Optimal size of kanban board in a single stage multi product system

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Abstract: The aim of this paper is to define a methodology for determining the optimal size of the supermarket (between two workstations) through the optimization of the number of kanban in a kanban board. It also identifies some production parameters that greatly influence the optimal size of a kanban board. The approach chosen is the building of a simulation model of a single stage multi-product system with Arena, while OptQuest has been used for the next optimization phase.

Key-Words: Supermarket pull system, kanban board, DES, simulation and optimization, data analysis.

1 Introduction
During the events of recent years it is easy to see a growing need in the industrial world: the traditional business model is no longer suitable to the context in which companies are increasingly subjected to different competitive pressure. There is the need to find new business models able to be creative and innovative and able to perceive and manage change. This need is the dominant reason throughout the literature and the media in recent years. This new understanding of the industry is the starting point of this work, which aims to apply the cornerstones of Lean Thinking for the Improvement of a production system which has as its first priority to meet as best as possible and as fast as possible customer requirements.

The system studied is a Single-Stage Multi-Product Kanban System: it consists of a single production unit, which produces 3 different products and there is only one supermarket to store them and a kanban board to collect and manage the production orders. This type of system was first studied through a specific and literature search in depth, and has been implemented in theory by a simulation model. The system was simulated using the software Arena 8.0 and hence has been optimized with OptQuest, using total cost minimization as the objective function.

2 Problem Formulation
The philosophy of hunting to "waste", typical of Lean Thinking, is the key objective of creating a continuous process flow. The continuous flow is an ideal situation: every single operation is performed only if necessary and if requested by the next station in order to avoid the overproduction that is, according to Ohno, the worst waste. In order to enable this, the production flow is no longer pushed by upstream station, but the customer pulls it and it proceeds backward from the downstream area, up to the first upstream station. Therefore we talk about pull production, whose aim is to create a continuous flow, where each lot must pass from one process to the next one without waiting time. It is not always possible to achieve a continuous flow of production and therefore, according to lean principles, it prefers to decouple some processes with a supermarket. The supermarket is a storage area between two workstations holding products contained in strictly necessary quantity. The downstream workstation collects only the requested amount by the customer and then it sends a replenishment request to the upstream station in the form of a kanban. The kanban is a technique of materials handling that allows the perfect synchronization between what is required from the downstream station (i.e. an assembly line) and the production started upstream from the production system. The Japanese word kanban means, literally "visual record", "visible documentation" and shows a card that accompanies the single container of materials or parts. The kanban is not necessarily a physical card, as it can be either electronic or may be represented by the container itself. The supermarket managed by kanban is called Supermarket Pull Kanban, and it is the aim of this study. The kanban are collected in a box called kanban board. This is filled from top to bottom, it consists of many columns as there are products and for each product is divided into 3 different zones:

- The green zone: it represents the highest production cost. It has a low priority for processing;
- The white zone (or yellow): it represents a normal production. It has the same production priority level of green area, but it has a warning signal, since it warns that we are going to fall into the red zone;

- The red zone: it represents the lowest production cost. It has a high priority for processing.
The red zone: it represents an emergency; it means urgent production. It means that there is a stock out for that product and then immediate container replenishment is needed as soon as the machine will be available.

This paper focuses on the optimal size problem of the kanban board to vary certain parameters such as cost, production time, the number of products and customer demand.

3 Literature review

There are numerous studies on the systems controlled by kanban. These studies were differentiated by type and topic. More specifically, the type indicates which kind of study has been conducted on kanban systems, such as:

- Algorithms (including genetic) - the kanban system is studied using an algorithm approach [2].
- Models of queue networks and Petri networks - the kanban system is represented and solved using the queue network models.
- Markov chains - the kanban system is studied by using Markov chains.
- Mathematical models – it provides a mathematical method for solving kanban systems.
- Simulation - the kanban system is studied and solved through a large family of simulation techniques [8, 12].
- Literature review - the authors whose works have argued for the kanban system are mentioned [10].
- Case study – the article deals with a real case where the implementation of a kanban system has been done.
- Conceptual – the article is based on a general and conceptual discussion of kanban systems.
- Methodology - a methodology is proposed in order to manage different systems using kanban.
- O. F. cost minimization – the aim of these articles is to minimize costs. An objective function focuses on costs minimization will be the key of this work.

Instead, under the topic entry we are enclosing the following concepts:

- Techniques – it shows the type of technique dealing in the article (that is kanban, or other techniques, such as conwip, hybrid, etc....) and if a benchmarking among several techniques was done.
- Implementation – it considers papers proposing an implementation of kanban in systems of different nature [8].
- Various topics with kanban - covers those studies focused on various aspects of kanban, as its characteristics, methods of operation and more [3].
- Cards – it is essentially the calculation of card number, calculated as a general formula and as a numerical parameter obtained from the kanban system implementation.
- Safety stock - this entry refers to articles considering the safety stock in kanban systems.
- Buffer size – it concerns studies where the buffer size in a kanban system is considered [11].
- Inventory - this parameter indicates the stock calculated following the implementation of a kanban system [1].
- Priority list – it indicates the priority rules chosen to appropriately manage a kanban system (such as sequencing, scheduling, backlog).
- Performance indicators - this entry indicates the various indices of performance that were used in the articles to assess the results obtained or obtainable in a kanban system.
- Supermarket – it indicates those articles focusing on a supermarket within a kanban system [9].

From this review of the literature it has been highlighted that for the study of problems concerning the kanban logic most authors use simulation techniques; while the performance parameters built and used by these authors are throughput, WIP, backorders, setup, costs, cycle time, lead time, and service level.

C. SendThe Kumar and R. Panneerselvam (2007) [10] have focused their attention on the review of the literature on systems managed by kanban. They first proposed a kanban classification system, given as a discriminating parameter the mechanism of blocking, namely the requirement that the
workstation cannot process other components because the buffer is a full collection of products and then stops. Hence they have analyzed the main performance measures used in the literature for the evaluation of kanban systems, including:

- Average number of WIP;
- Demand;
- Average waiting time of kanban in queue;
- Average production time;
- Average stocks number;
- Average setup time;
- Number of orders not fulfilled.

They have finally analyzed the various modelling approaches proposed in the literature, namely:

- Mathematical models;
- Queuing models;
- Markovian models;
- Simulation;
- Cost minimization model;
- Variability.

Richard P. Marek, Debra A. Elkins and Donald R. Smith (2001) [8] have introduced a simulation model of a series system controlled by kanban and CONWIP, respectively, using the software Arena. The system considered consists of 4 stations and produces 2 types of products. The costs of changeover are taken early and of low magnitude and then the setup cost is set equal to zero, assuming similar products. Assigned all the model parameters, the authors first established a model using the language of SIMAN Arena.

Consequently they have conducted experiments on the model and for each station have determined: the average time for crossing into the system, the average number of WIP, utilization of the stations and number of completed parts.

Georg N. Krieg [5, 6, 7] proposes a classification of kanban systems in:

- Single Stage Single Product Systems (fig.2);
- Single Stage Multi Product Systems (fig.3);
- Multi Stage Multi Product Systems (fig.4).

A single-stage single-product system [13] is characterized by a single production phase and only one product. In addition to the production plant, the system contains a collection box (the scheduling board, otherwise known as kanban board), an output storage for finished products, the containers for storing and handling the finished products, and a series of kanban for each product in the system (Fig. 2).

The single-stage multi-product kanban system is always characterized by a single stage production but by several different product codes. In kanban systems the customers whose request cannot be satisfied just in time (through the inventory stocked at warehouse) or they withdraw their request and apply to another supplier offering the same product or, if they have no alternative, they wait until their request is not satisfied.

This is the standard situation for the production stages taking raw materials or parts from one supplier (the supplier may be a previous production phase, or an external supplier).

In these systems, the maximum number of backorders depends on customer number generating the request. The model of a single stage multi-product kanban system with limited number of backorders and lost demand is illustrated in fig. 3.

The multi-stage multi-product kanban system is the one more generally characterized by two or more production phases and by two or more products.

In this case the products processed by a phase are input materials of the following phases (fig. 4).
Mohammad D. Al Tahat and Adnan M. Mukattash (2006) [14] have studied a synchronization mechanism for a kanban system, single - single stage - product, considering as main parameters of modelling:
- the WIP level in the system;
- the capacity at the station;
- the processing speed;
- the utilization factor of the system;
- the number server in the system;
- the arrival rate of raw materials.

The workstation line was modelled with a queuing system of type M / M / S: GD / ∞ / ∞ and here [it] was calculated timing parameters of the station and operating costs of the system (as the sum of the costs of raw materials, WIP in the system, the elements of production and transport).

Finally, the authors have diagrammed the influence of the number of servers on the average number of WIP in the system, the influence of utilization factor on the average number of WIP, and the influence of system parameters of total costs.

4 Single – stage multi - product model

The system considered consists of a production shop and an assembly shop acting as a demand generator, so this system is a single – multi-stage – product (fig.6). This system produces three types of components C1, C2 and C3, which are produced in the upstream manufacturing stage and are sent to the downstream assembly stage, that will mount the finished products P1, P2 e P3 (from C1, C2 and C3 respectively).

The coefficient of employment of the three products is a unit, which means that the demand for P1, P2 and P3 will be automatically translated into the demand of C1, C2 and C3 components. The two shops are decoupled from a supermarket managed by a kanban board where production orders coming from the assembly shop are collected.

This model was built by several sub models in Arena 8.0 [4], in particular, the block diagram depicted in Fig. 6 is structured in:
1. final customer demand sub model;
2. the kanban board logic sub model;
3. the production shop sub model;
4. the supermarket statement sub model.

- Production shop consists of a single machine, and then all products share the production plant.
- The annual demand of 540,000 pieces P1, 360,000 pieces P2 and 720,000 pieces P3 is perfectly levelled on daily basis with deterministic distribution.
- The production time is the same for all products.
- The values of demand required are already net of any waste.
- Demand arrivals are mutually independent.
- The failure rate is assumed to be zero.
- The setup time is negligible.
- The transportation time is negligible.
- The materials handling time is negligible.
- There is infinite availability of raw materials in the production shop.
- The demand is generated at the beginning of each day and the customer requires that his request be immediately satisfied. If not, the customer is willing to tolerate a delay that would not be extended beyond the day in question. If the day is spent, the request is to be considered withdrawn. Therefore in the system the backorders are not allowed and just only a temporary backlog situations is allowed.

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4.1 Part I: final customer demand
The demand of products P1, P2 e P3 been modelled through three create modules, having constant arrival distribution and daily arrival mode (all request arrives in the first hours of the day). The entities are retained in three modules (one for each product), and are released only when there is at least one container of that product present in the appropriate shelf of the supermarket.

A counter for each product marks the average number of retained entities in every hold, so providing a measure of the units that will be late delivered to the customer (backlog).

As soon as the entities are released, it was thought to split the entity into two distinct parts: a physical part, which represents the component which is delivered to assembly, and a signal representing the request of the recovery container consumed by the downstream shop (assembly).

4.2 Part II: the kanban board
The kanban board columns are formed by two areas: the green zone – the white one and the red zone.

Each one of these zones has been modelled with a hold module. Particularly, within each hold the following priority rule of issuing cards has been set: the cards in the 3 green areas may be issued only if the 3 red zones are empty. So the red kanban have processing priority and they will be issued as soon as the machine will be free.

Since the machine can process only one container at time, the first card to be issued will be the one that belongs to the red queue once it has reached its maximum size. If no queue is saturated, the precedence is given to the red zone, which has the largest number of elements in queue. This until all red areas has at least one element on queue. As soon as the red zone empties, we can pass to the green – white ones.

The card choosing mode to be processed is similar to the one established for the red zone, with the only difference that, once a card from the zone with the highest number of elements in queue has been taken, we will keep on processing cards of that zone until the zone will be empty or until at least one card is present in the red zone.

In this way the machine will work, when possible, the same product, reducing the setup number to process different products.

4.3 Part III: the production shop
Each card issued by a hold is sent to the production shop. This shop consists of a single block process formed by size, delay, and release modules.

4.4 Part IV: the supermarket
Once processed, the entity is sent to the supermarket and, particularly, through the modules, it decides on the product container, which is then sent to the appropriate shelf. The shelves are modelled with hold blocks known as “infinite hold”, holding the entities until one selecting condition through a remove module is set (using in part I to collect containers from the shelf).

5 Optimization and parametric analysis
The next step is to estimate the maximum size (control variable), which must have every zone of the Kanban board in order to optimize a specific chosen objective function [9, 15]. Afterwards, we will proceed to the parametric analysis of system main factors and to the study of their interactions. The optimizations are carried out with Optquest, an ARENA tool, where the objective function consists of minimizing the Total Cost ($C_T$), given by the sum of the backlog cost (CB) and the holding cost (CM).

So the problem is:

\[ \text{Min! } C_T = C_B + C \]
\[ Z_{r,i} \geq 0 \]
\[ Z_{r-b,i} \geq 0 \]

Where:

- $Z_{r,i}$ is the maximum size of red zone of the product “i”;
- $Z_{r-b,i}$ is the maximum size of green plus white zone of the product “i”;
- $Z_{r,i}$ and $Z_{r-b,i}$ are the control variables of the system.

Particularly:

- $C_B$ is the cost that the company holds up in order to holding at stock the codes of the product stored on the supermarket shelves, and it is equal to

\[ C_B = \sum_{i=1}^{3} (G_{m,i} \cdot C_{u,i}) \] (1)

where: $G_{m,i}$ = average stock of the product “I” over the considered period

$C_{u,i}$ = unit holding cost of maintaining to stock

- CB is the cost that the company holds up when it is not able to immediately satisfy customer requirements, so that it will have accumulated work to be done, and it is equal to

\[ C_B = \sum_{i=1}^{3} (N_{mR,i} \cdot C_{u,i}) \] (2)

where: $N_{mR,i}$ = average number of units in delay for the “i” product

$C_{u,i}$ = unit cost of backlog for the “i” product ([euro/unit]).

Another statistic for the optimization purpose is the Service Level, defined for each product as follows, has been considered:

\[ L_{s,i} = 1 - \left( \frac{N_{mR,i}}{N_{mE,i}} \right) \] (3)
where: \( N_{mr,i} \) = average number of units in delay for the “i” product
\( N_{me,i} \) = total number of processed orders for the “i” product

The technique of planning the used tests is of type OFAT (one factor at a time). We start the optimization of a baseline scenario (basic setting) and make one change at a time the various factors considered.

The basic setting is:
\[
\begin{align*}
Z_{r,1} &= 1 \\
Z_{r,2} &= 1 \\
Z_{r,3} &= 1 \\
Z_{v-h,1} &= 3 \\
Z_{v-h,2} &= 2 \\
Z_{v-h,3} &= 3.
\end{align*}
\]

In order to test the validity of the solution, the initial conditions were changed several times and the result has always been the same.

Thus the optimizations were run in different scenarios, by varying some parameters such as CB, CM, the demand, the production time, the number of products, and evaluating the influence of each parameter on the size zones of the Kanban board (control variable), on \( C_T \), and on the Service Level.

### 5.1 Scenario I: Backlog cost variability (CB)

The first analysed scenario concerns the backlog cost CB. Since we started from a situation where the backlog cost and the holding cost are both unit costs, (it is thought from us) we think that it is interesting to vary, iteratively, the value of only one factor, keeping the other cost variable fixed to unit value. In particular varying this parameter we obtained the following curves.

Fig. 7 - Influence of backlog cost value on the maximum kanban board size, service level and total cost

These graphs highlight an increase of size zones by level with increase backlog cost value. That is because the customer satisfaction is preferred and the delivery timeliness rather than warehouse stock reduction. Subsequently a service level increase is highlighted. From data analysis it also appears that the optimal zones find through OptQuest are always consistent with starting model data. As matter of fact the zone size of P3 product is the highest value compared to other products, since P3 is the product most required.

The consistency with expectations has also been strengthened from the analysis of total cost, already having an increasing trend to the backlog cost value increase.

### 5.2 Scenario II: holding cost variability

In this case the tendency is opposed to the previous case, as shown in fig. 8. In order to stock the least number of components, the firm must necessarily reduce the zones, following the service level reduction (since the number of pieces delivered on delay is greater); while the total cost is higher since the holding cost value increases.
5.3 Scenario III: demand variability

This considered scenario is related to the demand. At demand increasing the containers’ number to produce increase as well. Then it implies a greater zone sizes in the kanban board in order to avoid a meaningful number of units in delay. Besides this increase involves an overall one of service level and total cost (Fig. 9).

5.4 Scenario IV: production time variability
In this scenario we show the relationship between kanban size board and production time. Increasing production time, an increase of kanban board has been found. Since to process a container longer implies reintroducing codes slower, then a bigger size in the kanban board able to accept a bigger number of requests is needed. All results are shown in fig. 10.

![Fig. 10 - Influence of production time on the maximum kanban board size, service level and total cost.](image)

5.5 Scenario V: number of products variability
The increase in the number of products has underlined an increase of kanban board zone since the management of a product or more, having only one available machine, implies production slow-downs reducing the number of delivered-on-time units to the customers. Therefore, the increasing product number increases the total cost. Instead meaningful variations in the service level are not highlighted.
6 Conclusion

The experimental results obtained showed that the model constructed can be used as a valuable tool for strategic decision support for firms that want to design the supermarket managed with pull kanban logic: optimal size of the kanban board.

A future perspective would be to perform a DOE analysis on experimental data in order to understand the critical factors and the impact of their interactions on the scale of the regions of table (buffer size), total costs and service level.

It is also possible to stress the current model, whereby stochastic and random distribution data, then the assumption will be removed on setup time, considered to be in force on the relevant item of total cost incurred by the company.

The project is the study of multi-product with more than one phase (i.e. the system with various production departments are working like products using multiple machines in parallel) and therefore, will address the problem of multiple tables kanban sizing, more supermarket and the synchronization of the various production cells operating in logic and operated by a supermarket pull pull kanban.

The idea is to make the model more adaptable to many corporations, but more flexible in responding to the random fluctuations that characterize the production so as to constitute a valid support for the strategic management of any kanban pull system.

References:


