## A Reconfigurable FEC system based on Reed-Solomon codec for DVB and 802.16 network

LAMIA CHAARI, MOHAMED FOURATI, NOURI MASMOUDI, LOTFI KAMOUN Electronic and Information Technologies Laboratory (L.E.T.I) Sfax National Engineering School, 3038 SFAX TUNISIE Lamia.chaari@tunet.tn Mohamed.Fourati@isecs.rnu.tn

*Abstract:* This article proposes, a reconfigurable FEC system based on Reed-Solomon codec for DVB and WiMax networks. The proposed architecture implements various programmable primitive polynomials. A lot of VLSI implementations have been described in literature. This paper introduces a highly parametrical RS-coder-decoder on FPGAs. The implementation, written in a hardware description language (HDL), is based on an Berlekamp massey, Chain and Formey Algorithms. We have defined an advanced RS encoder-decoder architecture based on parameterization approach which is a key solution for software defined radio (SDR) systems. Our parameterization approach is used in order to implement on FPGA a generic RS coder-decoder for DVB and WiMax networks. IEEE Std. 802.16 specifies that the codec performs a variable number of check symbols in a codeword ( ranges from 0 to 32, inclusive). The value of check symbols are specified for each burst profile by the MAC layer according to cross layer concept.

*Keywords and phrases:* Reedsolomon, Berlekamp massey, Chain, Formey, FPGA, implementation , VHDL, WiMax, DVB.

#### **1 Introduction:**

Reed-Solomon (RS) codes are described in a paper by Reed and Solomon in 1960[1]. RS are powerful error correcting codes that can be employed in a wide variety of digital communications systems from digital media to wireless communications and deep-space probes as well as in memory and storage systems. Reed-solomon codes are used to correct errors in many systems including:

- storage devices (compact disk, DVD, barcodes,etc...) [2,3],
- wireless and mobile communications (including cellular telephones, microwave links, etc...)[4, 5],
- digital satellite communications[6],
- digital television, digital video broadcasting (DVB)[7],
- high speed modem such as ADSL, Xds1...[8]
- power line communications (PLC) [9]
- digital vestigial sideband (VSB) system
   [10]
- cable modem [11],

The speed and complexity of these systems necessitate designers and researchers to break a way from traditional architectures and design methodologies. A design combining software and hardware is flexible enough to make it optimal for 4th generation systems [12].

Field programmable gate arrays (FPGA) have evolved from being a flexible logic design platform to a signal-processing engine [13]. An increasing number of signal processing functions in FPGA and several capabilities like embedded memory and advanced routing. The availability of high density and high performance make them highly designable for developing hardware prototypes of communication systems.

Parameterization [14] is a new field of study derived from software radio domain. This field proposes a new approach in which similarities and differences between systems and standards must be identified and then parameterized. We can distinguish two types of parameterization either by common functions or by common operators. Parameterization by common operators, it consists to find a common operator of the highest level, which would be used by the maximum functions of many standards including future standard. Parameterization by common functions, it consists to identify the common functions of all standards that will be implemented in reconfigurable systems.

In addition, since past research has proposed several efficient algorithms [15, 16, 17] and architectures [18,19, 20] for the RS coderdecoder that could be used as parameters for an advanced reconfigurable architectures.

This article is structured in eight sections. Section 2 provide a brief description of Reed-Solomon codes. Section 3 describes RS codec architectures and is sketching briefly the principle functionality of RS decoder. In section 4, several implementation RS coderdecoder architectures are studied. Section 5 discuss parameterization approach used in order to implement a reconfigurable RS coderdecoder for DVB, mobile and wireless systems. Section 6 explains our conception and an optimized FPGA implementation of a reconfigurable FEC systems based on RS codes used in new generation systems. Design decisions and simulation results of the verification process are reported and discussed in section 7. Finally, we summarize and conclude this article in section 8; also we propose some recommendations for future research.

## 2 Reed-Solomon CODECs:

Reed Solomon (RS) codes are a subset of Bose Chaudhuri-Hochquenghem (BCH) codes [21 22] and are linear block codes[23]. They are powerful error-correcting codes whose symbols are chosen from a finite field, GF(m). Their non-binary nature makes them particularly suitable to correct error bursts.

A Reed-Solomon code is specified as RS(n,k) with m-bit symbols. This means that the encoder takes k data symbols of s bits each and adds parity symbols to make an n symbol codeword. There are n-k parity symbols of s bits each. A Reed-Solomon decoder can correct up to t symbols that contain errors in a codeword, where 2t = n-k.

If the location of the symbol errors is marked as an erasure, the RS decoder can correct twice as many errors. External circuitry identifies which symbols have errors and passes this information to the decoder using the eras\_sym signal. The eras\_sym input indicates an erasure (when the erasuressupporting decoder option is selected).

#### 2.1 Encoding of Reed-Solomon codes

Let  $(u_0, u_1, u_2,..., u_{k-1})$  denote k m-bit data symbols. These symbols are encoded into a codeword  $(c_0, c_1, c_2,..., c_{n-1})$ . This encoding process is best described in terms of data polynomial:

$$I(x) = u_0 + u_1 x + u_2 x^2 + \dots + u_{k-1} x^{k-1}$$
(1)  

$$C(x) = c_0 + c_1 x + c_2 x^2 + \dots + c_{n-1} x^{n-1}$$
(2)

C(x) are polynomial multiple of G(x), which is the generator polynomial of the code, which is defined as

$$G(x) = \prod_{i=0}^{2t-1} (x - \alpha^{(m0+i)})$$
(3)

where  $m_0$  is typically 0 or 1 Since 2t consécutive power  $\alpha^{m_0}, \alpha^{m_{0+1}}, \dots, \alpha^{m_{0+2t-1}}$  of  $\alpha$  are rootsof G(x), C(x) is amultiple of G(x), it follows that

$$C(\alpha^{(m0+i)})=0,0\leq i\leq 2t-1$$
 (4)

for all codeword polynomials C(x). In fact, an arbitrary polynomial of degree less than n is a codeword polynomial if and only if it satisfies equation 4.

Asystematic encoding produces codeword polynomials that are comprised of data followed by parity check symbols (figure 1), and it is obtained as follows (Equation 5)

n	_
k	2t
Data I(x)	Pariy Pa(x)

Figure 1: RS encoding

$$Pa(x) = (x^{2t} * I(x)) \mod G(x)$$
(5)

It follows that the codeword is given by  $(C_{n-1}, C_{n-2}, \ldots, C_1, C_0) = (u_{k-1}, u_{k-2}, \ldots, u_1, u_0, P_{n-k-1}, P_{n-k-2}, \ldots, P_1, P_0)$  and consists of the data symbols followed by the check symbols.

In digital hardware, the encoder is an LFSR with internal feedback connections corresponding to G(x), as seen in Figure 2. The operations involved are GF addition and multiplication. The computation of the remainder is implemented on digital hardware using a linear feedback shift register configuration as shown in Figure 2. The final contents of the shift registers will contain the remainder.



Figure 2: Typical RS encoder implementation

#### 2.2 Decoding of Reed-Solomon codes

The general decoding steps are illustrated in Figure 3. The syndrome calculator generates a set of syndromes from the received codeword polynomial R(x). From the syndromes, the key equation solver produces the error locator polynomial  $\sigma(x)$  and the error evaluator polynomial  $\Omega(x)$  which can be used by the Chien Search and the Error Value Evaluator to determine the error locations and error values, respectively.



Figure 3: The simplified Reed-Solomon decoding flowchart.

## **3 RS decoding Algorithms study**

#### 3.1 Syndrome computation

The Syndrome calculation block treats the input codeword as a series of polynomial coefficients and calculates syndrome а polynomial of 2t coefficients. The syndrome polynomial contains the location and magnitude of up to t errors in an invalid codeword. A valid codeword generates a syndrome polynomial with all zero coefficients.

Assuming a corrupt transmission, the received codeword R consists of the original codeword which is superposed by the error E:

By definition the syndrome polynomial is S(x)

$$S(x) = \sum_{i=1}^{2t} S_{iX}^{(i-1)}, \ S_i = R(\alpha^i) , \qquad (6)$$

$$\mathbf{R}(\mathbf{x}) = \mathbf{R}_0 + \mathbf{R}_1 \mathbf{x} + \mathbf{R}_2 \mathbf{x}^2 + \dots + \mathbf{R}_{N-1} \mathbf{x}^{N-1}$$
(7)

then 
$$S_i = R_0 + \alpha^i (R_1 + \alpha^i (R_2 + .... + \alpha^i (R_{N-1})))$$
 (8)

where R(x) is a received polynomial and  $R_{N-1}$  is the first received symbol into a syndrome cell.

This structure describe a recursive operation multiplies and accumulates a constant value  $\alpha^{I}$  with the input data. As shown in Figure 4(a), at each cycle, the partial syndrome is multiplied with and accumulated with the received symbol. After all the received symbols are processed, the accumulated result is the i<sup>ème</sup> syndrome. Figure 4(b) shows how the 16 syndrome cells (for t= 8) are organized in our chip. By controlling the multiplexer in Figure 4(b), we can generate different syndrome sequences for the calculation of the discrepancy in the key equation solver. Table I shows all 16 different syndrome sequences [24].



Figure 4 (a) Syndrome cell S



Figure 4 (a) Syndrome cell S

#### 3.2 Key Equation Solver

The main component of an RS-decoder is the key equation calculation block. It solves a set of 2t linearly dependent equations. It generates the key equations ( $\sigma(x)$ : locator polynomial and  $\Omega(x)$ : evaluator polynomial) from the syndrome polynomials. The locator polynomial contains information about the location of bad symbols in the codeword. The evaluator polynomial contains information about the error magnitude of the bad symbols. The two polynomials  $\sigma(x)$  and  $\Omega(x)$  are defined respectively by the following equations 9 and 10.

$$\sigma(x) = \prod_{i=1}^{w} \left( 1 - x \cdot X_i \right) \tag{9}$$

where w: is the number of errors occurs in R(x).

$$\Omega(\mathbf{x}) = \sum_{i=1}^{W} Y_i X_i \quad \prod_{j=1, j \neq i}^{W} (1 - X_j * \mathbf{x})$$
(10)

The two polynomials are related to S(x) through the Key equation (Eq11) [25, 26], so we can determine the above two unknown polynomials  $\sigma(x)$  and  $\Omega(x)$  by solving the key equation:

$$S(x) * \sigma(x) = \Omega(x) \mod x^{2t}$$
(11)

The techniques frequently used to solve the key equation include the Berlekamp–Massey algorithm [25,27,28,29], the Euclidean algorithm [29,30]. Compared to the Euclidean algorithm, the Berlekamp–Massey algorithm is generally considered to be the one with the least hardware complexity [31].

#### 3.2.1 Berlekamp-Massey algorithm

One of the fastest and hence often preferred algorithm is the so called "Berlekamp Massey Algorithm" (BMA) that solves

$$\sum_{w}^{2t-1} \sigma(x)S(x) = 0, \qquad (12)$$

where  $W \le t$  is the number of errors that have occurred. So eq 12 can be developed as Eq 13  $S_{w+1} + \sigma_1 S_w + \sigma_2 S_{w-1} + \dots + \sigma_w S_1 = 0$  $S_{w+2} + \sigma_1 S_{w+1} + \sigma_2 S_w + \dots + \sigma_w S_2 = 0$  $\dots$  $S_{2t} + \sigma_1 S_{2t-1} + \sigma_2 S_{2t-2} + \dots + \sigma_w S_{2t-w} = 0$ 

The problem of finding the minimum-degree solution to the key equation is the same as trying to find the smallest (LFSR)  $\sigma(\Box x)\Box$ , that generates the first 2t terms of S (figure 5).

The algorithm aims to find an LFSR of minimal length such that the first (2t) elements in the LFSR output sequence are the (2t) syndromes. The taps of this shift register are the coefficients of the desired error locator polynomial,  $\sigma(x)$  [33].



Figure 5 : Berlekamp–Massey algorithm based on LFSR implementation

$$S_{j} = -\sum_{i=1}^{w} \sigma_{i} * S_{j-i}$$

If syndrome values are known, we can compute  $\sigma(x)$  polynomial by the following diagram (figure6)



Figure 6: Barlekamp massey algorithm [32]

The implementation was a purely functional VHDL description.

3.2.2 Error Magnitudes polynomial Computing Solving the key equation (Eq. 11) determines the error evaluator or error magnitude polynomial,  $\Omega(x)$ . An efficient way of computing  $\Omega(x)$  is to perform parallel computation of  $\sigma(x)$ . Using the Berlekamp– Massey algorithm, this involves an iterative algorithm to compute. However, if is first obtained, from the key equation and the Newton's identity we could derive as follows:

$$\begin{aligned} \Omega(x) &= S(x)\sigma(x) \mod x^{2t} \\ &= (S_1 + S_2 x + \dots + S_{2t} x^{2t-1}) \bullet \\ &\quad (\sigma_1 + \sigma_2 x + \dots + \sigma_i x^i) \mod x^{2t} \\ &\equiv \Omega^{(0)} + \Omega^{(1)} x + \dots + \Omega^{(t-1)} x^{t-1} \\ \Omega^{(i)} &= S_i + i \sigma_0 + S_i \sigma_1 + \dots + S_I \sigma_i , \\ &\quad i = 0, 1, \dots, t-1 \end{aligned}$$

The penalty of this efficient computation is the additional latency because  $\sigma(x)$  and  $\Omega(x)$ are computed in sequence.

#### **3.3Chien Search Algorithm**

With the known error locator polynomial it is possible to determine the error locations by checking whether the error locator polynomial equals zero or not. The roots of the errorlocator polynomial are the inverse error locations of the codeword. To find the roots of the polynomial, a Chien Search (CS) was conducted. It uses all possible input values and then checks to see if the outputs are zero. This happens only when an error occurs. For each element that is substituted into the polynomial that equates to zero, the element is stored into memory, as these elements are the roots of the polynomial and hence, the inverse error locations.



Figure 7.a Chien search cell



Figure 7.b Chien search structure for t = 8.

There are (t+1) stages of the CS that are implemented in hardware. Each of these stages (where a stage consists of a multiplier, mux and register) (figure 7.a) represents a different value for *j* in the above CS equation. The search is run for n clock cycles (each clock cycle represents a different value of i in the above equation) and the output of the adder is examined to see if it is equal to zero. If it is equal to zero, the Zero Detect block will output a 1, otherwise, it will output a zero. The output of the Chien Search block is thus a string of nbits that have values of either 0 or 1. Each 1 represents the location of a symbol in error. For the first clock cycle, the mux will route the error locator polynomial coefficient into the register. For the remaining (n - 1) clock cycles, the output of the multiplier will be routed via the mux into the register.

#### **3.4Forney Algorithm**

The Forney algorithm is used to compute the error values  $Y_i$ . To compute these values, the Forney algorithm needs the error locator polynomial  $\sigma(x)$  and error magnitude polynomial  $\Omega(x)$ . The equation for the error values is given by Eq 14 :

$$Y_{i}=e_{i}=\frac{\Omega(X_{i}^{-1})}{\sigma'(X_{i}^{-1})} \text{ for } i=1...t,$$
(14)

where  $X_i^{-1}$  indicates roots indicates the root as computed from the Chien Search, and  $\sigma'(x)$ the derivative of the error locator polynomial. Because of the fact that any element will be zero while multiplying an even constant value, and will be its original value while multiplying an odd constant, the first derivative of can be represented by :

$$\sigma'(X_i^{-1}) = \frac{1}{X_i^{-1}} \sigma odd(X_i^{-1})$$
(15)

Then we can rewrite Eq 14 as the following format:

$$Y_{i}=e_{i}=\frac{\Omega(X_{i}^{-1})X_{i}^{-1}}{\sigma \text{odd}(X_{i}^{-1})}$$
(16)

The  $x\Omega(x)$  polynomial is then evaluated along using the same type of hardware as used for the CS. However, in order to form  $x\Omega(x)$ , the coefficients of  $\Omega(x)$  are shifted to the left by one location.



Figure 8  $\Omega(\alpha^i)$  calculator block for t = 8.

The numerator is then multiplied by the denominator using an inverse multiply. The inverse multiply contains a lookup table that finds the inverse of the denominator. For example, if the denominator was  $\alpha^3$ , the inverse is  $\alpha^{-3}$ . This can then be expressed as:  $\alpha^{-i} = \alpha^{(-i \mod n)} = \alpha^{(-3 \mod 255)} = \alpha^{252}$ .

Since the same type of hardware is needed for both the Chien Search and the Forney algorithm. The output of the adder for the odd stages is also used in the Forney algorithm, shown in the middle part of the figure 9. The sum of the odd stages represents the denominator of the Forney equation. This value is inversed in the Inverse Multiply block and then multiplied by the numerator value that is formed from evaluating the error magnitude polynomial. The output is "ANDed" with the zero detect output since the error values are only valid for the actual error locations (and they should be set to zero otherwise).

Once the error magnitudes are calculated, the error corrector block takes the received code and performs XOR-operation with the corresponding error magnitudes computed at the respective error locations to attain the original message stream (Eq. 17).

$$C(X_i) = R(X_i) \oplus Y_i \tag{17}$$



Figure 9 Error value evaluator structure for t = 8.

# 4 RS parameterization approach for new generation system

Past research has proposed several efficient RS algorithms and sub architectures. On the other hand there are others research works, which are interested on compiler development [34, 35]. However in the literature there are a few researches that are focused on implementing reconfigurable RS coderdecoder. K.SHIMIZU & N. TOGAWA have proposed a reconfigurable adaptive FEC System based on RS code with interleaving. In adaptive Scheme error correction capability t is changed dynamically according to the communication channel conditions. The packet error rate is employed as threshold value to change t [36].

In this section we define an advanced RS coder-decoder architecture based on parameterization approach which a key solution for software defined radio (SDR) systems. Our parameterization approach is used in order to implement on FPGA a generic RS coder-decoder for DVB and wireless systems.

Generic RS module must integrate all common RS configuration, which are used in most mobile and wireless systems. Implementing a generic RS module, match up parameterisation by common functions approach. Different parameters can have generic value in configurable RS module. Fully parameterized RS function, including:

- Number of bits per symbol
- Number of symbols per codeword
- Number of check symbols per codeword

- Field polynomial
- First root of generator polynomial

The symbol width (m) defines the field generator polynomial. Table 1 illustrates this correspondence.

Symbol Width	Field generator polynomial
3	$x^3 + x + 1$
4	$x^4 + x + 1$
5	$x^5 + x^2 + 1$
6	$x^{6}+x+1$
7	$x^7 + x^3 + 1$
8	$x^8 + x^4 + x^3 + x^2 + 1$
9	$x^9 + x^4 + 1$
10	$x^{10} + x^3 + 1$
11	$x^{11} + x^2 + 1$
12	$x^{12} + x^6 + x^4 + x + 1$

Table 1: Correspondence between symbol width and the field generator polynomial

All most new generation standards use eight value as symbol width this leads to use  $x^8+x^4+x^3+x^2+1$  as a field generator polynomial.

# 4.1 RS parameterization for DVB norm

DVB has three standards that use identical RS code parameters. These are satellite (DVB-S), cable (DVB-C) and terrestrial (DVB-T). The most widely used of the three protocols is DVB-S [Sohi20001.

All DVB standards employ the same (204,188) RS code. All DVB standards operate in  $GF(2^8)$ , and are based on a (255,239) RS code. Therefore, the same Galois Field arithmetic units and hardware can be used for different DVB standards. Table 2 summarize RS parameters for DVB.

Parameter	Symbol	DVB
Field Polynomial	P(x)	$X^{8}+X^{4}+X^{3}+X^{2}+1$
Generator polynomial	G(x)	$(x-\alpha^{0})(x-\alpha^{1})(x-\alpha^{2})(x-\alpha^{15})$
Bits number/Symbol	m	8
Code length	n	204
Message length	k	188
Parity Symbols	2t	16

Table 2: RS parameters for DVB

# 4.2 RS parameterization for Wireless 802.16

IEEE Std. 802.16 specifies the outer code requirements for RS code as follows:

The specified code generator polynomials are given by:

- Code Generator Polynomial:  $g(x) = (x+\mu^{1})(x+\mu^{2}) \dots (x+\mu^{2T})$ , where  $\mu=02$ hex - Field Generator Polynomial:  $p(x) = x^{8} + x^{4} + x^{3} + x^{2} + 1$ 

The specified code has a block length of 255 bytes and shall be configured as an RS(255,255-R) code with information bytes preceded by (255-*K*) zero symbols, where *K* is the codeword length and *R* the number of redundancy bytes (R = 2\*T ranges from 2 to 32, inclusive). The value of *K* and *T* are specified for each burst profile by the MAC. [37]

The variable decoder supports real-time changing of the number of symbols in the codeword, and R, the number of check symbols in a codeword.

# 5 FPGA implementation of a configurable FEC systems based on RS codes for DVB and 802.16 network

Overall hardware implementation of the controller design consists of the entry of the conceptual design into electronic description format (design entry), conversion of the design into a logic level form (synthesis), and translation of the design into the physical FPGA specific component placement and signal routing (implementation). The design verification process consists of testing the design for conformity at several intermediate stages. The verification steps performed after each major stage of the design are shown in figure 10 and include: behavioral or functional simulations, synthesis checks, postsynthesis timing verification, and post-implementation timing verification. All of these steps are done using simulation tools like Xilinx's Foundation ISE Tools [38] and Modelsim XE 6.0d.



Figure 7: Hardware Verification steps after each design stage [39]

The scope of our design methodology extends from specification to implementation. The discussion of the application system and parameterization approach described in the previous section determines the functions entities.

# 5.1 Code Generator Polynomial for wireless 802.16

Table 3 recapulates different code generator polynomials for wireless 802.16 according to the T value.

## **5.2 Encoder implementation**

To implement an adaptive FEC by switching between fixed RS coding levels. The CODEC include a switching entity that control the following RS coding levels. The first level is for DVB norm and the other RS coding levels are 802.16 norm.

- RS(204,188)
- RS(255,253), RS(255,251), RS (255,249),
- RS(255,247), RS(255,245), RS (255,243),
- RS(255,241), RS(255,239), RS (255,237),
- RS(255,235), RS(255,233), RS(255,231),
- RS (255,229), RS(255,227), RS(255,225),
- and RS(255,223)

The encoder and decoder units operate independently and each can be programmed on the fly to select the desired coding level. The decoder can operate independently to process blocks of up to 255 eight-bit symbols to provide corrections (t) of up to 16 errors per code block. The encoder output code block will contain the unaltered original data symbols followed by the generated parity symbols.

2t	Code Generator Polynomial
2	$G(x)=x^2+06x+08$
4	$G(x)=x^4+1Ex^3+D8x^2+E7x+74$
6	$G(x) = x^{6} + 7Ex^{5} + 04x^{4} + 9Ex^{3} + 3Ax^{2} + 31x$
	+75
8	$G(x) = x^8 + E3x^7 + 2Cx^6 + B2x^5 + 47x^4 + ACx^3 + Cx^6 + B2x^5 + 47x^4 + ACx^3 + Cx^6 + B2x^6 + B$
U	$08x^2 + F0x + 25x^2 + 26x^2 + 32x^2 + 17x^2 + 176x^2 + 176x^2$
10	$G(x) = x^{10} + ADx^9 + 2Ex^8 + 8Cx^7 + BEx^6 + C5x^5 + C5x^$
10	$1Ex^{4}+BCx^{3}+44x^{2}+D4x+A0$
12	$G(x) = x^{12} + 88x^{11} + C1x^{10} + 22x^9 + 33x^8 + 83x^7 + 93$
	$x^{6}+A7x^{5}+AAx^{4}+84x^{3}+AFx^{2}+FCx+78$
14	$G(x)=x^{14}+1Cx^{13}+D8x^{12}+B7x^{11}+14x^{10}+$
	$64x^9 + 2Ex^8 + 24x^7 + 4Dx^6 + 24x^5 + AFx^4 + 2Bx^3 + 22x^4 + 22x^$
	$BCx^2+9Cx+1A$
16	$G(x)=x^{16}+76x^{15}+34x^{14}+67x^{13}+1Fx^{12}+68x^{11}+$
	$7Ex^{10}+BBx^9+E8x^8+11x^7+38x^6+B7x^5+$
	$31x^4 + 64x^3 + 51x^2 + 2Cx + 4F$
18	$G(x)=x^{18}+C3x^{17}+CBx^{16}+D1x^{15}+43x^{14}+$
10	$57x^{13}+88x^{12}+33x^{11}+ABx^{10}+FEx^{9}+8Dx^{8}+63x$
	$^{7}$ +E6x <sup>6</sup> +74x <sup>5</sup> +19x <sup>4</sup> +B4x <sup>3</sup> +3Ex <sup>2</sup> +1Ex+B3
20	$\frac{G(\mathbf{x}) - \mathbf{x}^{20} + 2D\mathbf{x}^{19} + DF\mathbf{x}^{18} + D3\mathbf{x}^{17} + 50\mathbf{x}^{16} + DF\mathbf{x}^{18} + DF$
20	$61x^{15} + F5x^{14} + 27x^{13} + 64x^{12} + B2x^{11} + 4Fx^{10} +$
	$F7x^9+88x^8+D9x^7+47x^6+B3x^5+96x^4+74x^3+$
	$F4x^2 + A6x + 59$
22	$G(x) - x^{22} + B^2 x^{21} + E^2 6 x^{20} + 6 C x^{19} + C E x^{18} + 4^3 x^{17}$
	$+CBx^{16}+75x^{15}+FDx^{14}+F4x^{13}+\Delta 1x^{12}+$
	$B2x^{11}+B1x^{10}+75x^9+6Ex^8+1Ex^7+D9x^6+$
	$CBx^{5}+49x^{4}+4Bx^{3}+33x^{2}+6Fx+47$
24	$G(\mathbf{x}) - \mathbf{x}^{24} + FA\mathbf{x}^{23} + G5\mathbf{x}^{22} + 21\mathbf{x}^{21} + 14\mathbf{x}^{20}$
24	$O(x) = x + 1.4x + C_{3x} + 2.1x + 1.4x +$
	$96x^{13} + C6x^{12} + A7x^{11} + 2Cx^{10} + 7Dx^9 + EBx^8 + 85$
	$y^{7} + 2Dy^{6} + 4Ey^{5} + 4Dy^{4} + D0y^{3} + C7y^{2} + 6Cy + C1$
26	$C(\mathbf{x}) = \mathbf{x}^{26} + \mathbf{E1}\mathbf{x}^{25} + CC\mathbf{x}^{24} + D1\mathbf{x}^{23} + 40\mathbf{x}^{22} + CC\mathbf{x}^{24}$
20	$O(x) = x + 1^{1}x + CCx + D1x + 40x + D0y^{21} + 5y^{20} + 23y^{19} + 03y^{18} + 30y^{17} + B2y^{16}$
	$ECx^{15} + 6Ax^{14} + ABx^{13} + C2x^{12} + E3x^{11} + AAx^{10} + E2x^{11} + E3x^{11} $
	$ECx + 0Ax + ADx + C2x + E3x + 4Ax + 80x^{9} + E6x^{8} + 0Dx^{7} + ECx^{6} + 2Ex^{5} + 26x^{4} + 100x^{10} + 100x$
	$E_{2x^{3}} + E_{2x^{2}} + 7D_{x} + D_{0}$
28	$C(\mathbf{x}) = \mathbf{x}^{28} + \mathbf{E5x}^{27} + 24\mathbf{x}^{26} + \mathbf{E0x}^{25} + \mathbf{D0x}^{24} + \mathbf{E0x}^{26}$
20	$O(x) = x + E_{3x} + 24x + E_{0x} + D_{0x} + 7x^{23} + 2Cx^{22} + 7Cx^{21} + 5x^{20} + 93x^{19} + 1Cx^{18} + 7x^{10} + 10x^{10} + 1$
	$7Ax + 2Cx + 7Cx + A3x + 93x + 1Cx + 53x^{17} + 73x^{16} + 2Bx^{15} + D4x^{14} + 83x^{13} + 9Bx^{12} + 53x^{16} + 2Bx^{16} + 2Bx^{1$
	$94x^{11} + 6Fx^{10} + 3\Delta x^9 + 68x^8 + \Delta 1x^7 + 9Bx^6 + FBx^5$
	$+54x^4+CDx^3+\Delta 1x^2+25x+\Delta \Delta$
30	$G(\mathbf{x}) = \mathbf{x}^{30} + \mathbf{B5x}^{29} + \mathbf{E5x}^{28} + 52\mathbf{x}^{27} + \mathbf{E4x}^{26} + \mathbf{E5x}^{28} + \mathbf{E5x}^{28} + \mathbf{E5x}^{29} + \mathbf{E5x}$
50	$(x) = x + D_3 x + H_1 x + 32x + L_4 x + 45x^{25} + 45x^{24} + 65x^{23} + 45x^{24} + 52x^{24} + 65x^{24} + 65$
	$45x + 4Ax + 0Ex + AEx + D2x + 09x + 76x^{19} + 43x^{18} + ADx^{17} + 67x^{16} + 88x^{15} + 15x^{14}$
	$D_{2}\mathbf{y}^{13} + A_{1}\mathbf{y}^{12} + E_{2}\mathbf{y}^{11} + E_{2}\mathbf{y}^{10} + E_{2}\mathbf{y}^{9} + A_{2}\mathbf{y}^{8}$
	$D_{2x} + 41x + E_{2x} + 12x + E_{2x} + 45x + 50$
37	$G(\mathbf{x}) = \mathbf{x}^{32} + \mathbf{F8x}^{31} + 1\mathbf{Dx}^{30} + \mathbf{BD} = \mathbf{x}^{29} + 32\mathbf{x}^{28} + \mathbf{8F}$
54	$y^{27}_{\pm} = F6y^{26}_{\pm}F8y^{25}_{\pm}OF = y^{24}_{\pm}OP = y^{23}_{\pm}52y^{22}_{\pm}$
	$A4x^{21}+FFx^{20}+01x^{19}+9Fx^{18}+0Dx^{17}+77x^{16}+$
	$9Fy^{15}+F0y^{14}+86y^{13}+F3y^{12}+D2y^{11}+A3y^{10}+$
	$32x^9 \pm 68x^8 \pm 28x^7 \pm 18x^6 \pm 68x^5 \pm 68x^4 \pm 18x^3 \pm 18x^6 \pm 68x^5 \pm 68x^$
	52x + 00x + 20x + 10x
	LIX + D0X + 2D

Table 3 Code generator polynomials for wireless 802.16 according to the T value.

A representative symbol, with the signal names, is shown in figure 8 and described in table 4.



Figure 8 :Core schematic symbol

Signal	Direction	Description
D_in	Input	Input Data
Rst	Input	Active High: Initialize
Clk	Input	Clock-Active on rising
		edge
Par	Input	Used to active parity
		symbols transmission.
Sel	Input	If sel is high then
		configuration process, else
		encoding process.
Config	Input	Used to select Code
		generator polynomials.
D_out	Output	Data output & parity
		symbols.

Table 4: Encoder signals description

Code generator polynomials for wireless 802.16 according to the T value given in table 3 all of them are predefined in the encoder. When config value varying from  $(80)_{16}$  to  $(8F)_{16}$ , we can select a predefined code genertor polynomial. When config value varying from  $(01)_{16}$  to  $(21)_{16}$ , we can loaded from D\_in a new code genertor polynomial. Configuration step is defined according to table 5 and its implementation verification is illustrated in figure 9a and figure 9b.

	Config	Description
	value(Hexa)	
Downloading	01	D_in to $g(0)$
a new code	02	D_in to $g(1)$
genertor		
polynomial		
	21	D_in to $g(32)$
Selectining a	80	G1(2T=2)
predefined	81	G2(2T=4)
code		
genertor		
polynomial	8F	G16(2T=32)

Table 5 Configuration value

Figure 10 represent implementation verification of RS encoding. In this case of verification we have select as code genertor polynomial

 $G4(x)=x^8+E3x^7+2Cx^6+B2x^5+47x^4+ACx^3+08x^2$ +E0x+25.

And data frame(hexa) is:

00 00......00 02 03 83 93 9F 9F

After encoding process we obtain parity values: E7 38 1D F8 41 64 CD 6A.

The synthesis report of the RS encoder when using "xc4vlx15-12-sf363" as a target Device is sumarized in table 6.

Device utilization summary:							
Number of Slices:	1426	out of 6144 23%					
Number of Slice	559 o	out of 12288 4%					
Flip Flops:							
Number of 4 input	2698	out of 12288					
LUTs:	21%						
Number of bonded	28 ou	it of 240 11%					
IOBs:							
Number of GCLKs:	1 out	of 32 3%					
Timing Summary:							
Speed Grade:		-12					
Minimum period:		3.676ns					
Maximum Frequency	y:	(272.045MHz)					
Minimum input a	rrival	7.031ns					
time before clock:							
Maximum output rec	quired	3.921ns					
time after clock:							

Table 6: synthesis report of the RS encoder

#### **5.2 Decoder implementation**

The decoder input contains the received data and parity symbols including errors that

may be introduced during transmission. Decoder output will be a completely corrected block or will be marked as non-correctable and the block will be output as received without any changes.

A representative symbol, with the signal names, is shown in figure 11 and described in table 7.



Figure 11 : RS decoder schematic symbol

Signal	Direction	Description							
Х	Input	Input Data							
clrn	Input	Active High: Initialize							
Clk	Input	Clock-Active on rising							
		edge							
enable	Input	Used to validate input							
		data.							
Config	Input	Used to select Code							
		generator polynomials.							
Valid	Output	Set when error polynomial							
		is ready.							
With-	Output	Set when errors are							
error		occurred							
error	Output	Error value							

Table 7: Decoder signals description

In order to verify the decoder functionality wee have defined two scenarios: the message is received without error and the message is received with error. For simulation presented in this paper we have considered as code generator polynomial:

 $G4(x)=x^{8}+E3x^{7}+2Cx^{6}+B2x^{5}+47x^{4}+ACx^{3}+08x^{2}$ +E0x+25.

and as data frame(hexa) which is emitted by the encoder the following:

00 00......00 02 03 83 93 9F 9F **E7 38 1D F8 41 64 CD 6A** 

$$\underbrace{\begin{array}{c} 241 \\ k=247 \end{array}}_{n=255}$$

Simulation results which corresponds to the case in which the message is received without errors is illustrated in figure 11.

Simulation results which corresponds to the case in which the message is received with errors are illustrated in figure 12, 13, 14, 15. We suppose that the received message is:

V <u>0 00</u>	00/02 03 83 9	93 9F <u>00</u> E7 38	1D F8 41 64 CD	6A
24 <sup>4</sup> 1		)		
	k= 247			

n=255

The synthesis report of the RS decoder when using "xc4vlx15-12-sf363" as a target Device is summarized in table 8.

Number of Slices	6117	out	of	6144	99%			
register:								
Number of Slice	2170	out	of	12288	17%			
Flip Flops:								
Number of 4 input	11229	out	of	12288	91%			
LUTs:								
Number of bonded	29	out	of	240	12%			
IOBs:								
Number of GCLKs:	1	out	of	32	3%			
Timing Summary:								
Speed Grade:		-12						
Minimum period:		9.554ns						
Maximum Frequency:	:	(104.664MHz)						
Minimum input arriva	l time	12.729ns						
before clock:								
Maximum output requ	21.411ns							
time after clock:								

Table 8: synthesis report of the RS decoder

## 7 Conclusion

This work focuses on the problem of simultaneously designing and implementing Reconfigurable Reed Solomon codersdecoders for DVB and Wimax network. The proposed configurable architecture is modular and can be classified into two components: encoder and decoder. We propose an advanced RS encoder-decoder architecture based on parameterization approach which is a key solution for software defined radio (SDR) systems.

The implemented RS encoder-decoder was found to satisfy all timing constraints based on the detailed timing reports generated by the synthesis tool. Based on the simulation the design was found to conform to the design specifications and satisfy the timing criteria.

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由	00	00			ΈO	)(BC	A7	X24	ХВВ	X33	27	(75	χ08	(33	X7C	)(6E	XE8
中	00	00			(25	X44	<u>Ά</u> Α	X4D	XE8	ХАВ	<u>)</u> 64	) ED	χDΑ	<u>)</u> (03	JA5	) AE	)(OF
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	00	00	-			JAU	JAF	Yop	138	<u>18D</u>	JAE VEZ	<u>JA1</u>	JAE Voc	182	JIC VED	169	152
L (12)	00	00	-		-	6	170	YPC	107	103 YEC	YOD	YP1	136 100	YEA	103	1/6 YA2	YEE
品 (14)	00	00	-				Mr.O.	190	Y64	174	YD9	175	YA7	YAB	12B	YAD	101
<b>山</b> (15)	00	00	-					11A	¥51	119	147	YGE	12C	YC2	YD4	167	19E
聶	00	00					-		X2C	χB4	(B3	X1F	(7D	)(E3	(83	)(8B	(0D)
由	00	00							X4F	)(3E	X96	)(D9	χfb	(4A	)(9B	<u>)</u> (15	177
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中	00	00	-						1	<u>)</u> B3	XF4	<u>)</u> 49	X2D	) <u>E6</u>	)6F	<u>) 41</u>	<u>XEO</u>
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品 [24]	00	00									-		Yec	XE3	YEB	Y4B	132
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中	00	00											2.	)(D9	XA1	XBO	)(1B
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	00	00									-					YEQ	
(31) (32)	00	00			-		-								-	102	YD8
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Figure 9 a : Configuration step : selecting a predefined polynomials

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Figure 9b : Configuration step : Downloading a new polynomial

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Figure 10: implementation verification of RS (255, 247) encoding

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Figure 11 implementation verification of RS (255, 247) decoding (message is received without errors )

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↓ /sdec/s0       50       00       002       007       18D       194       143       143       175       1D2       1A4       1AD       106       158       11D       150         B→       /sdec/s1       DE       00       002       102       108       115       108       108       108       108       108       101       198       117       138       120       DE         B→       /sdec/s2       5E       00       102       102       118       148       1FD       198       157       132       120       DE         B→       /sdec/s2       5E       00       102       133       118       148       1FD       198       157       132       120       DE         B→       /sdec/s2       5E       00       102       133       118       148       1FD       198       158       150       128	♦ /rsdec/syn_shift	1																_	
E→       /tsdec/s0       50       00       102       107       180       194       144       149       175       102       144       140       106       168       110       150         E→       /tsdec/s1       DE       00       102       102       108       115       102       108       115       102       108       117       138       120       DE         E→       /tsdec/s2       5E       00       102       113       118       148       1FD       188       156       182       117       138       120       DE         E→       /tsdec/s2       5E       00       102       113       118       148       1FD       188       156       182       124       188       16D       128       188       55       55       122       144       188       16D       128       188       55       55       123       138       135       128       138       128       138       128       138       128       138       128       138       128       138       136       138       136       138       128       138       136       138       128       130	♦ /rsdec/berl_enable	1																A	
E→       /tsdec/s1       DE       00       )02       )08       )AF       )15       )CB       )08       )CB       )33       )17       )38       )20       DE         E→       /tsdec/s2       5E       00       )02       )13       )18       )48       )FD       )88       )56       )82       )E4       )38       )20       )2E       )38       5E         E→       /tsdec/s2       78       00       )02       )23       )29       )E8       )56       )82       )E4       )38       )20       )2E       )38       5E         E→       /tsdec/s2       78       00       )02       )23       )29       )E8       )34       )57       )34       )57       )34       )50       )22       )38       )56       )33       )21       )15       )40       )78         E→       /tsdec/s4       B1       00       )02       )43       )08       )24       )56       )33       )21       )15       )FE       )78       )81         IB→       /tsdec/s5       71       00       )02       )23       )C2       )23       )C2       )26       )70       )85       )89       )43	œ	50	00		)(	07	)(8D	94	ХАД	(49	<u>)</u> 75	XD2	XA4	(AD	(06	(68	(1D	150	),DE
Er       //sdec/s2       5E       00       )02       )13       )18       )48       )FD       )88       )56       )82       )E4       )80       )28       )88       5E         Er       //sdec/s3       78       00       )02       )23       )89       )EE       )89       )78       )34       )55       )82       )E4       )80       )28       )88       5E         Er       //sdec/s4       B1       00       )02       )43       )08       )EE       )13       )54       )56       )82       )E4       )80       )28       )88       )56       )78       )34       )55       )28       )08       )46       /78       )88       )56       )128       )38       )56       )28       )28       )38       )56       )78       )34       )55       )28	⊕	DE	00		χc	)2 <mark>)</mark> 0B	)AF	(15	CB	)(OB	)CB	(33	XD1	<u>Х</u> 9В	(17	(38	X2D	DE	X5E
Image: black state       78       00       102       123       189       178       134       15F       184       150       128       10C       178         Image: black state       13       130       132       133       15F       184       150       128       10C       178         Image: black state       13       130       122       143       108       12E       113       15A       168       189       1A3       121       115       1FE       178       181         Image: black state       71       00       102       143       102       128       102       121       113       15A       168       189       1A3       121       115       1FE       178       181         Image: black state       71       00       102       183       102       102       102       103       104       107       142       188       180       171	⊞	5E	00		X	)2 <mark>(</mark> 13	<u>(</u> 18	<b>(</b> 48	(FD	)(BB	)56	XB2	)E4	<u>X</u> 8B	)(6D	<b>)</b> 2B	(88	<mark>(</mark> 5E	(78
⊡→/sdec/s4         B1         00         )02         )43         )08         )EE         )13         )5A         )68         )83         )A3         )21         )15         )FE         )7B         ]B1           ⊡→/sdec/s5         71         00         )02         )83         )C4         )C6         )70         )B6         )BE         )A1         )D7         )A2         )38         )20         )71	⊞> /rsdec/s3	78	00	4	X	2 )23	89	)EB	(89	(78	34	)(5F	)84	(50	28	DE	JAC	78	)(B1
E → //sdec/45 71 00 )02 )83 )C4 )C8 )70 )86 )8E )A1 )07 )A2 )88 )80 71	⊞	B1	00		X	)2 )(43	)(OB	)EE	(13	)(5A	<u>)</u> 68	<u>(</u> 89	)A3	(21	(15	)(FE	)(7B	<mark>(</mark> B1	)71
	⊞	71	00		)(	)2 <mark>)</mark> 83	)C4		)(C8	(70	<b>)</b> B6	)(BE	)A1	D7	A2	)(8B	)(BO	<b>X</b> 71	(44
Er- √ //sdec/s5 44 00	⊞	44	00		XC	)2 <mark>(</mark> 1E	(38	C2	(16	)CF	)A0	)E6	(63	X2F	(5F	<b>)</b> D8	XC5	44	67
□ → //sdec/s7 67 00 )02 )39 )3C )45 )E5 )DB )D0 )C0 )28 )97 )F9 )EE )D9 67	œ /rsdec/s7	67	00		XC	)2 )39	<b>3</b> 0	45	)E5	)(DB	)D0	)(CO	)28	<u>(</u> 97	(F9	XEE	(D9	67	)(50

Figure 12 Syndrome computing value of c



Figure 13 Berlekamp module computing for RS (255, 247) (message is received with errors )

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→ /rsdec/s0	00	50 YDE Y00	
(T)	00	DE X3E X00	
- Vrsdec/s2	00	5E 1/78 1/00	
H /rsdec/s3	00	78 1/81 1/00	
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Figure 14 Chien module computing for RS (255, 247) (message is received with errors )



Figure 15: Errors polynomial computing

#### 9 Bibliography

[1] I. S. Reed and G. Solomon, "Polynomial codes over certain finite fields", *Journal of the Society for Industrial and Applied Mathematics*, 8:300-304, 1960

[2] T. R. N. Rao and E. Fujiwara, Error Control Coding for ComputerSystems, *Prentice-Hall, Englewood Cliffs, NJ, USA*, 1989.

[3] H.C.Chang, C.B.Shung, CY.Lee, "A Reed-Solomon product-code (RS-PC) decoder chip for DVD applications", *Solid-State Circuits, IEEE Journal*, Volume: 36 Issue: 2, Feb. 2001 Page(s): 229 –238

[4] Y.Cho, K.Kang, J.Lee and H.Shin "Proactive Reed-Solomon Bypasss (PRSB): A Technique for Real-Time Multimedia Processing in 3G Cellular Broadcast Networks", The 11th IEEE International Conference on Embedded and Real-Time computing system and application, 17-19 August 2005, Hong Kong

[5] J.SHIAN LI M.W. GUO, "Improving 802.11 Wireless TCP Performance with Adaptive Reed-Solomon Codes: An Experimental Study", JOURNAL OF INFORMATION SCIENCE AND ENGINEERING 21, 1201-1211 (2005)

[6]M.F.Arnal, "Optimisation de la fiabilité pour des communications multipoint par satellite géostationnaire, *Thèse*, *Ecole Nationale supèrieure des télecommunications de paris*, 15 dec 2004.

[7] DVB, "Framing structure, channel coding and modulation for digital terrestrial television," *ETSI EN 300* 744, vol. 4.1, January 2001

[8] Saswat Panigrahi and Tho Le-Ngoc "Fine-Granularity Loading Schemes Using Adaptive Reed-Solomon Coding for xDSL-DMT Systems" *EURASIP Journal on Applied Signal Processing*, volume 2006 (2006), Article ID 65716, 13 pages

[9]HomePlug Powerline Alliance, "Medium Interface Specification. Release 0.5," November 2000.

[10] DAVIC 1.4 Specification. Part 8, "Lower Layer Protocols and Physical Interface," 1998

[11] ATSC, "ATSC Digital Television Standard, *ATSC standard A/53B*," August 2001.

[12] M.Bednara, K.Danne, M.Deppe, O.Oberschelp, F.Slomka, J.Teich, "Design and Implementation of Digital Linear Control Systems on Reconfigurable Hardware", *EURASIP Journal on Applied Signal Processing 2003*:6, 594–602, © 2003 Hindawi Publishing Corporation

[13] W. Tuttlebee, "Software defined radio, baseband technology for 3Ghandsets and basestation,". *Edition JohnWiley & Sons, 2003*, 350 pages, ISBN 0-470-86770-1

[14] L.Chaari, M.Fourati, N.Masmoudi and L.Kamoun, "Re-configurability study for digital baseband processing unit for multimode handset architectures", 12th European Wireless Conference "Enabling Wireless *Technologies* for Multimedia Communications", April 2 - 5, 2006 - Athens, Greece

[15] G.V Meerbergen, M.Moonen, H.De Man, "TURBO-LIKE SOFT-DECISION DECODING OF REED-SOLOMON CODES »,in Proc. of the IEEE Global Telecommunications Conference (Globecom), Dallas, USA, Nov. 2004, pp. 199 – 203

[16] D. Augot, L.Pecquet, "An Alternative to Factorization: a Speedup for Sudan's Decoding Algorithm and its Generalization to Algebraic-Geometric Codes", *Projet CODES*, Rapport de recherche n\_3532 \_ Octobre 1998 \_ 15 pages, ISSN 0249-6399

[17] W.J. GROSS, F. R. KSCHISCHANG, R. KOETTER, P. GLENN GULAK," Towards a VLSI Architecture for Interpolation-Based Soft-Decision Reed-Solomon Decoders", *Journal of VLSI Signal Processing* 39, 93–111, ©2005 Springer Science + Business Media,

[18] D.V.Sarwate, N Rshanbhag, " High6Speed Architectures for reed-Solomon Decoders", *IEEE trans, VLSI System*, revised june 7, 2000

[19] A. Flocke, H. Blume, and T. G. Noll, "Implementation and modeling of parametrizable high-speed Reed Solomon decoders on FPGAs", Advances in Radio Science, 3, 271–276, 2005, *SRef-ID*: 1684-9973/ars/2005-3-271, © Copernicus GmbH 2005

[20] Jung H. Lee Jaesung Lee, Myung H. Sunwoo, "Design of Application-Specific Instructions and Hardware Accelerator for Reed-Solomon Codecs", *EURASIP Journal on Applied Signal Processing* 2003:13, 1346– 1354 Processing 2003:13, 1346–135 © 2003 Hindawi Publishing Corporation

[21] A. A. Pantchichkine, « Cours Mathématiques des codes correcteurs d'erreurs », *Master-2 de mathématiques*  (M2P), "Cryptologie, Sécurité et Codage d'Information", 2004/2005, Module 506a

[22] M. A. Ingale, "Error Correcting Codes in Optical Communication Systems", A Master Thesis, School of Electrical Engineering Department of Signals and Systems, Chalmers University of Technology, January 2003

[23] B.Sklar "Digital communication-Fundamentals *and Applications*", Pearson Education Asia, 2001

[24] H.C.Chang, C.B.Shung, and C.Y.Lee, "A Reed–Solomon Product-Code (RS-PC) Decoder Chip for DVD Applications", *IEEE JOURNAL OF SOLID-STATE CIRCUI*TS, VOL. 36, NO. 2, FEBRUARY 2001 229.

[25] E.R.Berklamp," Algebric coding theory, McGraw-Hill, New york, 1968: revised edition *Aegean Park Press*, Laguna Lills, CA, 1984.

[26]R.E.Blahut, "Theory and practice off error control codes", *Addison-Weseley*, 1983.

[27] J. Massey, "Shift-register synthesis and BCH decoding," *IEEE Trans. Inform. Theory*, vol. IT-15, pp. 122–127, Jan. 1969.

[28] N.Ben Atti, G.M.Diaz–Toca,Hlombardi, "The Berlekamp-Massey Algorithm revisited", *Volume 17*, *Issue 1 (April 2006)*, Pages: 75 – 82, Year of Publication: 2006, ISSN:0938-1279

[29]S.Dietler, « Implémentation de codes de Reed-Solomon sur FPGA pour communications spatiales », *Diploma Project*,, 24 janury 2006

[30] Y. Sugiyama, M. Kasahara, S. Hirasawa, and T. Namekawa, "A method for solving key equation for decoding Goppa codes," *Information and Control*, vol. 27, pp. 87–99, Jan. 1975.

[31] I. Reed, M. Shih, and T. Truong, "VLSI design of inverse-free Berlekamp–Massey algorithm," *Proc. IEE*, pt. E, vol. 138, pp. 295–298, Sept. 1991.

[32] Charles LEE , L.H , Error-Control Block Codes, Artech House Publishers, 2000

[33] S. B. Wicker, Error control Systems for Digital Communication and Storage, *Prentice Hall*, 1995.

[34] J.k.Park and J.T.Kim," Soft IP Compiler for a reed-Solomon Decoder", *ETRI Journal*, Volume 25, Number 5, October 2003.

[35] Reed-Solomon Compiler from Altera Corporation New in Version 4.1.0, Avril 2006.

[36]K.Shimizu, N.Togawa, I.Kenaga and S.Goto, "A reconfigurable adaptive FEC System based on Reed-Solomon code with interleaving", *IEICE Trans.INF SYST*, Vol E88-D N).7, july 2005

[37] Altera Corporation, "Implementing an IEEE Std. 802.16-Compliant FEC Decoder", *M-WP-IEEE802.16-1.0*, December 2001, ver. 1.0

[38] Xilinx Inc., *Xilinx Foundation* ISE version 8.12i, http://www.xilinx.com

[39] V.Subramanian, "Configurable Architecture for System-Level Prototyping of High-Speed Embedded Wireless Communication Systems », *Master Thesis*, *faculty of the Virginia Polytechnic Institute and State University*, January 13, 2003.