FAR = \frac{b}{a+b} \quad (3)$$

$$DB = \frac{a+b}{a+c} \quad (4)$$

where  $H$  is the hit rate,  $POD$  is the probability of detection,  $FAR$  is the false-alarm rate, and  $DB$  is the discrete bias. Hit rate is the fraction of the  $n_o$  estimating occasions when the categorical estimation correctly determines the occurrence of rainfall event or nonevent. Probability of detection is the likelihood that the event would be estimated, given that it occurred. The false-alarm rate is the proportion of estimated rainfall events that fail to materialize. Bias is the ratio of the number of estimated rainfall events to the number of observed events [13].

The continuous validation strategy consists of comparing the amount of rainfall that occurred with the estimated amount of rainfall at specific area in a particular time and the continuous accuracy scores used here are:

$$e_{ij} = y_{ij} - \hat{y}_{ij} \quad i=1, \dots, n \quad \text{and} \quad j=1, \dots, m \quad (5)$$

$$MAE = \frac{1}{n \ m} \sum_{i=1}^n \sum_{j=1}^m |e_{ij}| \quad (6)$$

$$RMSE = \sqrt{\frac{1}{n \ m} \sum_{i=1}^n \sum_{j=1}^m e_{ij}^2} \quad (7)$$

$$CB = \frac{\sum_{i=1}^n \sum_{j=1}^m \hat{y}_{ij}}{\sum_{i=1}^n \sum_{j=1}^m y_{ij}} \quad (8)$$

where  $y$  and  $\hat{y}$  are the observed and estimated amount of rainfall. The  $i$  and  $j$  subscripts represent time and space, respectively. The constant  $n$  is the total number of time intervals for a given storm, and  $m$  is the number of rain gauges that are collecting rain during a storm. The error  $e$

is the deviation between the observed and estimated amount of rainfall at a particular time and space and is computed only when at least one of  $y$  or  $\hat{y}$  is greater than zero.  $MAE$  is the mean absolute error,  $RMSE$  the root mean squared error, and  $CB$  is the continuous bias.

## 4. Validation results

### 4.1 Discrete validation

A contingency table was computed for each rain gauge during a given storm and the scores of those tables were summarized to create contingency tables for each storm for the HE and NEXRAD. The contingency tables were used to compute the validation scores, which measure the accuracy of the estimation and are given in Tables 2a) and 2b). The HE significantly underestimates the number of raining pixels in the three April-May events (DB of 0.49 to 0.52) but strongly overestimates the November-December events (DB of 1.54 and 2.15). The physical reasons behind this apparent strong seasonal variation in DB are not known at this time. Meanwhile, the NEXRAD had a consistent dry bias (0.62-0.68) for the last four events but virtually no bias (1.02) for the first; again, it is not clear at this time what led to such a significant difference. The hit rates of the HE range from 0.62 to 0.91 with an average of 0.76 and NEXRAD has a range from 0.82 to 0.95 with average of 0.87. Although, both HE and NEXRAD exhibit relatively high hit rate, the HE has a lower percentage of correct rain / no rain estimates than does the NEXRAD. The probability of detection of the HE ranges from 0.14 to 0.57 with an average value of 0.36, whereas, the NEXRAD shows a range from 0.4 to 0.74 with an average of 0.52. Thus, the HE correctly detected a smaller percentage of the observed rainfall events (36%) than did NEXRAD (52%) for these events. The false alarm rate for the HE varies between 0.39 to 0.73 with an average value of 0.61, meanwhile the NEXRAD varies from 0.25 to 0.35 with an average of 0.29. Thus, the false alarm rate was actually higher for the HE (61%) than for NEXRAD (29%). Overall, the discrete validation shows that the NEXRAD outperforms the HE in terms of correct rain / no rain estimates.

### 4.2 Continuous validation

The accumulated rainfall across the island was computed to compare the observed and the estimated rainfall:

$$Y_i = \sum_{j=1}^m y_{ij} \quad i = 1, 2, \dots, n \quad (9)$$

where  $Y_i$  is the total rainfall recorded by all 125 rain gauges across the island or the closest HE or radar pixels at the  $i^{\text{th}}$  time.

TABLE 2a. Discrete validation scores for the Hydro-Estimator.

	17 Apr. 2003	19-21 May 2003	11-18 Nov. 2003	5 Dec. 2003	20 Apr. 2005	Avg.
DB	0.49	0.52	1.54	2.15	0.52	1.04
HR	0.70	0.91	0.68	0.62	0.86	0.76
POD	0.30	0.14	0.55	0.57	0.23	0.36
FAR	0.39	0.72	0.64	0.73	0.56	0.61

TABLE 2b. Discrete validation scores for the NEXRAD.

	17 Apr. 2003	19-21 May 2003	11-18 Nov. 2003	5 Dec. 2003	20 Apr. 2005	Avg.
DB	1.02	0.68	0.66	0.62	0.67	0.73
HR	0.82	0.95	0.84	0.85	0.91	0.87
POD	0.74	0.51	0.47	0.40	0.49	0.52
FAR	0.27	0.25	0.29	0.35	0.27	0.29

Tables 3a) and 3b) show the continuous validation scores for HE and NEXRAD, respectively. The continuous bias of the HE is even more seasonally variable than the DB, with values ranging from 0.16-0.26 for the April-May storms and 1.68-2.42 for the November-December events. The lower CB relative to the DB for the April-May storms suggests that the HE is underestimating the conditional rainfall rates in addition to the spatial extent of the rainfall, while the opposite is happening for the November-December events. The NEXRAD has nearly no continuous bias for two storms and a strong dry bias for three (0.41-0.68), albeit with no apparent seasonal pattern like the HE. As a result, both the mean absolute error and root mean squared error of the HE are also higher than that of NEXRAD.

TABLE 3a. Continuous validation scores for the Hydro-Estimator.

	17 Apr. 2003	19-21 May 2003	11-18 Nov. 2003	5 Dec. 2003	20 Apr. 2005	Avg.
CB	0.26	0.23	1.68	2.42	0.16	0.95
MAE (mm)	1.33	0.74	1.10	0.86	0.79	0.96
RMSE (mm)	2.73	2.10	2.24	1.93	1.71	2.14

TABLE 3b. Continuous validation scores for NEXRAD.

	17 Apr. 2003	19-21 May, 2003	11-18 Nov. 2003	5 Dec. 2003	20 Apr. 2005	Avg.
CB	1.02	0.68	0.41	0.42	1.01	0.71
MAE (mm)	1.02	0.66	0.85	0.53	0.80	0.77
RMSE (mm)	1.91	1.79	1.78	1.15	1.68	1.66

## 5. NEXRAD bias

Radar measurements over the western part of PR are frequently inaccurate. This is because reflectivity measurements are conducted at about 2000m above the surface as a result of the elevated location of the radar and a relatively high scan angle which was selected to minimize beam block by nearby mountains. In order to estimate the NEXRAD bias, the following validation exercise was conducted. PR was divided in three zones. The first zone includes the rain gauges that are located in a radius of equal or less that 35km, the second region includes stations that are in the radii that is larger than 35km but equal and smaller than 90km, and the third region consists of stations at a range larger than 90km from the location of the NEXRAD. Figure 2 shows the study zones, which were designed to provide an appropriate sample size to derive reliable statistics.

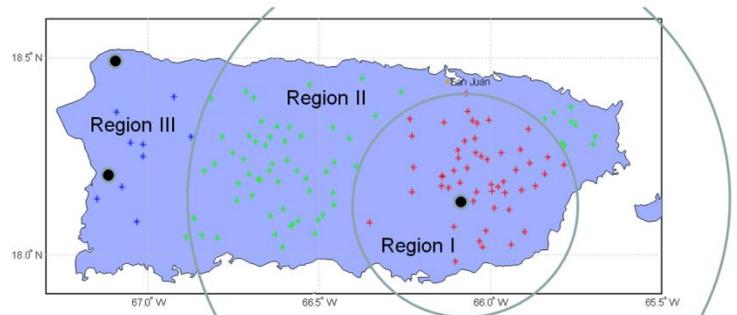


FIG. 2. Location of rain gauges (stars) and NEXRAD (black dot on Region I) in PR. Black dots in Region III are small and high resolution radar that will be used to derive the bias correction factor for NEXRAD. The radii of the circles are 35km and 90km.

An unnamed tropical storm, which becomes stationary over the PR area during November 11-18, 2003, was studied to determine the NEXRAD bias over the designed zones. The continuous red lines in Figures 3a, 3b and 3c show the cumulative rainfall recorded every 15 minutes by all gauges of PR rain-gauge network. The horizontal axis shows the Julian day and the vertical axis shows the 15-minutes accumulated rainfall in mm. The blue line represents the 15-minutes accumulative rainfall recorded by the radar pixel that is the closest to each rain gauge. The difference between the red and blue lines represents the estimation error of the accumulative rainfall. Figures 3a and 3b show reasonable rainfall estimation by the radar. However, Figure 3c shows that the NEXRAD exhibits a significant underestimation in Region III. The corresponding scatter plots in Figures 4a, 4b, and 4c show the actual rainfall amount recorded by the individual gauges versus the estimates from the radar pixels. These figures also confirm that although Region III generally experiences lighter rainfall events than in the other two regions, the NEXRAD bias is largest in this region.

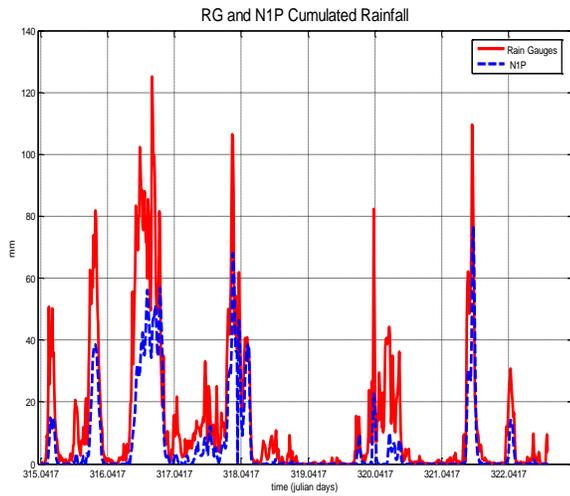


FIG. 3a. Cumulative rainfall during November 11-18, 2003, over Region I.

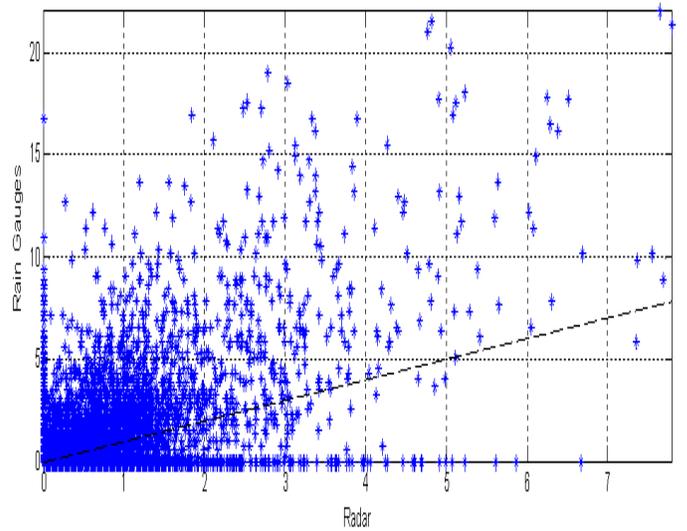


FIG. 4a. Scatter diagram for rain gauges and NEXRAD pixels during November 11-18, 2003 for Region I.

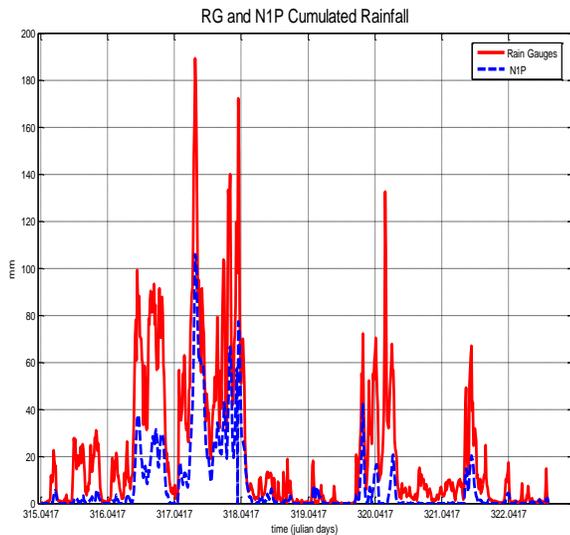


FIG. 3b. Cumulative rainfall during November 11-18, 2003 for Region II.

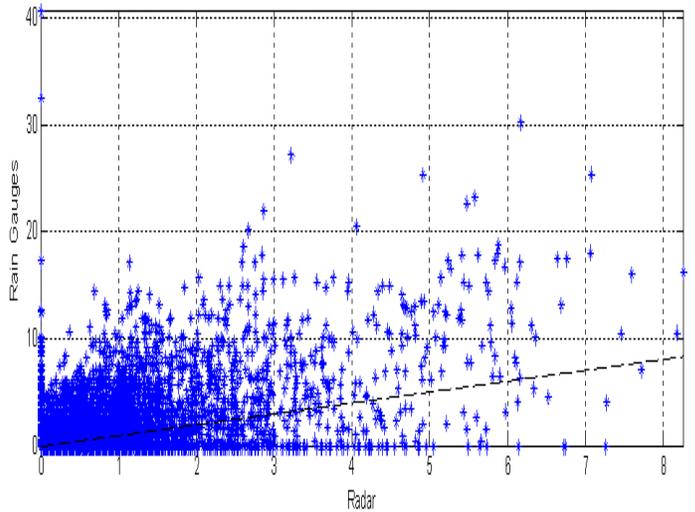


FIG. 4b. Scatter diagram for rain gauges and NEXRAD pixels during November 11-18, 2003 for Region II.

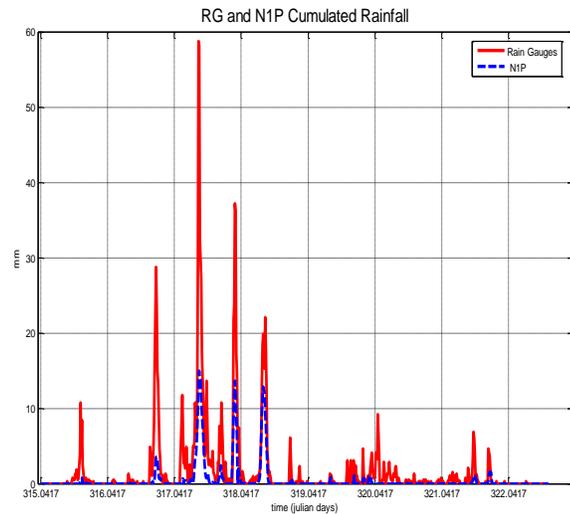


FIG. 3c. Cumulative rainfall during November 11-18, 2003 for Region III.

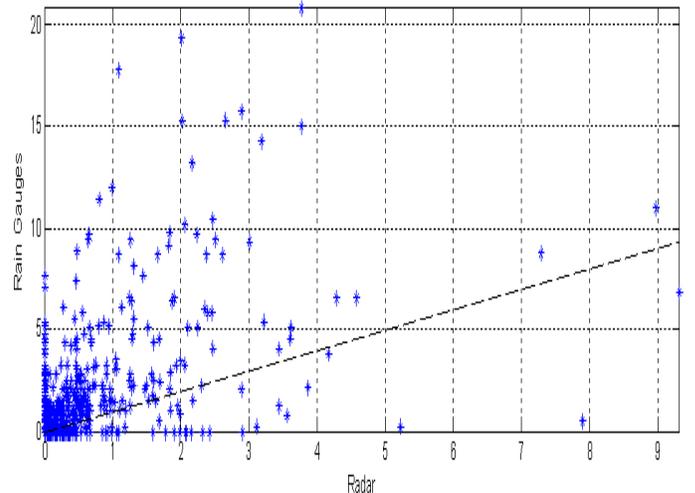


FIG. 4c. Scatter diagram for rain gauges and NEXRAD pixels during November 11-18, 2003 for Region III.

Table 4 shows that the probability of detection increases with distance from the NEXRAD. Figures 3a, 3b and 3c show that the NEXRAD exhibits underestimation in the three regions; however, the underestimation is larger in Region III. Table 4 shows that the bias ratio become smaller, which indicates that the estimation error becomes worse for larger distances between the station and radar. Although, the dry bias actually is stronger in Zone II than in Zone III

TABLE 4a. Discrete comparison of NEXRAD performance for each region.

	Region I (0-35 km from NEXRAD)	Region II (35-90 km from NEXRAD)	Region III (>90km from NEXRAD)
DB	0.74	0.64	0.46
H	0.83	0.83	0.80
POD	0.50	0.46	0.37
FAR	0.32	0.27	0.29

TABLE 4b. Comparison of NEXRAD performance

	Region I (0-35 km from NEXRAD)	Region II (35-90 km from NEXRAD)	Region III (>90km from NEXRAD)
MAE	0.92mm	1.07mm	1.06mm
RMSE	1.76mm	2.07mm	2.18mm
CB	0.45	0.35	0.37

## 6. Algorithm Improvements

### 6.1 Rainfall detection

As stated previously, the HE uses GOES brightness temperatures ( $T_b$ ) from channel 4 ( $10.7 \mu\text{m}$ ) to discriminate raining from non-raining events [1]. During the validation exercise we noted that there are some warm-top convective events that are not detected by the HE. The HE generally produces little or no rainfall for brightness temperatures exceeding 235K; however, there are numerous events in PR where rainfall was in fact observed at these temperatures. For instance, Fig. 5 shows the observed accumulated rainfall for all gauges located in PR (red line) and the accumulated rainfall by the corresponding HE pixels (blue line) on November 14, 2006. The horizontal axes shows the time every 15 minutes and the vertical axis exhibits the accumulated rainfall in mm. Fig. 6 shows the distribution of brightness temperatures over the GOES pixels corresponding to

gauge locations during this storm and there are few pixels below 235 K; a comparison with Fig. 5 indicates that the poor detection by the HE was at least in part because it was not calibrated to produce rainfall from relatively warm clouds. In order to improve the detection skill of the HE, we plan to examine the differences in brightness temperature between  $10.7 \mu\text{m}$  and the water vapor band ( $6.5 \mu\text{m}$  in GOES). Positive values of the WV-infrared window temperature difference have been shown to correspond with convective cloud tops that are above the tropopause (i.e. overshooting tops), ([14 and [15]). Convective clouds with positive differences indicate the possibility of warm-top convection.

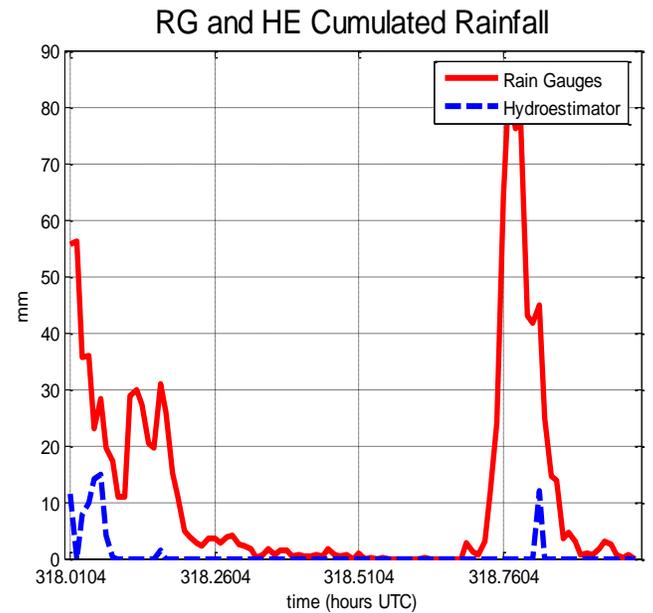


FIG. 5. Comparison between observed and estimated accumulated rainfall (Nov. 14, 2006).

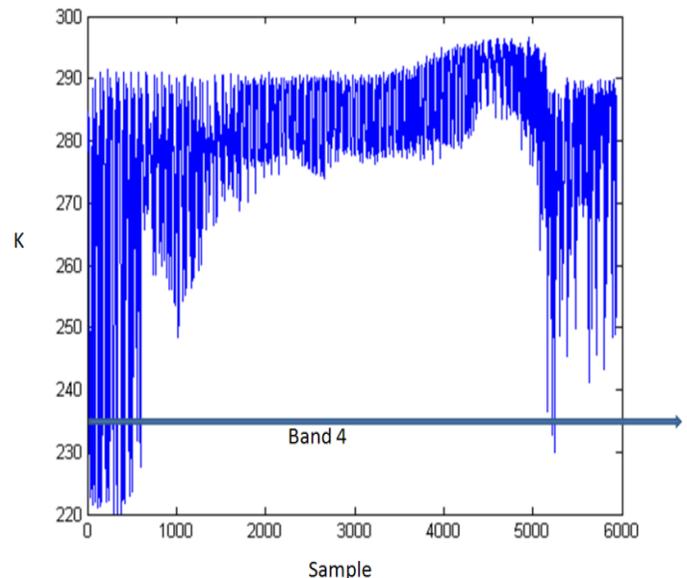


FIG. 6. GOES-12 brightness temperature from channel 4 (Nov. 14, 2006).

It is known that precipitation processes in clouds with warm tops are very sensitive to the microphysical structure of their tops. Specifically, precipitation processes are more efficient when water droplets or/and ice particles grow to larger sizes. It has been shown that the uses of the reflected portion of the near-IR during the daytime indicates the presence large cloud-top particles and suggest rain in warm-top clouds. It has been used the effective radius of clouds particles derived from the AVHRR 3.75- $\mu\text{m}$  window channel to detect warm raining clouds ([16], and [17]). This concept was also applied to rainfall estimation from GOES data in the GMSRA [2].

Preliminary work was conducted to explore improving the HE warm rainy-cloud detection using the GOES band 2 (3.9  $\mu\text{m}$ ) reflectance during the daytime. This will be used as a proxy for cloud-top particle size to identify any correlation with the presence or absence of rain from warm-topped clouds over PR. In this work we present the estimation of daytime reflectance of band 2.

It is assumed that during the daytimes the total radiance measured by GOES band 2 (3.9  $\mu\text{m}$ ) is composed by the sum of emitted radiances and the reflected radiances.

$$T_{3.9,d} = E_{3.9,d} + R_{3.9,d} \quad (10)$$

where  $T_{3.9,d}$  is the total radiance during the day,  $E_{3.9,d}$  is the emitted radiance, and  $R_{3.9,d}$  is the reflected radiance of band 2 during the day. However during the night since the sun is not present the total radiance is equal to the emitted radiances, as shown as follows:

$$T_{3.9,n} = E_{3.9,n} \quad (11)$$

An empirical equation can be developed to estimate the emittance measured by band 2. The emittance during the night it is assumed to be a function of the radiance measured by bands 3 (6.9  $\mu\text{m}$ ) and band 4 (10.7  $\mu\text{m}$ ). The general relationship may be expressed as follows:

$$E_{3.9} = f(T_{6.9}, T_{10.7}), \quad (12)$$

where  $E_{3.9}$  is the emittance of band 2,  $T_{6.9}$  is the total radiance of band 3, and  $T_{10.7}$  is the total radiance of band 4. A linear relationship was assumed first and the performance of the model will indicate whether or not a linear model is appropriate. Thus, the postulated model is as follows:

$$\hat{E}_{3.9,n} = \hat{a}_0 + \hat{a}_1 T_{6.9,n} + \hat{a}_2 T_{10.7,n}, \quad (13)$$

where  $\hat{E}_{3.9,n}$  is the estimated emittance of band 2 during the night,  $T_{6.9,n}$  is the total radiance of band 3, and  $T_{10.7,n}$  is the

total radiance of band 4 during the night, and the  $\hat{a}$ 's are the parameters of the linear equation.

The parameters were estimated using a severe rainfall event that occurred on October 27-29, 2007. The data set was divided in two parts: the first part (October 27-28) was used to estimate the parameters and the second part (October 28-29) for validation. Data from October 28 was divided in two separate time series the first part for model fitting and the second for validation. The parameter estimation results are summarized in Table 5.

TABLE 5. Parameter estimation

Parameter	Estimate
$a_0$	-0.69348
$a_1$	0.083468
$a_2$	0.024352

The second part of the data was used to perform validation. The mean absolute error (MAE) and the coefficient of multiple determination ( $R^2$ ) were computed to measure the accuracy of equation (13) and were found to be  $\text{MAE}=0.0389\text{mW}/(\text{m}^2\text{-sr}\text{-cm}^{-1})$  and  $R^2=0.92$ . A quadratic model was also fitted to measure if a significant improvement can be obtained. However, the quadratic model provides  $R^2=0.93$ , and consequently, these results show that the selected linear model sufficiently represents the estimated reflectance. Figures 7 and 8 show a comparison between the observed and estimated emittance during the nighttime.

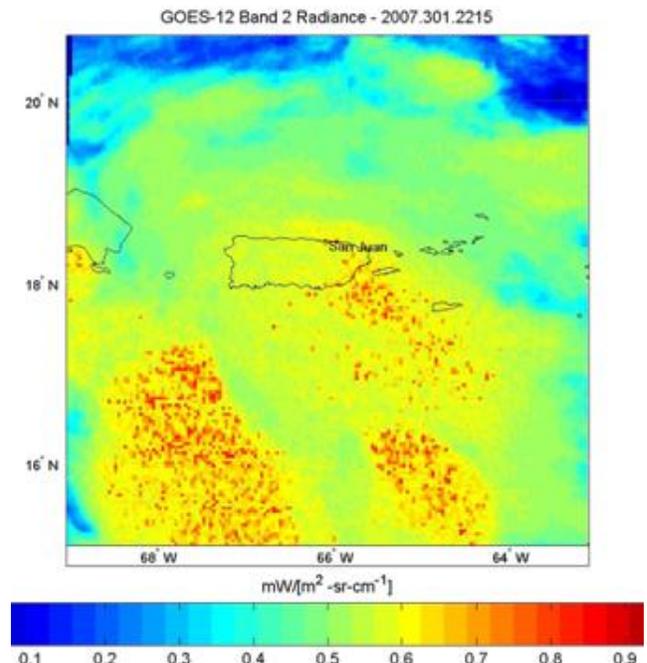


Figure 7 Observed emittance of band 2 for a nighttime image.

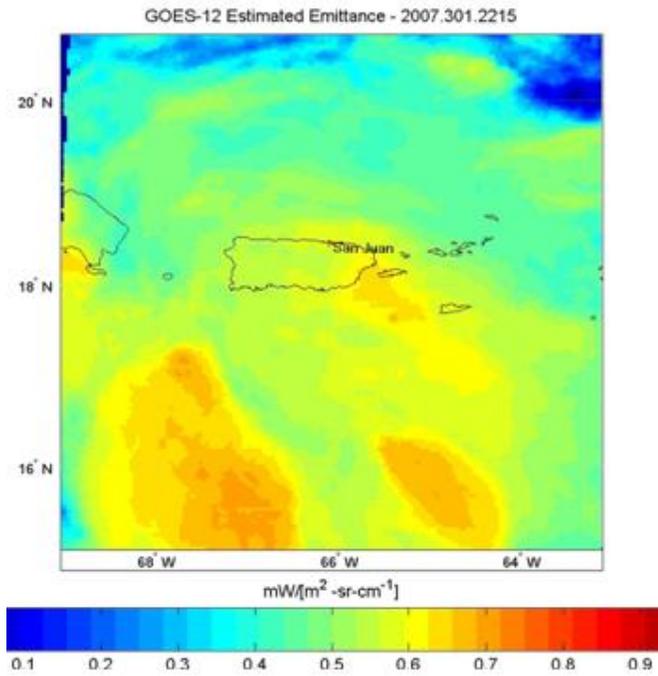


Figure 8. Estimated emittance of band 2 for the same image as in Figure 7.

Assuming that equation (13) also holds during the daytime, the emittance of band 2 can be estimated as follow:

$$\hat{E}_{3,9,d} = \hat{a}_0 + \hat{a}_1 T_{6,9,d} + \hat{a}_2 T_{10,7,d} \quad (14)$$

where the subscript  $d$  refers to variables observed during the daytimes and the regression coefficients are obtained from equation (13). Figure 9 shows the estimated emittance which will be subtracted from the observed radiance during daytime of band 2 and compared to corresponding rain / no rain areas to determine its usefulness in discriminating raining areas in relatively warm clouds. Figure 10 shows the observed reflectivity (converted to rainfall rates) for the same rainfall event.

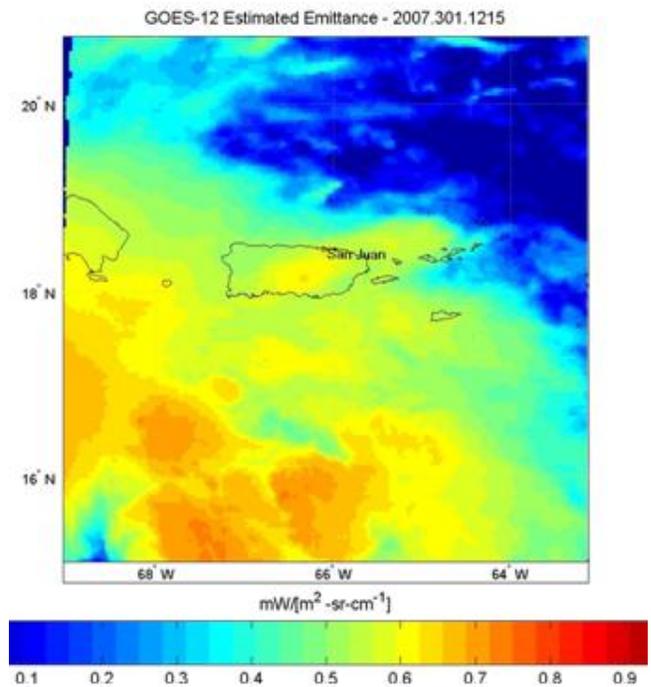


Figure 9 Estimated emittance of band 2 during the day

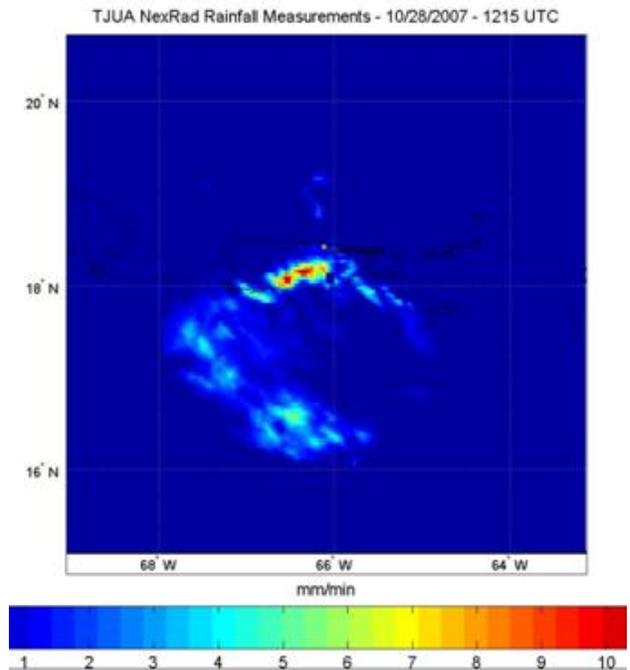


Figure 10. Estimated rainfall from NEXRAD.

## 6.2 Improving rain rate estimates

The rainfall retrieval procedure of the HE is also mainly based on the relationship between the brightness temperature ( $10.7 \mu\text{m}$ ) and observed rain rate. Estimation of the amount of rainfall may be improved by classifying the brightness temperature patterns (BTP) with the corresponding rain formation processes. The following channels will be used to classify the BTP with the corresponding rain process. Channel 1 ( $0.65 \mu\text{m}$ ) will be used to classify the events according to the cloud optical thickness. The reflected portion of channel 2 ( $3.9 \mu\text{m}$ ) during the daytime will be used as an indirect measurement of the cloud drop size distribution, thermodynamic phase, and particle shape [18]. Channel 4 ( $10.7 \mu\text{m}$ ) will be used to classify the rainfall events according to temperature. Brightness temperature differences will also be used to develop the classification algorithm: The difference between the  $10.7\text{-}\mu\text{m}$  and  $3.9\text{-}\mu\text{m}$  brightness temperatures will be useful to determine whether a cloud top is composed of liquid water or ice. As stated previously, the IR-WV difference ( $6.5\text{--}10.7 \mu\text{m}$ ) is usually negative; however, convective clouds with positive differences have likely already begun to precipitate, especially in tropical atmospheres that support warm top convection. The  $13.3\text{--}10.7 \mu\text{m}$  differencing technique is used to characterize and delineate cumulus clouds.

There are a large number of successful applications of classification algorithms reported in the literature. It has been shown that fuzzy neural networks (FNNs) provide a new approach for classification of multispectral data and to extract and optimize classification rules, they applied these algorithms to classify pixels in multispectral images and to extract fuzzy classification rules [19]. A classification neural network algorithm was successfully used to perform image texture classification [20]. Xiao and Zhang [21] and Xiao et al [22] used neural networks, rough sets, and support vector machine to classified remote sensing images. Rodriguez et al [23] successfully applied the general types Feed-forward, Self-Organizing Maps (SOM), and Auto-associative Networks. They also implemented Backpropagation algorithm and the Kohonen learning rule to perform star classification.

In this research will focus on convective clouds, and consequently, the factors to be considered for the classification of BTP and rain types are: area, depth, duration, and updraft velocity. Thus, a variable selection algorithm will be used to identify the variables that best explain rainfall variability. The selected variables will be used to develop training patterns for a self-organized artificial neural network, which will be used to identify a set of homogenous groups that reveal similarities within

the member of a class, but different among the classes. The Kohonen learning rule will be used to determine the optimal weights of the artificial neural network ([23], [25], [26], [27] and [28]).

## 7 Summary and conclusions

The HE is a high resolution satellite rainfall retrieval algorithm run operationally by NOAA/NESDIS that provides estimates of rainfall every 15 minutes at 4-km resolution over the CONUS and nearby areas including PR. (Global estimates are also produced in real time on an experimental basis.) The rain rates are primarily derived from GOES  $10.7\text{-}\mu\text{m}$  brightness temperatures and then adjusted using parameters derived from a numerical weather prediction model. The HE estimates should be especially useful over regions of complex topography such as western PR because of the difficulties associated with radar in those regions such as beam block. However, for the very small sample of heavy rainfall events examined in this paper, NEXRAD clearly outperforms the HE, perhaps in part because of most of the rainfall events were located in the central and eastern parts of the island where the radar data will be most reliable. Specifically, the HE underestimates both the number of rainfall events and the amounts of rainfall, whereas NEXRAD is nearly unbiased in these respects. The HE algorithm does exhibit a satisfactory hit rate, but a very low probability of detection and a large false alarm rate that is surprisingly higher than that of NEXRAD despite the dry bias of the HE. A research effort is undergone to improve the performance of the HE for PR; specifically, the algorithm proposed by Ramirez-Beltran et al. [24] will be implemented to improve the HE rainfall detection and the equation that relates brightness temperatures with rain rates.

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