# Thermodynamic Analyses for Optimizing the Design of HTGR's Helium Brayton Cycles

FLORIN ALEXE, and VICTOR CENUSA Power Engineering Department, Power Generation and Use Chair "Politehnica" University of Bucharest Splaiul Independentei 313, Sector 6, Bucharest ROMANIA florin.alexe@energ.pub.ro http://www.energ.pub.ro

Abstract: - The paper analyzes the close-circuit Brayton (Joule) cycles for High Temperature Gas (Helium) cooled nuclear Reactors (HTGR). Analyzed cycles are with Regenerative Heat Exchanger (RHE), Fragmented Compression and Inter-Cooling (FC&IC). The HTGR imposes the working agent and hot source's parameters. The cooling conditions give the cycle's minimal temperature. In the 1<sup>st</sup> paper's section, for ideal processes cycles, we show that: A) the boundary parameters and design schemes inflict:  $A_{l}$ ) the compression ratios ( $\epsilon$ ),  $A_2$ ) the specific net work per 1 kg He ( $w_{net}$ ), and  $A_3$ ) the thermal efficiencies ( $\eta_{th}$ ); **B**) the performances are increasing with the IC's number. In the  $2^{nd}$  section we are taking into consideration the irreversibility's factors (temperature difference at RHE, revolving machines isentropic efficiencies, and pressure drops) doing sensitivity analyses about their influences on real processes cycle's performances. We show that: 1) cycle's performances are not continuous growing with IC's number, and 2) the main influences on design's option are given by:  $2_1$ ) the temperature difference at RHE and  $2_2$ ) the pressure drops. In the 3<sup>rd</sup> section we adjusted all the quality factors in a similar manner, reducing the irreversibilities, showing the synergic influences. The 4<sup>th</sup> section relaxes the hot source's restrictions. It analyses the influence of HTGR output/input temperatures variation on the main thermodynamic data, showing:  $\alpha$ ) the benefit of maximal temperature increase and  $\beta$ ) the need to correlate HTGR's temperature increment output vs. input with the maximal temperature. The final section contains the main conclusions of the paper.

*Key-Words:* - Brayton Cycle, HTGR, Irreversibility, Sensitivity Analysis, Numerical Computation, and Thermodynamic Optimization.

#### **1** Introduction. Problem Formulation

The paper analyses the performances of single loop close circuit Brayton cycle, using HTGR as hot source. The closed cycle allows using: 1) a clean working agent, with advantageous properties; 2) work pressures not depending from the atmospheric one [1 to 4]. Helium's use in thermodynamic circuits offers the following advantages [1, 2, and 5]: a) it performs as an ideal gas; b) it has a big heating capacity per kg; c) the big sound velocity allows rising the compression and expansion ratios per compressor's / turbine's stages; d) the small viscosity leads to low pressure drops; e) linked with the elevated thermal conductivity it leads to high heat exchange coefficients. For HTGR it is also important the fact that Helium is chemically and radiological inert.

The HTGR imposes: I) the working fluid, II) the hot source inlet/output parameters. The cooling conditions give the cycle's minimal temperature. In a previous paper [4] we analyzed the ideal processes cycles on this kind of boundary conditions.



Fig.1 Brayton cycle with RHE, FC and  $n_{IC \text{ stages}}=1$ 

Our results where showing the low performances of simple cycle, without or with RHE. We continue the analysis only for cycles with RHE, FC&IC (see fig. 1 and 2), starting with ideal processes cycles and continuing with the real processes ones.



Fig.2 Brayton cycle with RHE, FC and n<sub>IC stages</sub>=2

The targets are to envisage the thermodynamic performances of ideal and real processes cycles, in both designs, and to determine the influence of different input data on these performances, in order to choose the optimal design.

#### 2 Analytical Approach

#### 2.1 Ideal processes cycles

In both designs we fixed the hot source's input/output temperatures  $T_a/T_z$ . In order to have the same temperatures at turbine's output and NR's input ( $T_b=T_z$ ), and knowing the Helium's isentropic coefficient ( $\gamma$ ), the turbine's expansion ratio ( $\varepsilon_T$ ), equal with the compression one ( $\varepsilon_K$ ), is [5, and 6]:  $\varepsilon_T = (p_a / p_z) = (T_a / T_z)^{\gamma/(\gamma-1)} = \varepsilon_K$  (1)

At the cold source, we considered the same minimal Helium's temperatures at External Cooler (EC) and IC outputs:

$$T_d = T_f = T_h \tag{2}$$

It is generally accepted [5 to 7] that for FC&IC it is recommendable to equal allocate the compression between stages. The values are depending on intercooling stage's number ( $n_{IC}$ ):

$$\varepsilon_{K t \text{ stage}} = \sqrt[(n_{IC} + 1)]{(p_a / p_b)} = (T_a / T_b) \frac{\gamma}{(n_{IC} + 1) \cdot (\gamma - 1)}$$
(3)

The temperatures at EC and IC output's are:

$$T_{e} = T_{g} = T_{i} = T_{d} \cdot (T_{a} / T_{z})^{[1/(n_{IC} + 1)]}$$
(4)

The general equation for determining the  $\eta_{th}$  of ideal processes RHE, FC and IC cycles became:

$$\eta_{t} = [(T_{a} - T_{z}) - (n_{IC} + 1)(T_{e} - T_{d})]/(T_{a} - T_{z}) =$$

$$= 1 - \frac{T_{y}}{T_{z}} \cdot (n_{IC} + 1) \cdot \frac{(T_{a} / T_{z})^{\frac{1}{n_{IC} + 1}} - 1}{(T_{a} / T_{z}) - 1}$$
(5)

It show that, if  $n_{IC}\rightarrow\infty$ , the cold source's process became isotherm, and it's average temperature ( $T_{csa}$ ), became equal with the minimal one:  $T_{csa}=T_d=T_f=T_h$  (see fig. 3, representing in T-s coordinates the processes in an ideal cycle with  $n_{IC}=2$ ). Conventionally, the technical entropy was considered  $s_0=0$  for  $p_{ref}=10$  MPa, respectively  $T_{ref}=273.15$  K (0 °C).



Fig. 3 T-s diagram of an ideal processes cycle with RHE&FC, with  $n_{IC}$ =2 (fig. 2 design)

The middle hot source's temperature  $(T_{hsa})$ , could be determined as a logarithmic average:

$$-T_{z})/\ln(T_{a}/T_{z})$$
(6)

The maximal thermal efficiency, allowing fully using the hot source's exergetic potential [5 to 7], is:  $\eta_{\text{max t (IC=\infty)}} = 1 - T_y \cdot [\ln(T_a / T_z)]/(T_a - T_z)$  (7)

#### 2.2. Real Processes Cycles.

 $T_{hsa} = (T_a)$ 

We continue to consider Helium as ideal gas, but we are taking into account the processes irreversibility [5 to 9], due to:

a) The temperature difference, characterizing the exergetic degradations by heat exchange into RHE,  $\Delta T$ , same at the warm and cold ends:

$$\Delta T = (T_b - T_{z_i}) = (T_c - T_g)_{n_{1C=1}} = (T_c - T_i)_{n_{1C=2}}$$
(8)

b) The entropy grows in the compressors and turbine's processes. They are computed starting from isentropic efficiencies:

$$\eta_{\text{is T}} \quad \eta_{\text{is T}} = (T_a - T_{b \text{ real}}) / (T_a - T_{b \text{ theoretic}})$$
(9)

$$\eta_{is K} = (T_{e \text{ theoretic}} - T_d) / (T_{e \text{ real}} - T_d)$$
(10)

c) The relatively pressure drops in NR, RHE, EC, IC, and pipes. With the notation:

$$\Delta p_{rel} = (p_{output} - p_{input}) / \sqrt{p_{input} \cdot p_{output}}$$
(11)

the improper fraction for pressure drops R is:

$$R = (p_{output} / p_{input}) = \{2 / [\sqrt{(4 + \Delta p_{rel}^2) - \Delta p_{rel}}]\}^2 (12)$$

For real processes cycles with RHE, FC&IC, the turbine's real output temperature  $(T_{b\,r})$  should be with  $\Delta T$  bigger than the NR input one:

$$T_{br} = T_z + \Delta T \tag{13}$$

The turbine's theoretic outlet temperature is: T = T = (T = T = AT)/2

$$\mathbf{I}_{bt} = \mathbf{I}_a - (\mathbf{I}_a - \mathbf{I}_z - \Delta \mathbf{I}) / \mathbf{I}_{is Tb}$$
(14)

We obtain the turbine's real expansion ratio:

$$\varepsilon_{\text{Tb r}} = \{T_a / [T_a - (T_a - T_z - \Delta t) / \eta_{\text{is Tb}}]\}^{[\gamma/(\gamma-1)]}$$
(15)  
Considering the same relatively pressure drops

Considering the same relatively pressure drops for NR, RHE, EC, and IC:

$$\mathbf{R}_{\mathrm{RN}} = \mathbf{R}_{\mathrm{RHE}} = \mathbf{R}_{\mathrm{EC}} = \mathbf{R}_{\mathrm{IC}} = \mathbf{R} \tag{16}$$

we obtain the global compression fraction (define as a ratio between the last stage output pressure and the first stage input pressure):

$$\varepsilon_{K r gl} = p_g / p_d = p_i / p_d = \varepsilon_{Tb r} \cdot R^{3 + n_{IC}}$$
(17)

The identical compression ratios per one stage will depend on: a) relatively pressure drops on IC, and b) the IC number:

$$\varepsilon_{\text{K r stage}} = \sqrt[(n_{\text{IC}} + 1)]{\varepsilon_{\text{K r global}} \cdot \mathbf{R}^{n_{\text{IC}}}}$$
(18)

It allows calculating the compressors outlet real temperatures:

$$T_{e} = T_{g} = T_{i} = T_{d} \cdot [1 + (\epsilon_{K \text{ stage}}^{(\gamma - 1)/\gamma} - 1)/\eta_{is K}]$$
(19)

For low pressure Helium, the RHE's output / EC's input temperature should be bigger with  $\Delta T$  than the last compressor's output one:

$$T_{c} = T_{d} \cdot \left[1 + \left(\frac{\varepsilon_{K \text{ stage}}^{(\gamma-1)/\gamma} - 1\right)}{\eta_{\text{is } K}}\right] + \Delta T$$
(20)

Finally we are determining the work and heat exchanges for each process, and the real thermal efficiencies of analyzed cycles.

#### **3** Numerical Solution for Given Data

The main conclusion of real cycle's analysis is that the boundary restrictions on NR and cold source, cumulated with data describing the irreversibility ( $\eta_{is K}$ ,  $\eta_{is T}$ ,  $\Delta T$ , and  $\Delta p_{rel}$ ), leads for each scheme at imposed values of: **1**) expansion / compression ratios, and **2**) real thermal efficiencies. It is difficult and irrelevant comparing the performances of different designs only on formulas. We did computations with a typical set of input data [1, 2]:

- \* For the RN we have:  $p_z=7.2$  MPa,  $T_z=840$  K (566.85 °C),  $T_a=1.200$  K (986.85 °C).
- \* For the cold source,  $T_d=T_f=T_h=305$  K (31.85 °C), is restricted by the cooling water temperature.
- \* For characterizing the irreversibility we considered: **a**)  $\Delta T_{RHE ref}=35$  K, as a fraction from the geometric average cycle's temperature, see relation (17), **b**)  $\eta_{is K ref}=\eta_{is T ref}=0.91$ , respectively **c**)  $\Delta p_{rel ref}=3.16 \%$  (R=p<sub>output</sub>/p<sub>input</sub>=1.03213).

 $\Delta T_{\text{HRE ref}} = (1/16) \cdot \sqrt{T_{\text{hsa}} \cdot T_{\text{d}}} \cong 0.063 \cdot \sqrt{T_{\text{hsa}} \cdot T_{\text{d}}} \qquad (21)$ 

The main results, given in table 1, show that the efficiency increase is very low, when  $n_{IC}$  go up from  $n_{IC}=1$  to  $n_{IC}=2$ . We did computation and for  $n_{IC}=3$  [4], showing that  $\eta_{th}$  is lower than for  $n_{IC}=2$ .

Table 1. Numerical values characterizing the analyzed cycle's performances

No	NoData		Notation	n <sub>IC</sub> =1	$n_{IC}=2$	Average
1	Number of compressor's stages	-	n <sub>K</sub>	2	3	-
2	Number of inter-cooling stages	-	n <sub>IC</sub>	1	2	-
3	Primary heat at source	kJ/kg	$q_{\rm NR}$	1,871.1		
4	Global compression ratio	-	$\epsilon_{K r gl}$	2.8383	2.9306	2.8840
5	Compression ratio per stage	-	$\epsilon_{\rm Kr \ stage}$	1.6847	1.4310	1.5527
6	Turbine's expansion ratio	-	ε <sub>Tb</sub>	2.4186		
7	Turbine's generated mechanical work	kJ/kg	W <sub>Tb</sub>	1,689.19		
8	Compressor's consumed mechanical work	kJ/kg	W <sub>K</sub>	808.29	805.56	806.93
9	Compressor mechanical work (relatively to turbine)	%	w <sub>K</sub> /w <sub>Tb</sub>	47.851	47.689	47.770
10	Net mechanical work (at revolving machines shift)	kJ/kg	$w_{net} = w_{Tb} - w_K$	880.89	883.62	882.26
11	Regenerate heat in RHE	kJ/kg	$q_{\rm RHE}$	2,376.5	2,512.1	2,444.3
12	Quota of regenerate heat (relatively to primary heat)	-	$q_{\rm RHE}/q_{\rm NR}$	127.01	134.26	130.64
13	Waste heat at cold source	kJ/kg	$q_{\rm EC}$	990.21	987.48	988.84
14	Thermal cycle efficiency	%	$\eta_{\mathrm{th}}$	47.079	47.225	47.152
15	Thermal cycle efficiency versus maximum theoretic one	%	$\eta_{th}/\eta_{max}$	67.466	67.675	67.571

It results that, for these input data, the thermodynamic optimal design require  $n_{IC}=2$ .



Fig. 4 T-s diagram of real processes in RHE, FC&IC cycle, with  $n_{IC}=1$  (fig. 1 design)





Using the results we build fig. 4 and fig. 5, representing the processes in real cycles, for both of technical interesting designs, in T-s coordinates.

#### **4** Sensitivity Analyses

The verdict that the efficiency augment is low when  $n_{IC}$  ascend from  $n_{IC}$ =1 to  $n_{IC}$ =2, and becomes lower

for  $n_{IC}=3$  than for  $n_{IC}=2$  is true for specified input data. The question is: this conclusion will remain true when the input data will be different.

In this chapter we are doing thermodynamic sensitivity analyses, modifying one by one the irreversibility factors ( $\Delta T_{RHE \ relatively}$ ,  $\eta_{is \ K} = \eta_{is \ Tb}$ , and  $\Delta p_{relatively}$ ) in order to determine their individual influences, on real cycles computed data, especially on  $\eta_{th}$ , by enlarging the range of input data:

★ For  $\Delta T_{RHE}$ , we choose a scale in geometric progression; the peak value is the double of the reference  $(\Delta T_{RHE max} \cong 0.125 \sqrt{T_{hsa} \cdot T_d})$ , and the inferior one,  $(\Delta T_{RHE min} \cong 0.032 \sqrt{T_{hsa} \cdot T_d})$ , equal to

the half of the reference, with a decrement  $\sqrt[10]{10}$ .

- \* For  $\eta_{is K} = \eta_{is Tb}$  we considered a linear variation from 0.88 to 0.94, with a step equal with 0.01;
- \* For  $\Delta p_{rel}$ , we choose a geometric progression scale with the decrement  $\sqrt[20]{10}$ , from the maximal  $\Delta p_{rel \max} \approx 4.5 \%$ , up to the minimal  $\Delta p_{rel \min} \approx 2.2 \%$ The minimal ratio is the half of the maximal; the reference is the geometric mean.
- The main computed data are characterizing:
- ▲ Turbo-machineries requirements ( $\epsilon_{K r gl}$ ,  $w_{Tb}$ ,  $w_{K}$ ).
- ▲ RHE design  $(q_{RHE}/q_{RHE reference}, S_{RHE}/S_{RHE ref.})$ .
- ▲ The cycle's thermal efficiency  $(\eta_{th}/\eta_{th reference})$ .

The obtained results show that, in the given combinations of irreversibility factors, the cycle's thermal efficiencies stays lower for  $n_{IC}=3$  than for  $n_{IC}=2$ . We are ongoing the study for  $n_{IC}=1$  and  $n_{IC}=2$ . With the obtained results for these situations we built fig 6. to 18. The data on Oy axis are given as relative quotas from the references (see the right column of table 1). The abscissa's scale is ranged as the irreversibility going down from left to right.







 $\begin{array}{l} Fig. 7 \ Global \ compression \ relative \ ratio, \\ \epsilon_{K\ r\ gl}/\epsilon_{K\ r\ gl\ reference}, \ vs. \ \eta_{is\ K} = \eta_{is\ Tb} \end{array}$ 

The global compression's necessary ratio,  $\mathcal{E}_{Krgl}$ , is higher in the  $n_{IC}=2$  design than in  $n_{IC}=1$  scheme (see Fig.6 to 8). In both designs it:

- \* increases with  $\Delta T_{RHE}$  diminish,
- \* decreases with  $\eta_{is K} = \eta_{is Tb}$  growth,
- \* diminishes with  $\Delta p_{relatively}$  decrease.

The bigger weight is give by  $\Delta p_{relatively}$  followed by  $\Delta T_{RHE}$ , and the smaller by  $\eta_{is K} = \eta_{is Tb}$ .





Fig.9 shows that *the turbine's generated mechanical work,*  $w_{Tb}$ , and *the compressors work,*  $w_K$ , are strongly influenced by  $\Delta T_{RHE}$ . Both increase with  $\Delta T_{RHE}$  diminish, but stay almost the same for  $n_{IC}=1$  and  $n_{IC}=2$  schemes. We mention that  $w_{Tb}$  isn't influenced by the others irreversibility factors.

In contrast,  $w_K$ , is varying with all the

#### irreversibility factors (see Fig. 9 to 11).



Fig.9  $W_{Tb relatively}$  &  $W_{K relatively}$  vs.  $\Delta T_{RHE relatively}$ 







Fig.11  $w_{K relatively}$  vs.  $\Delta p_{relatively}$ 



Fig.12  $q_{RHE}/q_{RHE}$  reference vs.  $\Delta T_{RHE}$  relatively

It increases, quickly than  $w_{Tb}$ , with  $\Delta T_{RHE}$  growth, and decreases when: **a**)  $\eta_{is K} = \eta_{is Tb}$ , goes up, respectively **b**)  $\Delta p_{relatively}$  goes down. For  $\Delta p_{relatively} > 3.6 \%$ ,  $w_K$  become higher in the  $n_{IC} = 2$  than in  $n_{IC} = 1$  scheme. It modifies the quota of compressor's work, related to the turbine one.

In both analyzed designs, for a wide range of input data, the regenerate heat is higher than primary heat (see fig.12 to 14).



Fig.13  $q_{RHE}/q_{RHE reference}$  vs.  $\eta_{is K} = \eta_{is Tb}$ 

The quota of regenerated heat:

- \* decreases with  $\Delta T_{RHE}$  diminish,
- \* goes up when  $\eta_{is K} = \eta_{is Tb}$  raise,
- \* increases when  $\Delta p_{relatively}$  goes down.

For the entire irreversibilities factor's variation, the relatively deviations are small, less than  $\pm 4 \%$  from the reference values.



Fig.14  $q_{RHE}/q_{RHE}$  reference vs.  $\Delta p_{relatively}$ 



Fig.15  $S_{RHE}/S_{RHE}$  reference vs.  $\Delta T_{RHE}$  relatively

The main difference for RHE design is given by  $\Delta T_{RHE}$ , witch influence *the active heat exchange surface* (fig.15). It shows that reducing  $\Delta T_{RHE relatively}$  at the half of the reference, requires rising the heat exchange surface at 190÷200 % from the reference. Doubling  $\Delta T_{RHE relatively}$  reduces the surface at 50÷52 % from the same reference value. It inflicts important changes in RHE investment's cost.

The key effects regard *the thermal cycle's efficiencies*. Because the primary heat is the same, the thermal efficiency is depending only on the net mechanical work. Generally,  $\eta_{th}$  is increasing when irreversibilities are going down. The influences are analogous, but the increasing rates could be different for  $n_{IC}$ =1 than for  $n_{IC}$ =2. Consequently, some of irreversibility's factors might change the design's classification.

The variation from 88 % to 94 % of  $\eta_{is K} = \eta_{is Tb}$ ,

doesn't change the order:  $\eta_{th}$  stays superior in the  $n_{IC}$ =2 design (see Fig.16).



Fig.16  $\eta_{th}/\eta_{th \ reference}$  vs.  $\eta_{is \ K} = \eta_{is \ Tb}$ 



Fig. 17  $\eta_{th}/\eta_{th reference}$  vs.  $\Delta T_{RHE relatively}$ 



Fig. 18  $\eta_{th}/\eta_{th reference}$  vs.  $\Delta p_{relatively}$ 

If  $\Delta T_{\text{RHE relatively}}$  and  $\Delta p_{\text{relatively}}$  are involving higher irreversibilities ( $\Delta T_{\text{RHE relatively}} > 0.1^* \sqrt{T_{\text{hsa}} \cdot T_d}$ , respectively  $\Delta p_{\text{relatively}} > 3.5 \%$ ),  $\eta_{\text{th}}$  become higher in the simplest design, with  $n_{\text{IC}} = 1$  (see Fig.17, and 18).

# 5 The Effects of Simultaneously Variation of Irreversibility Factors

In the sensitivity analysis the irreversibility factors where modified individually. In practice it is possible having, at the same time, deviations of 2 or all 3 factors. In this chapter we consider only the situation when all the factors are coincident adjust in the same way: simultaneously reducing all the irreversibilities.

Table 2 shows the combinations between the previous discrete factors, taken in to consideration for building a 7 steps "improvement scale", by simultaneously reducing all the irreversibilities.

Table 2. Numerical values characterizing the"improvement's steps"

Irreversibility axis	maximal $\rightarrow$ average $\rightarrow$ minimal								
Irreversibility steps	1	2	3	4	5	6	7		
$\Delta T_{RHE relatively}, \%$	12,5	10	8	6,3	5	4	3,2		
$\eta_{is K} = \eta_{is Tb}, \%$	88	89	90	91	92	93	94		
$\Delta p_{\text{relatively}}, \%$	4,5	4	3,5	3,2	2,8	2,5	2,2		

With these input data we computed the real cycles characteristic output data. Using the results we build fig 19 to 22.



Fig.19 Global compression ratio vs. improvement's steps

*The global compression's ratios,*  $\boldsymbol{e}_{Krgl}$ , higher in the n<sub>IC</sub>=2 design than in n<sub>IC</sub>=1 scheme (see Fig.19), reaches peak values:

\* among the improvement's steps #2&3, for  $n_{IC}=2$ ;

\* at the improvement's step #3, for  $n_{IC}=1$ .



Fig.20  $w_k/w_T$  vs. improvement's steps

Fig.20 shows that the quota of compressors consumed work, divided by the turbines generated work,  $w_K/w_{Tb}$ , is weakly influenced by  $n_{IC}$ . Starting with improvement's step #3, the ratio  $w_K/w_{Tb}$  for  $n_{IC}=2$  is lower than for  $n_{IC}=1$ . In both designs it increases with irreversibilities diminish.



Fig.21  $\eta_{th}$  vs. improvement's steps

The thermal cycle's efficiency,  $\eta_{th}$ , is strongly influenced by irreversibility factors. It increases

when irreversibilities are going down (see fig 21 and fig. 22). The maximal efficiency goes up to 55% (in absolute values), respectively, 116% from the amount established reference. The minimal one lessens at 36% (in absolute values), respectively, 76% from the reference.



Fig.22  $\eta_{th}/\eta_{th reference}$  vs. improvement's steps

The values of  $\eta_{th}$  for  $n_{IC}=1$  and  $n_{IC}=2$  are comparable, but after the improvement's step #3,  $\eta_{th}$  ( $n_{IC}=2$ ) becomes higher than  $\eta_{th}$  ( $n_{IC}=1$ ).

## 6 The Influence of HTGR's Output / Input Temperatures on the Real Cycles Performances

In this chapter we are relaxing the restrictions imposed by the NR, taking into consideration the option that the NR's outlet temperature "T<sub>a</sub>"could be dissimilar from the previous fixed value. We considered for  $T_a$  a linear variation from 1150 K to 1250 K with a step equal with 50 K. The NR's inlet temperature,  $T_z$ , respectively the NR's temperatures difference " $\Delta T_{NR}=T_a-T_z$ " should be correlated with the global compression's ratios,  $\mathcal{E}_{Krgl}$ , accordingly to the amount described mathematical relations.

For  $\varepsilon_{Krgl}$  we choose a scale, from  $\varepsilon_{Krgl\min}=2$  to  $\varepsilon_{Krgl\max}=4$ , in geometric progression. The maximal value is the double of the minimal one, and the growth ratio is  $\sqrt[12]{2}$ . For the previous reference irreversibilities (improvement's step #4) we where computing the values of  $T_z$ , respectively of  $\Delta T_{NR}$ , depending on  $\varepsilon_{Krgl}$  and  $T_a$  (see fig. 23). It shows that  $\Delta T_{NR}$ , the same in both design, is increasing with

 $\boldsymbol{\varepsilon}_{Krgl}$  and  $T_a$  growth.



Fig.23  $\Delta T_{NR}$  vs. global compression ratio

We stated the NR's relatively temperatures difference,  $\Delta T_{NR \ relatively}$ , given by:

$$\Delta T_{\text{NR relatively}} = (T_a - T_z) / \sqrt{T_a \cdot T_z}$$
(22)

, where  $\sqrt{T_a \cdot T_z}$  is the geometric average of input / output NR's temperatures. If we know  $T_a$  and  $\Delta T_{NR \ relatively}$ , it is possible to compute  $\Delta T_{NR}$  in absolute value as:

$$\Delta T_{\rm NR} = T_{\rm a} \cdot \{1 - \frac{4}{\left[\sqrt{(\Delta T_{\rm NR \ rel}^2 + 4)} + \Delta T_{\rm NR \ rel}\right]^2}\} \quad (22')$$



Fig.24  $\Delta T_{NR relatively}$  vs. global compression ratio

Fig. 24 shows that  $\Delta T_{\text{NR relatively}}$  is depending mainly on  $\boldsymbol{\varepsilon}_{Krgl}$ . Starting from all the 39 chosen and calculated values we established the correlation's equation:

$$\Delta T_{\rm NR \ rel} = 0.36988322 \cdot \ln(\epsilon_{\rm K \ r \ gl}) - 0.0161489$$
 (23)

The correlation coefficient between data is  $R^2=0.999662013826965$ . The average deviation is very small:  $\pm 0.00148914242653972$ .

The inverse of (23) equation is:

$$\varepsilon_{\text{K r gl}} = e^{[(\Delta T_{\text{NR relatively}} + 0.0161489)/0.36988322]}$$
(23')

In the next analyses we will utilize the  $\Delta T_{NR \text{ relatively}}$  adimensional parameter.



Fig.25  $w_K/w_T$  vs.  $\Delta T_{NR relatively}$ 



Fig.26  $w_{net}$  vs.  $\Delta T_{NR relatively}$ 

Fig. 25 shows the followings:

\* The quota of compressor's work, divided by the

turbine's one,  $w_K/w_{Tb}$ , reaches minimal values in the analyzed range of  $\Delta T_{NR rel}$ , along these lines:

- for  $n_{IC}=1$ , when  $\Delta T_{NR rel} \cong 0.275$ , matching to  $\epsilon_{K r g} \cong 2.2$ ;
- for  $n_{IC}=2$ , when  $\Delta T_{NR rel} \cong 0.325$ , related to  $\epsilon_{K r gl} \cong 2.5$ .
- \* For  $\Delta T_{\text{NR rel}} < 0.345$ , corresponding to  $\varepsilon_{\text{K r gl}} \cong 2.65$ ,  $w_{\text{K}}/w_{Tb}$  is lower for  $n_{\text{IC}}=1$  than for  $n_{\text{IC}}=2$ . For  $\Delta T_{\text{NR rel}} > 0.345 w_{\text{K}}/w_{Tb}$  become higher for  $n_{\text{IC}}=1$  than for  $n_{\text{IC}}=2$ .
- \* The NR's output temperature  $T_a$  increasing reduces the ratio  $w_K/w_{Tb}$ .

In both design the net work  $w_{Tb}-w_K$  is continuously increasing with  $\Delta T_{NR rel}$  and  $T_a$  rising (see fig. 26). For the same  $\Delta T_{NR rel} > 0.345$ , corresponding to  $\varepsilon_{K r gl} \approx 2.65$ ,  $w_{Tb}-w_K$  become higher for  $n_{IC}=2$  scheme.



 $\Delta T_{
m NR}$  relatively, -



The quota of regenerated heat (see fig. 27):

- \* has a variation on a wide domain, decreasing with  $\Delta T_{NR \text{ relatively}}$  increases,
- \* for the same  $T_a$  is lower in the  $n_{IC}=1$  design than in  $n_{ic}=2$  scheme,
- \* for the same  $n_{IC}$  is increasing with  $T_a$  grow.
- The effects of  $\Delta T_{NR rel}$  variation on *the thermal cycle's efficiencies* are put into evidence in fig. 28:
- \* For  $\Delta T_{\text{NR rel}} \cong 0.345$ , equivalent to  $\varepsilon_{\text{K r gl}} \cong 2.65$ ,  $\eta_{th}$ are the same for  $n_{\text{IC}} = 1$  and  $n_{\text{IC}} = 2$ . For  $\Delta T_{\text{NR rel}} > 0.345 \eta_{th}$  is higher in the  $n_{\text{IC}} = 2$  design.
- \*  $\eta_{th}$  reaches peak values in the analyzed range of  $\Delta T_{NR rel}$ , in this manner:
  - for  $n_{IC}=1$ , when  $\Delta T_{NR rel} \in [0.28 \div 0.285]$ , matching to  $\varepsilon_{K r gl} \in [2.23 \div 2.28]$ ;

- for  $n_{IC}=2$ , when  $\Delta T_{NR rel} \in [0.3875 \div 0.3925]$ , related to  $\varepsilon_{K r gl} \in [2.98 \div 3.02]$ .
- \* The maximal efficiencies for  $n_{IC}=2$  design are superior to  $n_{IC}=1$  scheme.
- \* Increasing the NR's outlet temperature  $T_a$  leads to  $\eta_{th}$  augmentation.
- \* The values of  $\varepsilon_{Krgl}$  witch allows maximizing  $\eta_{th}$  of FC&IC cycles are much lower than in simple cycle [10].







Fig.29  $\Delta T_{NR}$  for  $\eta_{th}$  maximizing, vs.  $T_a$ 

In order to determine the optimal NR's design we computed the absolute values of  $\Delta T_{NR}$  for maximizing  $\eta_{th}$ . With the obtained values we erected fig. 29. It shows the continuous growth of  $\Delta T_{NR}(\eta_{th max})$  with  $T_a$  increase. For  $n_{IC}=2$  design  $\Delta T_{NR}(\eta_{th max})$  is higher with approximately 90 K than for  $n_{IC}=1$  scheme.

### 7 Conclusions

The first paper's section (up to chapter # 4) refers to comparatively analyzing the influence of irreversibilities causes ( $\Delta T_{RHE \ relatively}$ ,  $\eta_{is \ K}=\eta_{is \ Tb}$ , and  $\Delta p_{relatively}$ ) on real Brayton cycles (with RHE, FC&IC, for  $n_{IC}=1$  and  $n_{IC}=2$ ) main indicators. The sensitivity analysis shows that:

- η<sub>th</sub> is increasing when any of irreversibilities is decreasing. For low irreversibilities it is possible to attain η<sub>th</sub>>50 %.
- The irreversibilities reasons have comparatively effects on  $\eta_{th}$  (from minus 7÷10 % up to plus 4÷6 % relative to  $\eta_{th \ reference}$ ).
- $\Delta T_{RHE relatively}$  influence too the RHE surface, inflicting changes in investment's cost.
- The efficiencies  $\eta_{is K} = \eta_{is Tb}$  have effects on  $\eta_{th}$ , without shifting the performances order;  $\eta_{th}$  is higher in the more complex design ( $n_{IC}=2$ ).
- When the irreversibilities are bigger than the chosen references (in this case for  $\Delta T_{\text{RHE relatively}} > 0.1^* \sqrt{T_{\text{hsa}} \cdot T_d}$ , or  $\Delta p_{\text{relatively}} > 3.5 \%$ ), the simplest design, with  $n_{\text{IC}}=1$ , offers in the same time: *a*) a lower investment's cost, and *b*) a higher thermal efficiencies than  $n_{\text{IC}}=1$  design.

In the  $5^{\text{th}}$  chapter we considered a simultaneously variation of irreversibility factors, by concomitantly reducing in 7 steps all the irreversibilities. The results show the followings:

- \* The global compression's ratios,  $\varepsilon_{Krgl}$ , is higher in the  $n_{IC}=2$  design than in  $n_{IC}=1$  scheme and reaches peak values among the improvement's steps #2&3, for  $n_{IC}=2$ , respectively at the improvement's step #3, for  $n_{IC}=1$ .
- \* The ratio  $w_{K}/w_{Tb}$ , is weakly influenced by  $n_{IC}$ . In both designs it increases with irreversibilities reducing. Starting with improvement's step #3 it becomes lower for  $n_{IC}=2$  than for  $n_{IC}=1$ .
- \* The thermal efficiencies are strongly influenced by irreversibility factors. They increase when irreversibilities are going down up to 55% (in absolute values), respectively, 116% from the amount established reference. The minimal values lessen at 36% (in absolute values), respectively, 76% from the reference. The values of  $\eta_{th}$  for  $n_{IC}$ =1 and  $n_{IC}$ =2 are comparable, but after the improvement's step #3,  $\eta_{th}$  ( $n_{IC}$ =2) becomes higher than  $\eta_{th}$  ( $n_{IC}$ =1).

In chapter # 6 we where relaxing the restrictions imposed by the NR, taking into consideration different output / input temperatures  $(T_a/T_z)$  from

the previous fixed ones. It shows their influence on the real cycle's performances:

- \* For the same  $n_{IC}$ , the NR's output temperature  $T_a$  increasing reduces the ratio  $w_K/w_{Tb}$ .
- \*  $w_{K}/w_{Tb}$ , reaches minimal values in the analyzed range of  $\Delta T_{NR \text{ relatively}} = (T_a - T_z) / \sqrt{T_a \cdot T_z}$
- \* The quota of regenerated heat has a large variation, decreasing with  $\Delta T_{NR relatively}$  increases. For the same  $T_a$  it is lower in the  $n_{IC}$ =1 design than in  $n_{ic}$ =2 scheme, and for the same  $n_{IC}$  is increasing with  $T_a$  grow.
- \* The effects of  $\Delta T_{\text{NR rel}}$  variation on the thermal cycle's efficiencies are the followings:
  - For ΔT<sub>NR rel</sub>≅0.345 (ε<sub>K r gl</sub>≅2.65), η<sub>th</sub> is the same in both designs. If ΔT<sub>NR rel</sub>>0.345, η<sub>th</sub> is higher in the n<sub>IC</sub>=2 scheme.
  - $\eta_{th}$  could be optimized in the analyzed range of  $\Delta T_{NR rel}$ . For  $n_{IC}=1$  it happens when  $\Delta T_{NR rel} \approx 0.283$  ( $\varepsilon_{K r gl} \approx 2.25$ ), and for  $n_{IC}=2$ , when  $\Delta T_{NR rel} \approx 0.39 \varepsilon_{K r gl} \approx 3$ .
  - The maximal efficiencies for n<sub>IC</sub>=2 design are superior to n<sub>IC</sub>=1 scheme.
  - Increasing the NR's outlet temperature  $T_a$  leads to  $\eta_{th}$  augmentation.
- \* The absolute values of  $\Delta T_{NR}=T_a-T_z$  for maximizing  $\eta_{th}$  are continuously growing with  $T_a$ increase. For  $n_{IC}=2$ ,  $\Delta T_{NR}(\eta_{th max}) \in (368 \div 404)$  K, being higher with approximately 90 K than  $\Delta T_{NR}(\eta_{th max}) \in (280 \div 309)$  K, for  $n_{IC}=1$  scheme.

The general directions for optimizing the performances of HTGR's Helium Brayton cycles with FC&IC are: A) reducing the irreversibilities and choosing the correct design, correlated with them; B) increasing the NR's outlet temperature and choosing the optimal  $\Delta T_{NR}=T_a$ - $T_z$ , according to  $T_a$  and the scheme's design. The  $\Delta T_{NR}$  choice involves the value of compression ratio.

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