Theoretical and Practical Aspects of Heating Equation

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Abstract: - We are interested in a null controllability problem for a class of strongly degenerate heat equations. Heat equation parameters are represented graphically (temperature, heat flux) for a particular situation. Then, first for all T>0, we prove a regional null controllability result at time T at least in the region where the equation is not degenerate. The proof is based on an adequate observability inequality for the homogeneous adjoint problem. This inequality is obtained by application of Carleman estimates combined with the introduction of cut-off functions. Then we improve this result: for all T’>T, we obtain a result of persistent regional null controllability during the time interval [T,T’]. We give similar results for the (non degenerate) heat equation in unbounded domain. Analysis by numerical simulation of the heating room space has highlighted that the use of composite materials instead of the usual materials of construction is more advantageous in terms of achieving the microclimate conditions, making possible, within certain limits of temperature exterior, a passive air conditioning, which involves reducing energy consumption.

Key-words: - Representation equations, Control, Null controllability, Air conditioning.

1 Introduction

In this article, we study first the null controllability of a class of equations of degenerate heat (in limited areas) (α,β)⊂(0,1) different from zero and δ>0 (results ). 1<δ+α
If we consider as positive, a(x)>0 for all x∈[β,1].
There is the problem of regional null controllability:
Problem 1. For all T>0 and all u0∈L2(0.1), found the solutions:
\[ \begin{align*}
    u(t,x) &= f(t,x)X_{α,β}(x), \quad (t,x)\in(0,T)\times(0,1) \\
    u(t,0) &= u(T,L) = 0, \quad t\in(0,T) \\
    u(0,x) &= u_0(x), \quad x\in(0,l)
\end{align*} \]

verifies
\[ u(T,x) = 0 \quad \text{for} \quad x\in(α+δ,1). \]

Notes:

a) It can be shown that the problem is well posed (see [1], [7]) within the meaning of the theory of semigroups working in areas with adequate weight.

b) In the not degenerated case (ie a> 0 on [0,1]), the null controllability (overall) is now well known: for all T>0, it exists f∈L2((0,T)×(0,1)) so that the solution in (1) verifies u(T,·)=0 in all (0,1).

This result is generally obtained via Carleman estimate (see for example [2], [3], [4]).

c) We consider here the case of an equation of degenerate heat, possibly strongly degenerate so that a(x) can be null all through the range (0,α’) for 0≤α<β.

Under this hypothesis, with an f control located in (α, β), we can not hope to bring the system to zero in any (α, 1). The area of influence of control is necessarily located in the region (α,1). That is why we focus on the local null controllability [12].

d) Many results are known for non-degenerate parabolic equations. But to our knowledge, no result was known for degenerate equations.

Recently, another result of null regional controllability has been obtained for an linearized Crocco-type equation [5], [9], [13].

This is a degenerate parabolic equation (where there are are phenomena of diffusion and transport) so the type of degeneration is quite different from that studied here.
e) The null controllability (global) at time $T$ is a strong property. Indeed, because of the decrease in energy, it implies that, from time $T$, the system remains indefinitely at rest (by ceasing to apply a control from the time $T$): for all $t \geq T$, $u(t, \cdot) = 0$ in $(0,1)$.

On the contrary, the null regional controllability is a property much weaker since, if one ceases to apply a control from the time $T$, it does not imply that the system remains at rest in the region $(\alpha + \delta, 1)$ for $t \geq T$.

Problem 2. For all $T^*>T>0$ and all $u_0 \in L^2(0,1)$, find $f \in L^2((0, T^*) \times (0,1))$ so that the solution of

$$u_t(t, x) - (a(x)u_x(t, x))_x = f(t, x), \quad x \in (0, 1), \quad t \leq T$$

$$u(t, 0) = u_0(t), \quad u(t, 1) = f(t, 1), \quad t \in (0, T^*), \quad \forall x \in (0, 1), \quad u(t, x) = 0, \quad x \in (0, 1)$$

verifies

$$u(t, x) = 0 \quad \text{for} \quad (t, x) \in (T, T^*) \times (\alpha + \delta, 1). \quad (4)$$

2 Equations of degenerate heat

Problem 1. It shows first the observability of the inequality for the secondary problem associated:

$$v_x(t, x) - (a(x)v_t(t, x))_x = 0, \quad \forall x \in (0, 1), \quad \forall t \in (0, T)$$

$$v(t, 0) = v(t, 1) = 0, \quad t \in (0, T)$$

Theorem 1 ([1]). For all $\delta>0$ (so that $\alpha+\delta<1$), there exists $C>0$ so that any solution $v$ of (5) verifies:

$$\int_0^T \int_0^1 v(x, t)^2 dx dt + C \int_0^1 v(0, t)^2 dx \leq \frac{\beta}{\alpha} \int_0^1 v(1, t)^2 dx \quad (6)$$

we deduce the

Theorem 2 ([1]). Under the previous assumptions, it exists $f \in L^2((0, T^*) \times (0,1))$ so that the solution to (1) verifies (2).

Note. If $\alpha=0$, there is actually (global) null controllability throughout $(0,1)$ (and not only for $(\delta, 1)$).

Principle of evidence. For Theorem 1, we used truncation functions. In particular, in the region where it doesn’t become null, it boils down to a non-degenerate equation to which we apply the Carleman estimates. The planned Theorem 2 is based on the introduction of the penalized problem.

$$\inf_{f \in L^2((0, T^*) \times (0,1))} \left\{ \int_0^T \int_0^1 f(x, t)^2 dx dt + \frac{1}{\alpha+\delta} \int_0^1 \mu'(x, t)^2 dx \right\},$$

where $\mu'$ is the solution of (1) associated to $f \in L^2((0, T^*) \times (0,1))$.

Problem 2. For all $t \in (0, T^*)$ we consider the family of adjoint problems:

$$v_x(s, x) - (a(s)v_t(s, x))_x = 0, \quad (s, x) \in (0, t) \times (0,1)$$

$$v(t, 0) = v(s, 1) = 0, \quad (s, t) \in (0, T^*)$$

Fig. 1: Variation of heat equation parameters [11]:

a) temperature variation across the $x$ axis;

b) the variation of the heat flow in time;

c) the heating variation in time.
Theorem 3 ([1]). For all $\delta > 0$ (so that $\alpha + \delta < 1$), it exists $C > 0$ so that

$$\int_0^T \left( \int_0^T v'(0,x) dt \right)^2 dx \leq C \int_0^T \left( \int_0^T (s,x) dt \right)^2 dxds + C \int_0^T v(s,x)^2 dxds$$

we deduce the

Theorem 4 ([1]). Under the previous assumptions, there is $C > 0$ so that the solution to (3) verifies (4).

Principle of evidence. For the 3rd Theorem, we apply the 1st Theorem to the function $\phi$:

$$w(s,x) := \int_{\max(s,R)}^T v'(s,x) dt$$

The planned Theorem 4 based on the introduction of the penalized problem

$$\inf_{f \in L^2((0,T') \times (0,1))} \left( \frac{1}{2} \int_0^{T'} f(t,x)^2 dxdt + \frac{1}{2k} \int_0^{T'} u'(t,x)^2 dxdt \right)$$

A different result. The concept of persistent regional null controllability also gives interesting results even in the equation of not degenerate heat.

For example, if we are given a null starting value on a part of $(0,1)$, we can maintain (cheaper) the solution to be zero on that part (instead of bringing it to zero on the whole domain).

Results: $0 \leq \alpha < \gamma < \alpha + \delta < \beta < 1$.

Let’s suppose that $a \in C^1([0,1])$ so that $a(x) > 0$ for all $x \in [0,1]$.

For all $T > 0$ and all $u_0 \in L^2(0,1)$ so that $u_0(x) = 0$ for $x \in (\gamma,1)$, $f \in L^2((0,T') \times (0,1))$ exists, so that the solution of (1) verifies $u(t,x) = 0$ for $(t,x) \in (0,T) \times (\alpha + \delta,1)$.

In [1], we give another result of persistent regional null controllability for the heat equation subject to a localized source term.

3 Heat equation in an unbounded domain

We consider now the equation of heat (non-degenerate) on the positive half-axis for $T > 0$ and $u_0 \in L^2(0,1)$

$$u(t,x) - u_{xx}(t,x) = f(t,x) \chi_{(\alpha,\beta)}(x), \quad (t,x) \in (0,T) \times (0,\infty)$$

$$u(t,0) = 0, \quad t \in (0,T)$$

$$u(0,x) = u_0(x), \quad x \in (0,1)$$

Micu, Zuazua [10] and then Popescu [14], [15] have shown that there is no data to support initial regular compact that can be brought to zero in finite time. This negative result is that one seeks to control the heat equation in unbounded domain by a control $f \chi_{(\alpha,\beta)} \in L^2((0,T) \times (\alpha,\beta))$ located in a bounded domain $(\alpha, \beta)$.

Cabanillas, De Menezes and Zuazua [1] have subsequently obtained a positive result of null controllability, with the condition to use an $f$ control located in an unbounded domain like $(\alpha, +\infty)$.

With the techniques previously used, we have the following intermediate result (see [1]): with an $f$ control located in the bound domain $(\alpha, \beta)$, there is a null regional controllability at time $T$ in the region $(0, \beta - \delta)$ (for all $\delta > 0$).

In particular, if $\beta = +\infty$, we find the result of [7].

We can also improve this result to obtain the persistent regional null controllability in the region $(0, \beta - \delta)$. During the whole time range $(T, T')$.

Notes:

1. We have proven in [8] another intermediate result for the null (global) controllability by a control $f$ located in an unbounded domain, but of finite extent
2. The techniques of evidence used are not specific to the dimension 1. The results presented here can be a statement in dimension N.
4 Experimental result

In the modelling space of room, difficult issues arise in determining intakes heat introducing outside non stationary regime due to heat transmission. In literature this problem is resolved differently; there are a number of approximate models [14], [15], [16]. Consider a room with space monolayer structure and low surface without glass surfaces.

$Q_{ed}$ noting the amount of heat that passes through the wall into the hall of time, and assuming that heat transfer will be conduction from the inside out, then the thermal resistance equivalent to the construction transfer will be

\[
Q_{cd} = \frac{\theta_e - \theta_i}{R_f} + \frac{\theta_e - \theta_i}{R_z} = \frac{(\theta_e - \theta_i)R_f + R_z}{R_fR_z},
\]

or

\[
\theta_i - \theta_e \left[W\right] = \int_{t_0}^{t} Q_{ed} dt,
\]

where:
- $\theta_e, \theta_i$ are air temperatures outside and inside;
- $R_f$ and $R_z$ represent thermal resistances of the doors and walls, data relations

\[
R_f = \frac{z_f}{\lambda_fS_f}, \quad R_z = \frac{z_z}{\lambda_zS_z}, \quad [^\circ C/W]
\]

where:
- $z_f, z_z$ are thickness doors and walls of built space, [m];
- $\lambda_f, \lambda_z$ are the thermal conductivity of material [W/m·C];
- $S_f, S_z$ areas are sections of the interior doors and walls, the normal direction of heat flow [m$^2$].

Expressing $C_i$, heat capacity of air, as the product between the mass $m$ of the existing room air and specific heat of indoor air $c_{si}$, then mass balance equation, assuming the existence of consideration heat from the rooms attached $Q_i$, the release produced by thermal evaporation $Q_{se}$, or warm air $Q_{sw}$, or from other sources is [13]:

\[
C_i \frac{d\theta_i}{dt} + Q_i + Q_{cd} = 0 \leftrightarrow R_iC_i \frac{d\theta_i}{dt} + \theta_i - \theta_e + R_iQ_i = 0,
\]

the report $\frac{d\theta_i}{dt}$, temperature gradient is the direction of heat flow, and $Q_i$ is the quantity of heat released in unit time incubation space expressed as:

\[
Q_i = Q_{1} + Q_{2} + \ldots.
\]

In the absence of this release of heat ($Q_i=0$), and considering $\theta_e$ outside air temperature is constant, equation (12), integrated on the time interval $[t_0, t]$, corresponding temperatures and $\theta_{i0}$ and $\theta_i$ the ends of time [15]

\[
\frac{1}{R_iC_i} \int_{t_0}^{t} dt \frac{d\theta_i}{\theta_i - \theta_e} \Rightarrow \frac{t-t_0}{T_0} = \ln \left( \frac{\theta_i - \theta_e}{\theta_{i0} - \theta_e} \right),
\]

final solution will

\[
\theta_i = \theta_e + (\theta_{i0} - \theta_e) \exp \left( \frac{t-t_0}{T_0} \right) = \theta_e \left[ 1 - \exp \left( \frac{t-t_0}{T_0} \right) \right] + \theta_{i0} \exp \left( \frac{t-t_0}{T_0} \right),
\]

where $R_iC_i = T_0$, is the constant heat of the system. If the heat transfer by conduction takes place and the transfer of heat by convection (natural or artificial) $Q_{CV}$, then mass balance equations in the room will be:

- for natural convection,

\[
C_i \frac{d\theta_i}{dt} + Q_i + \frac{\theta_i - \theta_j}{R_i} = D_m \cdot c_{se} \left( \theta_e - \theta_i \right)
\]

- for all air conditioning systems (heating, ventilation and moistening)

\[
C_i \frac{d\theta_i}{dt} + Q_i + \frac{\theta_i - \theta_e}{R_i} = D_m \cdot c_{se} \left( \theta_{ff} - \theta_i \right)
\]

where:
- $D_m$ is the mass flow of fluid circulating in the hall (air) or plant (water) [kg/s];
- $\theta_e$ - initial temperature of the air outside, [$^\circ C$]
- $\theta_{ff}$ - final temperature of the fluid (water) from the heat, [$^\circ C$]
- $\theta_j$ - initial temperature of the fluid from the plant,$^\circ C$;
- $c_{se}$ is specific heat of the fluid circulated in the hall (air), or the heating (water), [J/kg·$^\circ C$].

In the absence of heat release $Q_i=0$, and considering $\theta_e$ outside air temperature is constant, equation (14),
integrated on the time interval \([t_0, t]\), corresponding temperatures \(\theta_i\) and \(\theta_e\), \([12]\)

\[
\int_{t_0}^{t} \frac{d\theta}{T_0 - \theta} = -\int_{t_0}^{t} \frac{dtheta}{\theta_i - \theta_e} \left(D_m R_c - 1\right) \\
\int_{t_0}^{t} \frac{1}{D_m R_c - 1} \ln \left(\frac{\theta_i - \theta_e}{\theta_i - \theta_e}\right)
\]

(17)

final solution will

\[
\theta = \theta_i \left(1 - \exp \left(-\frac{\left(D_m R_c - 1\right)\left(t - t_0\right)}{T_0}\right)\right) + \\
\theta_0 \exp \left(-\frac{\left(D_m R_c - 1\right)\left(t - t_0\right)}{T_0}\right)
\]

(18)

In most practical applications, the amount of heat is expressed in \([W]\), reporting the quantity in \([J]\), the unit of time.

For the amount of heat coming through natural convection \(D_m c_x e(\theta_e - \theta_i)\), \([J]\), using the relationship

\[
nV \rho c_x e(\theta_e - \theta_i) [W],
\]

where:

- \(V\) - hall volume \([m^3]\),
- \(\rho\) - outside air density \([kg/m^3]\),
- \(n\) - number of hours of air exchanges per hour \([1/s]\).

For conditions that have made inquiries, Incubation space is bordered with a desktop, in the natural temperature remains constant. During the exothermic phase Incubation is \(\theta_i < \theta_e\) and the question of disposal of excess heat. Temperature variation was examined for heat transfer by conduction (Fig. 3, Fig. 4) for heat transfer by conduction and convection artificial (Fig. 5, Fig. 6) assuming that \(\theta_i > \theta_e\) and the temperature difference is 1°C.

It is noted that if ventilation (Fig. 5) decrease in temperature is faster. The result of this analysis was verified experimentally as follows:

- in the first round of experiments we have used 4 fans with a total flow of 640 m³/h;
- in the second phase of experiments we have used two fans with the flow 1700 m³/h, one mounted on the inlet pipe and one mounted on the exhaust pipe.

Since buildings may be constructed and under conditions other than those specific to our research, continued analysis of heat transfer for a concrete wall and a composite material, subject to the same average external temperature for 24 hours, using Schedule block in Figure 7, were obtained curves of Figure 8, \([19]\), \([20]\).
behaviour of the two materials under simulation namely a variation of a concrete wall temperature compared to that of wall material composite.

In the first phase of the Incubation stage, phase which takes about 2 days, is required for space heating for Incubation temperature should be maintained between 19 and 23 °C. Using the block diagram in Figure 9, can simulate temperature regulation inside the hall from room temperature inside a reference in a spread, by modifying the block parameters "Thermostat".

![Fig. 7: The thermodynamic [102] room of space.](image)

**Fig. 7**: The thermodynamic [102] room of space.

![Fig. 8: Changes in room temperature for 24 hours for concrete θ_{i-beton} (λ=1,74W/m°C), and composite material and composite θ_{i-compozit} (λ=0,21W/m°C), for θ_{em}=28°C.](image)

**Fig. 8**: Changes in room temperature for 24 hours for concrete θ_{i-beton} (λ=1,74W/m°C), and composite material and composite θ_{i-compozit} (λ=0,21W/m°C), for θ_{em}=28°C.

![Fig. 9: The block structure for regulating the temperature within the space of room.](image)

**Fig. 9**: The block structure for regulating the temperature within the space of room.

If the room no major release of heat, the only disturbance being outside temperature θ_e, which varies between 10°C and 26°C (Fig. 10) and is intended to help maintain the temperature of an air conditioning part [17], observed that the operation of the heating is necessary only in the time the outside temperature is lower than the values prescribed for the inside temperature, 21°C respectively, as only the mass flow of fluid circulating in D_m plant. Figure 10.a shows the process of adjustment during the 24 hours, and in Figure 10.b are detailing this process during a cycle "switched-off". Results of the simulations serve to determine service operation [11] electric motor to drive the fan. To further analyze the phenomenon of heat transfer from the room if it is not built into the ground for periods of autumn - spring. Considered that (Fig. 11) θ_e is the outside temperature varies between 4 and 20°C (curve 1).

![Fig. 10: Variation of the temperature outside (curve 1) and inside (curve 2) room space for θ_{em}=18°C.](image)

**Fig. 10**: Variation of the temperature outside (curve 1) and inside (curve 2) room space for θ_{em}=18°C.

It is noted that the air must operate throughout the period considered. Results of the simulations serve to analyze energy consumption and production scheduling cycle, so that electricity consumption should be reduced as much as possible. It is noted that a facility is required of air, to alter the air temperature and suppress default air temperature of...
the room.

Modeling the phenomenon recirculation air in the event of release of heat, on the one hand, highlights interdependency between climatic variables (pressure-temperature), on the other hand, allows a consistent determination of ventilation used in describing the effectiveness of a ventilated cavity.

In conclusion, this constant will be taken into account when choosing the elements of the implementation of the automation process.

Also demonstrated that the use of composite materials instead of the usual materials of construction is more advantageous in terms of achieving the microclimate conditions, making possible - within certain limits on the temperature outside - a passive air-conditioning (justified according to climatic conditions outside a non-adjustable temperature and, therefore, an air conditioning installation, which involves reducing energy consumption).

In conclusion, the design of rooms must be an economic analysis of investments related to construction materials, on the one hand and the cost of equipment insurance climate, on the other. On the other hand, for an elementary volume of fluid, in motion mono-dimensional the x direction (along the pipe interior), the second of the motion and Newton’s equation of continuity is written [19], as

\[
\frac{\partial H}{\partial x} + \frac{1}{gS} \frac{\partial D}{\partial t} + \frac{k_f D}{2gZS^2} = 0,
\]

and

\[
\frac{\partial D}{\partial x} + \frac{gS}{\nu^2} \frac{\partial H}{\partial t} = 0. \tag{19}
\]

where:

- \(v\) - air velocity [m/s];
- \(D\) - volume flow [m/s];
- \(t\) - time [s];
- \(Z\) - pipe diameter [m];
- \(S\) - area of pipe cross-section [m²];
- \(H\) - total pressure (static and dynamic), expressed in [m], given by the relationship [18]

\[
H = \frac{p}{\rho g}, \tag{20}
\]

where \(p\) is the total pressure [N/m²].

- for the laminar (Re <2000), with the formula of Poiseuille's:

\[
k_f = \frac{16}{Re},
\]

- for the turbulent regime (Re> 3000), with the formula of Colebrook-White:

\[
k_f = \frac{0.25}{41g\left(\frac{k_s}{3.72} + \frac{5.74}{Re^{0.7}}\right)}.
\]

where \(k_s\) is the relative roughness parameter.

Noting with \(H_0\) and \(D_0\) values of absolute total pressure and flow on the outer portion of the conduit, and passing the coordinates relative, \(h = \frac{H}{H_0}\),

\[
d = \frac{D}{D_0},\]

will be achieved

\[
\frac{\partial h}{\partial x} + \frac{D_0}{H_0gS} \frac{\partial d}{\partial t} + \frac{k_f D^2}{2gZS^2 H_0} d|\partial d| = 0,
\]

\[
\frac{\partial d}{\partial x} + \frac{H_0gS}{D_0\nu^2} \frac{\partial h}{\partial t} = 0, \tag{21}
\]
and then into equations,
\[ \frac{\partial h}{\partial x} \rightarrow \frac{\Delta h}{\Delta x}, \quad \frac{\partial h}{\partial t} \rightarrow \frac{d(h)}{dt}, \quad \frac{\partial d}{\partial x} \rightarrow \frac{\Delta d}{\Delta x} \]
resulting
\[ \Delta h = -\frac{D_0 \Delta x}{gH_0 S} \frac{d(d)}{dt} - \frac{k_f D_0^2}{2gZ^2 H_0} dh \]
\[ \Delta d = -\frac{H_0 gS \Delta x}{D_0 v^2} \frac{dh}{dt} \] (22)

Noting reports
\[ \frac{D_0 \Delta x}{gH_0 S} = L, \quad \frac{k_f D_0^2 \Delta x}{2gZ^2 H_0} = R, \quad \frac{H_0 gS \Delta x}{D_0 v^2} = C, \]
equations (22) for a discrete volume of fluid in motion become:
\[ \Delta h = -L \frac{d(d)}{dt} - R dh, \quad \Delta d = -C \frac{dh}{dt}. \] (23)

Based on these equations to establish a model analog of the heating of the incubation space in the form of an electrical circuit in a "T" in Figure 12.

Structural block scheme for the analysis of heating, during the liberation of heat by the mushrooms is depicted in Figure 13 and corresponding electrical equivalent circuit in Figure 12. The airing of the room space is equivalent to connecting the electrical circuit in a “T” to an alternative source of power (Fig. 14) [20]. Efficiency room space ventilation can be established with constant ventilation
\[ T_C = \frac{H_0 S_C}{D_0}, \]
here \( S_C \) is cross-sectional area covered by discrete volume of fluid.

In technical air conditioning the premises shall be deemed recirculation processes are isobar. However during the research, noted that the start ventilation fans for the exothermic stage, the pressure variations occur. It is believed that research can be continued in the direction of pressure on the analysis of the influence of heating process of the room space, where the use of fans supplied by static converters. For this purpose it is proposed the model in Fig. 15.

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6 Conclusion
In this paper, we study the null controllability of a class of degenerate parabolic equations in a bounded domain.

Null controllability of non degenerate parabolic equations has been recently widely studied, using
Carleman estimates. Roughly speaking, in the non degenerate case, the following result, there exists a control that drives the solution to zero on the holds: given $T>0$ and an initial condition $u_0$ whole domain at time $T$. However many physical problems are described by degenerate parabolic equations.

The main difficulty in the study of degenerate parabolic equations comes from the fact that in general it is not possible to find a control that drives the solution to zero on the whole domain. This is why we will study regional null controllability properties: the problem is to find a control that drives the solution to zero on some part of the domain. The proof follows from the observability inequality (8), obtained via Carleman estimates and well hosen-cut-off functions.

This notion of persistent regional null controllability allows us also to extend classical results on the (non degenerate) heat equation in a bounded domain when the initial condition is compactly supported in the domain, and to extend also some results on the null controllability of the heat equation in an unbounded domain, for which proved that global null controllability does not hold if the control region is bounded.

Of section through the experimental results the following conclusions:

Analysis of microclimate in the event of release of heat, on the one hand, highlights interdependeting between climatic variables (pressure-temperature), on the other hand, allows a consistent determination of ventilation used in describing the effectiveness of ventilation. In selecting items for the implementation of ventilation used in de.

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