

Yaw Phase Mode Attitude Control Using Z Wheel for LEO Microsatellite

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Abstract: A control system is proposed for a low Earth orbit gravity gradient stabilised microsatellite using Z wheel. The microsatellite is 3-axis stabilized using a yaw reaction wheel, with dual redundant 3-axis magnetorquers. Two vector magnetometers and four dual sun sensors are carried in order to determine the full attitude. The attitude was estimated using an Euler angles (small libration version) on based extended Kalman filter (EKF). After the satellite has been detumbled and deploy the gravity gradient boom, in order to have the accurate Nadir pointing we will use the Z zero-bias mode controller. The Z momentum wheel will be damped by the magnetorquers. This paper describes the attitude determination and control system design of LEO microsatellite using Z reaction wheel for yaw phase mode control.

Keywords: Modelling, Simulation, Microsatellite, LEO, Attitude, Yaw, Control, Z Wheel, Magnetorquer.

1 Introduction

Small low cost satellites are becoming more important in the last few years when the possibility of piggyback launch opportunities. The aim of this control system is to achieve a stable Earth pointing attitude, maximizing the pointing accuracy and minimizing the control energy, within the limitation of the existing low cost technology.

A possible resource to be explored for improved performance of future low cost satellites is the processing capability of on board microprocessors. Innovative attitude control theory, more explicitly discrete time estimators, and control laws can be used to obtain this goal. As an example, a small satellite controller, making use of a gravity gradient (GG) boom, and coils (magnetorquers) to maintain an Earth pointing attitude [17].

The motion of a spacecraft presents two dynamic aspects of interest. The most obvious one is the trajectory traced by its center of mass which is governed by the classical Keplerian relations. The other is rotational motion about its center of mass, commonly referred to as libration, which is our attention. Due to the influence of internal and external torque, the undesirable orientation must be controlled for successful completion of a given mission [2].

A wide range of attitude control concepts has been proposed over the years and several have practical application. In general, they might be classified as active, passive, and semi passive procedures. The active approach use energy available on board the satellite. The passive and semi-passive systems, on the other hand, exploit the environmental forces for stabilization and control [15].

Passive stabilization techniques using gravity gradient torques have been in use for a long time, specifically for damping the libration motion of a spacecraft. This technique does not use any additional sensors or actuators, if the spacecraft can be designed in such a way that it is a gravity gradient stabilized. Even though this technique works well; it generally requires a long time to accomplish the libration damping (on the order of a few days). Moreover the attitude control errors are fairly loose (5° to 10°), which may be adequate to meet some mission requirements [12].

To improve the libration damping time and the attitude control errors, an active magnetic control technique using three torquorods has been suggested for a class of small satellites ranging in total mass from 40 to 200kg. This active control can reduce the libration damping time from days to a few orbits, and can achieve attitude control errors of less than 3° for roll, 2° for pitch, and 5° for yaw [14].

The proposal satellite attitude determination and control system uses a Z reaction wheels, gravity gradient boom (6 meter + 3 kg tip mass) and 3-axis magnetorquer rods. The magnetorquer rods do momentum maintenance and nutation damping for Z wheel, libration damping and yaw phase control.

The Z wheels are used for the following control functions on satellite [1], [3], [7]

- Yaw control for push broom for Earth observation;
- Quick transfer between BBQ mode and yaw steering for thermal control;
- Z disturbance cancellation during X thruster firings for orbital control;

2 Attitude Dynamic Modelling

In common with boats and aircraft the orientation of a spacecraft can be defined by three angles (roll, pitch, and yaw). These angles are obtained from a sequence of right hand positive rotations from a reference X_R, Y_R, Z_R frame to a X_B, Y_B, Z_B set of spacecraft body axes. There are 12 possible sequences of rotations, which can be expressed using Euler angles. One example is a 2-1-3 sequence rotation. The first rotation is a pitch about the reference Y_R axis, this defines a pitch angle θ . The second rotation is a roll about the intermediate L axis, this define a roll angle φ . The last rotation is a yaw about the body Z_B axis, this define a yaw angle ψ . The attitude matrix, \mathbf{A} , which transforms an arbitrary vector from the reference X_R, Y_R, Z_R coordinates to the spacecraft body X_B, Y_B, Z_B coordinates can be expressed as [18]:

$$\mathbf{A} = \begin{bmatrix} c\psi c\theta + s\psi s\phi s\theta & s\psi c\phi & -c\psi s\theta + c\psi s\phi c\theta \\ -s\psi c\theta + c\psi s\phi s\theta & c\psi c\phi & s\psi s\theta + c\psi s\phi c\theta \\ c\phi s\theta & -s\phi & c\phi c\theta \end{bmatrix} \quad (1)$$

Where

- φ : Roll angle;
- θ : Pitch angle;
- ψ : Yaw angle;
- c : cosine function;
- s : sine function.

The dynamics of the spacecraft in inertial space is governed by Euler's equations of motion can be expressed as follows in vector form [15], [18]

$$\mathbf{I}\dot{\boldsymbol{\omega}}_B^I = \mathbf{N}_{GG} + \mathbf{N}_D + \mathbf{N}_M + \mathbf{N}_T - \boldsymbol{\omega}_B^I \times (\mathbf{I}\boldsymbol{\omega}_B^I + \mathbf{h}) - \dot{\mathbf{h}} \quad (2)$$

Where $\boldsymbol{\omega}_B^I$, \mathbf{I} , \mathbf{N}_{GG} , \mathbf{N}_D , \mathbf{N}_M and \mathbf{N}_T are respectively the inertially referenced body angular velocity vector, moment of inertia of spacecraft, gravity-gradient torque vector, applied magnetorquer control firing, unmodelled external disturbance torque vector such as aerodynamic or solar radiation pressure.

The rate of change of the quaternion is given by

$$\dot{\mathbf{q}} = \frac{1}{2} \boldsymbol{\Omega} \mathbf{q} = \frac{1}{2} \boldsymbol{\Lambda}(\mathbf{q}) \boldsymbol{\omega}_B^O \quad (3)$$

Where

$$\boldsymbol{\Omega} = \begin{bmatrix} 0 & \omega_{oz} & -\omega_{oy} & \omega_{ox} \\ -\omega_{oz} & 0 & \omega_{ox} & \omega_{oy} \\ \omega_{oy} & -\omega_{ox} & 0 & \omega_{oz} \\ -\omega_{ox} & -\omega_{oy} & -\omega_{oz} & 0 \end{bmatrix} \quad (4)$$

$$\boldsymbol{\Lambda}(\mathbf{q}) = \begin{bmatrix} q_4 & -q_3 & q_2 \\ q_3 & q_4 & -q_1 \\ -q_2 & q_1 & q_4 \\ -q_1 & -q_2 & -q_3 \end{bmatrix} \quad (5)$$

Where

$\boldsymbol{\omega}_B^O = [\omega_{ox} \ \omega_{oy} \ \omega_{oz}]^T$ = body angular velocity vector referenced to orbital coordinates.

3 Attitude Determination Modelling

A Kalman filter is an optimal, recursive, data processing algorithm [1], [11] and [16] all address Kalman filtering for spacecraft attitude estimation.

The attitude was estimated using a Euler angles (small libration version) based extended Kalman filter (EKF) [2], [6]. This filter uses measurement vectors (in the body frame) from all the attitude sensors and by combining them with corresponding modeled vectors (in a reference frame) [10], [13] it estimates the attitude of the satellite.

The attitude sensors (magnetometer, sun sensor) will be used to determine the attitude of the satellite relative to the orbital frame. When using magnetic field data: a GPS receiver or an orbital propagator is used to obtain the position of the satellite. Using this position data, a model of the geomagnetic field, the International Geomagnetic Reference Field (IGRF) model, computes the geomagnetic **B**-field in orbit coordinates. On the other hand, the magnetic **B**-field is also measured by the 3-axis magnetometer in body coordinates. The attitude can then be solved from these two vectors over time.

The EKF cycle is given as follows [9]:

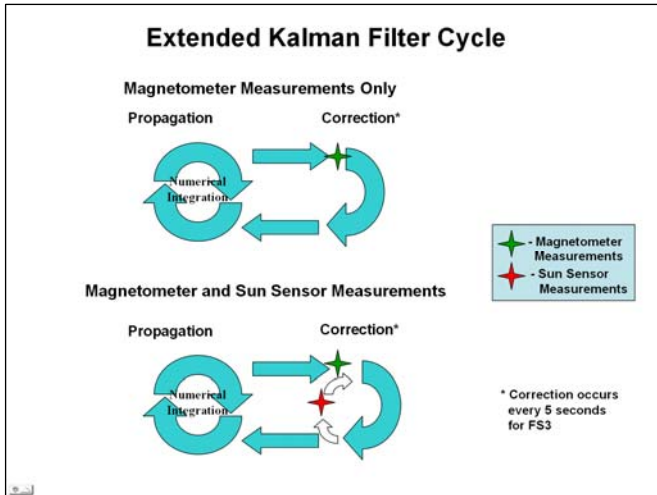


Fig. 1 Extended Kalman Filter Cycle

In order to damp nutation of the satellite after boom deployment, it is required to obtain roll, pitch and yaw rate and attitude knowledge. Therefore we have to design an estimator including Y/Z wheel under the restriction of the processing power of an OBC 186.

The Kalman filter design should be only valid under the strict assumption of a small roll and pitch oscillation of Alsat-1 [1], [6].

The state vector to be estimated is 6 dimensional such that

$$\mathbf{X} = [\phi \ \theta \ \psi \ \dot{\phi} \ \dot{\theta} \ \dot{\psi}] \quad (6)$$

3.1 System Equation

If the satellite is axially symmetric and the small libration angle can be assumed, then the system equation becomes

$$\begin{aligned} \ddot{\phi} &= (4\omega_0^2 \left(\frac{I_z}{I_T} - 1\right) + \frac{h_y \omega_0}{I_T})\dot{\phi} + \left(\frac{I_z}{I_T} \omega_0 + \frac{h_y}{I_T}\right)\dot{\psi} \\ &\quad + \frac{h_z \omega_0}{I_T} - \frac{h_z}{I_T} \dot{\theta} + \frac{N_x^{MT}}{I_T} + w_x \\ \ddot{\theta} &= 3\omega_0^2 \left(\frac{I_z}{I_T} - 1\right)\dot{\theta} + \frac{h_z}{I_T} \dot{\phi} - \frac{h_z \omega_0}{I_T} \dot{\psi} - \frac{\dot{h}_y}{I_T} \\ &\quad + \frac{N_y^{MT}}{I_T} + w_y \\ \ddot{\psi} &= \left(-\frac{h_y}{I_z} - \omega_0\right)\dot{\phi} + \frac{h_y \omega_0}{I_z} \dot{\psi} - \frac{\dot{h}_z}{I_z} + \frac{N_z^{MT}}{I_z} \\ &\quad + w_z \end{aligned} \quad (7)$$

Where

θ : Roll angle in rad ;

ϕ : Pitch angle in rad ;

ψ : Yaw angle in rad;

$w = [w_x \ w_y \ w_z]$ zero mean system noise vector;

$N = [N_x^{MT} \ N_y^{MT} \ N_z^{MT}]$ applied magnetorquer control firing;

$I = \text{diag} [I_T \ I_T \ I_z]$ moment of inertia tensor of the spacecraft;

$h = [0 \ h_y \ h_z]$ wheel angular momentum vector;

ω_0 : orbital rate.

Notice that equation (7) claims that the pitch dynamics is de-coupled. The dimension of state vector to be estimated is 6, which requires manipulating many 6x6 matrices. This is not ideal both from a program-size as well as a processing time point of view. Therefore we should take advantage of the de-coupled nature of equation (7) and design the Pitch and Roll/Yaw estimator separately.

3.1.1 Roll/Yaw Estimator:

We have used a standard Kalman filter algorithm to implement the Roll/Yaw. The state transition matrix Φ and the observation matrix \mathbf{H} would sufficient to design the Kalman filter. For the state vector we have

$$\mathbf{X} = [\phi \ \psi \ \dot{\phi} \ \dot{\psi}] \quad (8)$$

$$\Phi \approx \begin{bmatrix} 1 & 0 & \Delta t & 0 \\ 0 & 1 & 0 & \Delta t \\ \Phi_{31} & 0 & 1 & \Phi_{34} \\ 0 & \Phi_{42} & \Phi_{43} & 1 \end{bmatrix} \quad (9)$$

where

$$\Phi_{31} = (4\omega_0^2 \left(\frac{I_z}{I_T} - 1\right) + \frac{h_y \omega_0}{I_T}) \Delta t$$

$$\Phi_{34} = \left(\frac{I_z}{I_T} \omega_0 + \frac{h_y}{I_T}\right) \Delta t$$

$$\Phi_{42} = \frac{h_y \omega_0}{I_z} \Delta t$$

$$\Phi_{43} = \left(-\frac{h_y}{I_T} - \omega_0\right) \Delta t$$

and

$$\mathbf{H} \approx \begin{bmatrix} H_{11} & H_{12} & 0 & 0 \\ H_{21} & H_{22} & 0 & 0 \\ H_{31} & 0 & 0 & 0 \end{bmatrix} \quad (10)$$

$$H_{11} = s\psi M s m t_z$$

$$H_{12} = -M s m t_x s \psi + M s m t_y c \psi + (\theta s \psi + \phi c \psi) M s m t_z$$

$$H_{21} = c\psi M s m t_z$$

$$H_{22} = -M s m t_x c \psi - M s m t_y s \psi + (\theta c \psi - \phi s \psi) M s m t_z$$

$$H_{31} = -M s m t_y$$

Where

c : cosine function;

s : sine function.

Where Δt is the measurement sampling time, which is planed to be 10 seconds, and $M s m t_i$ is the vector components of predict magnetic field vector or solar vector with respect to orbit-referenced coordinate.

The process matrix noise is

$$\mathbf{Q} \approx \begin{bmatrix} \frac{\sigma_\phi^2(\Delta t)^3}{3} & 0 & 0 & 0 \\ 0 & \frac{\sigma_\psi^2(\Delta t)^3}{3} & 0 & 0 \\ 0 & 0 & \sigma_\phi^2 \Delta t & 0 \\ 0 & 0 & 0 & \sigma_\psi^2 \Delta t \end{bmatrix} \quad (11)$$

3.1.2 Pitch Estimator :

The design of pitch estimator is even simpler. The state transition matrix Φ and the observation matrix \mathbf{H} is given by

$$\Phi \approx \begin{bmatrix} 1 & \Delta t \\ 3\omega_0^2 \left(\frac{I_z}{I_T} - 1\right) \Delta t & 1 \end{bmatrix} \quad (12)$$

and

$$\mathbf{H} \approx \begin{bmatrix} -M s m t_z c \psi & 0 \\ M s m t_z s \psi & 0 \\ M s m t_x & 0 \end{bmatrix} \quad (13)$$

The process matrix noise is

$$\mathbf{Q} \approx \begin{bmatrix} \frac{\sigma_\theta^2(\Delta t)^3}{3} & 0 \\ 0 & \sigma_\theta^2 \Delta t \end{bmatrix} \quad (14)$$

Note that to compute the observation matrix for the roll/yaw estimator, the pitch angle knowledge is required, while to compute the observation matrix for the pitch estimator, the yaw angle knowledge is required. Therefore the following procedure is often employed on the real satellite flight code:

- Propagate the roll, pitch and yaw based on the previous estimation of the roll, pitch and yaw angles by both estimators.
- Using propagated pitch, the observation matrix for the roll/yaw estimator is obtained and the roll and yaw are updated by the roll/yaw estimator.
- Using updated roll and yaw, the observation matrix for the pitch estimator is obtained and the pitch is updated by the pitch estimator.

when 2 vector measurements are available, such as the magnetometer measurement and the sun sensor measurement at the same sampling time t_k , the usual procedure in the estimator is as follows:

- Propagate the state vector and covariance.
- Using less accurate sensor measurement vector (magnetometer measurement) first, update the state vector and covariance.
- Successively using more accurate sensor measurement vector (sun sensor measurement) update the state vector and covariance.

However, if 2 or more vectorial measurements (such as by star sensors) are assumed, then it can be possible to obtain the direction cosine matrix - or attitude matrix standard pseudo-inverse method. This means that the attitude parameter itself - Euler angles or quaternion - can be the measurement of the estimators.

3.2 State Propagation

A simple second order Adams integrator would sufficient to propagate the state by integration of equation (7). The second Adams integrator is defined by

$$\mathbf{X}_{n+1} = \mathbf{X}_n + \frac{1}{2}(3\dot{\mathbf{X}}_n - \dot{\mathbf{X}}_{n-1})dt \quad (15)$$

Where dt is the integration step size (not sampling time).

4 Magnetic Wheel Torquer Control Law

Reaction wheels are essentially torque motors with high-inertia rotors. They can spin in either direction. Roughly speaking one wheel provides for the control of one axis.

Magnetorquers generate magnetic dipole moments whose interactions with the Earth's magnetic field produce the torques necessary to remove the excess momentum. The magnetic torque vector can be expressed as the cross product of the magnetic dipole moment \mathbf{M} of the magnetic coils with the geomagnetic field strength \mathbf{B} in the body frame [4], [14]:

$$\mathbf{N}_M = \mathbf{M} \times \mathbf{B} \quad (16)$$

Where

\mathbf{M} : magnetic dipole control moment vector;

The following cross-product control law is used

$$\mathbf{M} = \frac{\mathbf{e} \times \mathbf{B}}{\|\mathbf{B}\|} \quad (17)$$

Where

\mathbf{B} : Magnetometer measured magnetic field vector;

The error vector for a magnetorquer cross-product controller including Z wheel is given by [2]

$$\mathbf{e} = \begin{bmatrix} Kd_x \omega_{ox} / \omega_0 \\ Kd_y \omega_{oy} / \omega_0 \\ K_z (h_z - h_{z-ref}) \end{bmatrix} \quad (18)$$

Where

\mathbf{M} : Magnetorquer switch-on time;

Kd : Derivative gain;

ω_0 : Orbit angular rate in rad/s;

ω_{0x}, ω_{0y} : X and Y orbit referenced angular rate of the satellite in rad/s;

K : Momentum maintenance gain constant;

h_{z-ref} : Reference yaw wheel momentum (nominally 0.052 Nms);

h_z : Yaw wheel momentum measurement in Nms;

ϕ, θ, ψ : Roll, Pitch and Yaw angle in rad;

The feedback control law for the Z wheel is given by

$$N_{z-wheel} = Kd_z \omega_z^0 + Kp_z (\psi - \psi_{ref}) \quad (19)$$

$$h_{z-wheel-cmd} = \int N_{z-wheel} dt / I_{z-wheel} \quad (20)$$

Where Kp_z, Kd_z is the controller gain constant, ω_{oz} is the orbit reference angular rate, and $N_{h_{wheel}}$ is the commanded wheel torque vector.

5 Simulation Results

The magnetic moment in the orthogonal X, Y and Z-axes was assumed to be equal to 10 Am^2 each. The Z reaction wheel has a MOI of 8.10^{-4} kgm^2 and the maximum speed is $\pm 5000 \text{ rpm}$. The maximum wheel torque is 5 milli-Nm.

We assume that we have gravity gradient torque and aerodynamic torque as external torque.

An International Geomagnetic reference Field (IGRF) model was used to obtain the geomagnetic field values.

A sampling period of $TS = 10$ seconds was utilised for the discrete filter algorithm.

To initialize the full state filter we use the yaw filter [5].

5.1 Optimal Gain Choice for the Magnetorquer Cross-Product Controller plus Z Wheel

The main goal of this section is how to choose the gain of the error vector Eq.(14) against the average magnetorquer power drain, the total accumulated on time of magnetorquer, Euler angles RMS and Euler angles RMS error.

For this simulation we are going to compute the Euler angles RMS and the Euler angles RMS error when the yaw angle is commanded to 0° [170°, respectively] and we are using estimator (magnetometers plus sun sensors).

Simulations done, the optimal gain is given as follows

Table 1. Optimal gain for the magnetorquer cross-product controller plus Z wheel

Kd_x	Kd_y	K_z
10	10	25

5.2 Yaw Phase Mode Accuracy State

Figure 2 to 5 presents the results of magnetorquer plus Z wheel yaw phase mode. The satellite is left to librate freely for the two orbits starting from an initial attitude of 3° roll, 0° pitch, 0° yaw, 0°/sec roll rate, 0°/sec pitch rate and 0.6°/sec yaw rate. At the start of the third orbit the magnetorquer plus Z reaction wheels activated and within one orbits the pitch and roll librations are damped to nadir pointing error of less than 2°, the yaw angle is controlled to 0°. At the start of the eighth orbit the yaw angle is commanded to 170° for six orbits.

The total accumulated on time of magnetorquer is approximately 9092 seconds during a active control window of 12 orbits (72000 seconds). This gives an average magnetorquer power drain of 0.10 Watt from the start until the attitude is achieved.

Table 2. Euler angles RMS

(Yaw angle is commanded to 0 deg)

Roll	Pitch	Yaw
0.06 deg	0.08 deg	0.20 deg

Table 3. Error Euler angles RMS

(Yaw angle is commanded to 170 deg)

Roll	Pitch	Yaw
0.05 deg	0.20 deg	0.25 deg

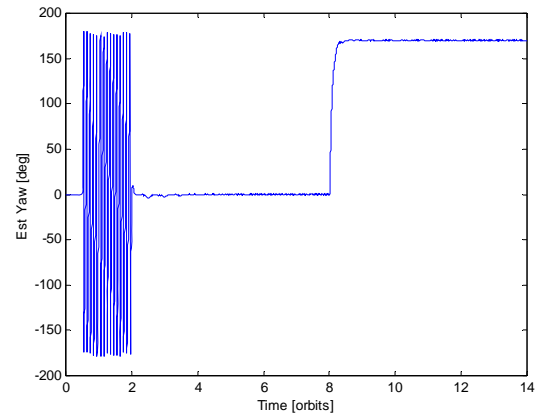


Fig. 2 Estimated yaw angle during yaw phase control

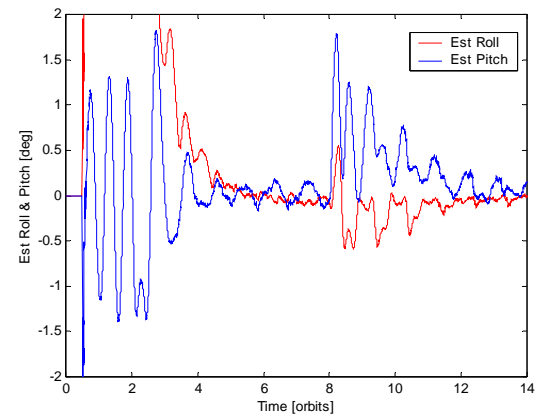


Fig. 3 Estimated roll/pitch angle during yaw phase control

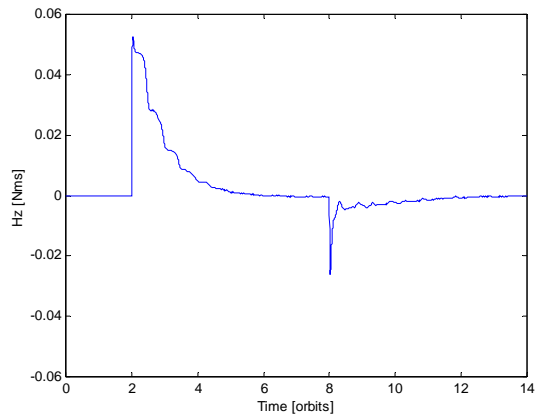


Fig. 4 Z Wheel momentum during yaw phase control

6 Conclusion

The proposed attitude determination and control system was tested on 3-axis stabilized satellite, using yaw reaction wheel, with dual redundant 3-axis magnetorquers. We have demonstrated successful operation of Z wheel controller on a gravity gradient stabilised satellite.

To conclude, a low cost and light weight attitude determination and control system was proposed to be used by three axis Nadir stabilised platform satellite.

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