Algebra-Logical Diagnosis Model for SoC F-IP

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ABSTRACT: – Algebra-logical model, method and algorithm of fault embedded diagnosis in functional blocks of SoC are proposed. The reduced SoC Functional Intellectual Property Infrastructure that is characterized by minimal set of the embedded diagnosis processes in real time and enables to realize the services: testing of the nominal functions on basis of generable input patterns and analysis of output reactions; fault diagnosis with given resolution of fault location by means of utilization of the IEEE 1500 multiprobe; fault simulation to provide of realization of the first two procedures on basis of the fault detection table is presented.

Key-Words: - Diagnosis, System-on-Chip, Electronic System Level, Transaction Level Modelling, Infrastructure Intellectual Property, Functional Intellectual Property, Testbench, Fault

1 I-IP Infrastructure
Computational and hardware complexity of modern digital systems on a chip (SoC) is characterized by millions of equivalent gates and requires making and implementation of new high-level design technologies: Electronic System Level (ESL) Design, Transaction Level Modelling (TLM) and embedded service – Infrastructure Intellectual Property (I-IP). It means that search for high-performance methods and facilities [1-12, 15-17] reduces all researchers to necessity to rise of an abstraction level of Functional Intellectual Property (F-IP) models, which are created and embedded into a chip. EDA market suggests facilities for computer-aided modelling and verification of system level devices, beginning with HDL- compilers (C++, SystemC, SystemVerilog, UML, SDL) [7] up to graphics environments (Simulink, LabView, Xilinx EDK). These facilities enable to create projects using existing library components by means of ESL-mapping and creation of TLM-interfaces [8, 9]. Market appeal of the implementation of a digital system to FPGA is determined by following services into a chip [8]:
1) Observation for state of input and output lines in functioning, verification and testing of standard blocks on basis of utilization of the boundary scan standard IEEE 1500 [10, 12];
2) Testing of functional modules by means of input of the fault detection patterns from different test generators, which are oriented on complex solving of the project quality problem and yield increasing in manufacturing that is determined by implementation of the following services into a chip [8]:
3) Fault diagnosis by means of analysis of information obtained on the testing stage and utilization of special methods of embedded fault lookup on basis of the standard IEEE 1500 [10, 12];
4) Repair of functional modules and memory after fixation of negative testing result, fault location and its type on diagnosis stage;
5) Measurement of the general characteristics and parameters of a device operation on basis of on-chip facilities, which enable to make time and volt-ampere measurements;

The research aim is development of algebra-logical method of SoC Functional Intellectual Property Infrastructure that is intended for the diagnosis of SoC components in real time.
6) Reliability and fault tolerance of a device operation in working that is obtained by diversification of functional blocks, redundancy of them and repair of SoC in real time.

In Fig. 1 it is represented the reduced structure [8], oriented on solving of the following problem: 1) testing of the functionalities on basis of generable input patterns (Automated Test Pattern Generator) and analysis of output reactions; 2) Fault simulation [5] to ensure the diagnosis and repair on basis of the fault detection table; 3) Fault diagnosis with given resolution of fault location by means of utilization of the IEEE 1500 multiprobe.

![Infrastructure Intellectual Property of SoC](image)

**Fig. 1. Infrastructure Intellectual Property of SoC**

1. Automated Test Pattern Generator for verification of functionalities and single faults consists of a set of input patterns generators, which provide creation of the following tests [1,2]: PRTG is pseudo-random generator of input stimuli with uniform distribution law of zero and unit signals at input variables; SATG is test generator of hexadecimal codes on basis of the signature analysis; SPTG is algorithmic generator of the test patterns, which activate one-dimensional logical paths, oriented on verification of given single faults; ADTG is test generator that is designed for verification of the summatory ALU circuits; BSTG is test generator for the bus organized structure of data transceiving; METG is test generator, oriented on the matrix memory verification; DFTG is test generator for automata, specified in the form of algorithm flow graphs; RCTG is test generator for sequential arithmetic-register structures and trigger circuits.

Generator module analyses the structural-functional model of a tested block and assigns a subset of such synthesizers, which provide given fault cover quality ($F^c$) and functional modes ($P^c$): $F^c(\bigwedge_{i=1}^{n} T_i) \geq F^c_{\min}$, $P^c(\bigcup_{i=1}^{n} T_i) \geq P^c_{\min}$, \( (1) \)

$T = \{Pr, T_2, Sp, T_3, T_4, T_5, T_6, T_7, Pr, Rc\}$. Generalized structure of Testbench synthesis [1] is represented in Fig. 2 and includes HDL-code generator that is designed for functional testing and verification on the stage of project development. A number of test generators on the SoC development stage can be considerably greater than a subset of ones that embedded into a chip later. So, on the simulation and verification stage the analysis of covering features of every test generator is performed to search for the minimal aggregate configuration of them that is satisfied expression (1). It is important to say that within the next 5 years the test synthesis ideology for SoC will borrow the best traditions of ESL-, TLM-design [7,11].

**Fig. 2. Structure of the Testbench synthesis process for F-IP**

It means: 1) Use of the Testbench libraries of the lead companies in the world for testing and verification of standardize functionalities, which are designated as F-IP. 2) Application of I-IP standard solution for on-chip testing of SoC components. 3) Creation of own test libraries for new-developing functionalities. 4) Adoption of new technology of the test synthesis for a digital system, based on the discrete mapping [11] (Fig. 3) of covering of functionalities and faults of the initial specification by means of minimal Testbench set from a test library. 5) Application of the on-chip testability facilities, such as IEEE boundary scan and six I-IP components, to increase of the technological effectiveness of test synthesis procedures.

**Fig. 3. Mapping of the test synthesis model for F-IP**

2. Fault analysis module. It uses the deductive algorithm that is oriented on verification of single faults, which are generated on basis of analytical or tabular definitions of SoC functionalities. It means that deductive simulation can be applied for projects, represented on gate abstraction level or on some higher one (register or system). The main idea of the
method is making of deductive functionality model on basis of the known expression using [5]:

\[ F = f(X_1 \oplus T_1),(X_2 \oplus T_2),...,(X_n \oplus T_n) \oplus T_i \]  

where deductive function \( F \) on test-vector \( T \) is the modified definition of fault-free behaviour that enables to determine an input fault lists, which are transported on a circuit output under the influence of input signals. On the example of Xor function the synthesis of a deductive function according to the Karnaugh map is demonstrated:

\[ F = (xy) \land (ab) \]

The variables \( x, y \) are Boolean, the signals \( a, b \) are register and they are used for storage of fault lists:

\[ L = f(x, y, a, b) = ab \lor a \overline{b} \]  

Hardware realization of the deductive function, defined by formula (4), is represented in Fig. 4.

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Fig. 4. Deductive primitive of the Xor function
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The circuit primitive is universal with respect to various test patterns. The model synthesis strategy, proposed in the paper, is based on creation of a deductive element library that covers all standardize functional elements, which are used by a designer in the process of computer-aided project creation in a SoC form. In this case the matter is synthesis of a deductive structure on basis of mapping [11], the kernel of that is represented in Fig. 5.

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Fig. 5. Mapping - deductive model of F-IP
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The proposed approach to the deductive analysis provides creation one more embedded model on a chip, which must ensure practically all six services, specified by the I-IP infrastructure standard [8]. “Pay” for quality of diagnostic and test assistance is sufficiently large cost of additional hardware costs, which greater than nominal functionality in 10-15 times. At that gain in the performance in comparison with the external software realization of the deductive analysis is 2-3 orders that practically provides the service in real time. Other more economical solution of the problem is the interactive modification of the deductive model circuit structure for every test-vector. For that the internal memory of a chip is used, where the model is formed in compliance with the rules, defined in (2). Mapping (Fig. 5) gives a deductive function, where the hardware costs is equal to the cost of F-IP functionality.

### 2 Algebra-Logical Method of the Fault Diagnosis

The general role is assigned to the boundary scan technology [10,12] that is implemented into a chip now has to simplify solution of practically all problems of SoC Functional Intellectual Property Infrastructure. The access controller to internal lines and ports of the boundary scan register uses a cell or a stage of the register. In the aggregate a number of such cells, which provide monitoring in this case, must be equal to the quantity of problem observable lines of a project, which are necessary for exact establishment of a diagnosis. Diagnosis procedure, based on the boundary scan register uses information from the fault detection table that is a fault set, which are covered by test patterns. Using result information of a diagnostic experiment that is represented in an experimental validation vector form \( V = (V_1, V_2,..., V_n) \), as well as the fault detection table \( F \) [5], the diagnosis procedure is carried out in compliance with the expression, written in the product of disjunctions form for all faults [6], which can give an experimental reaction in the form of \( V \) that determined by unit and zero values:

\[ F = \bigwedge_{i=1}^{i=n} \bigvee_{j=1}^{j=m} F_j. \]  

\[ \forall V_i = 1 \land \forall M_{ij} = 1 \]  

The conjunctive normal form, derived from the fault detection table, is transformed to the disjunctive normal form by means of equivalent transformations (conjunction, minimization and absorption) [6]. Therefore we have the Boolean function, where terms are the logical product, which represent full solution set in the fault combination form (they give the experimental validation vector \( V \) at SoC outputs or its component):

\[ F = \bigwedge_{i=1}^{i=n} \bigvee_{j=1}^{j=m} F_j \]

\[ \forall V_i = 1 \land \forall M_{ij} = 1 \]

Represented procedure in general case diagnoses some fault subset that later needs a refinement by
application of additional flexing of internal points by means of the boundary scan register. An example of defect finding is considered on basis of the following fault detection table (columns are faults, rows are test patterns) that is product of the deductive fault analysis and the experimental validation vector [13,14]:

<table>
<thead>
<tr>
<th>T1</th>
<th>F1</th>
<th>F2</th>
<th>F3</th>
<th>F4</th>
<th>F5</th>
<th>F6</th>
<th>V</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>T2</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>T3</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>T4</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>T5</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

A number of units in the experimental validation vector V forms quantity of CNF disjunctive terms (6). Every term is line-by-line writing of faults (by logic operation OR), which influence on functional outputs. Table representation in the analytical form (conjunctive normal form) makes possible to reduce volume of diagnostic information for defect finding essentially. Subsequent transformation of CNF to DNF on basis of the Boolean algebra identities enables to reduce the Boolean function that is illustrated by the following result:

\[ F = (F_1 \vee F_4)(F_2 \vee F_3)(F_1 \vee F_5)(F_1 \vee F_6) = \]

\[ = (F_1 \vee F_4)(F_2 \vee F_3)(F_3 \vee F_4 \vee F_5)(F_1 \vee F_5) = \]

\[ = (F_1 \vee F_4)(F_2 \vee F_3)(F_3 \vee F_4 \vee F_5)(F_1 \vee F_4 \vee F_5 \vee F_6) = \]

\[ = (F_1 \vee F_4)(F_2 \vee F_3)(F_3 \vee F_4 \vee F_5)(F_1 \vee F_4 \vee F_5 \vee F_6)(F_1 \vee F_4 \vee F_5 \vee F_6) \]

(7)

The derived result

\[ F = F_1 F_5 \vee F_1 F_2 F_3 \vee F_2 F_3 F_4 \vee F_3 F_4 F_5 \vee F_1 F_2 F_4 \]

represents all possible solutions (fault covering of the fault detection table rows of SoC functionality on condition that the experimental validation vector has all unit coordinates V = (111111)). Taking into account the actual value of the experimental validation vector V = (110111), it is carried out the simulation of function F by substitution of zero fault values, which are verified theoretically, but they give zero coordinate in the vector V. Such fault are:

\[ \bar{F} = F_3 \vee F_4 \vee F_5 \]

Final result is determined by the next function:

\[ F = F_1 F_5 \vee F_1 F_2 F_3 \vee F_2 F_3 F_4 \vee F_3 F_4 F_5 \vee F_1 F_2 F_4 \]

\[ \vee F_1 F_2 F_4 | F_3 \vee F_4 \vee F_5 = 0 \]

Whatever combination is DNF conjunctive term, presented in solution

\[ F = F_1 F_5 \vee F_1 F_2 F_3 \vee F_2 F_3 F_4 \vee F_3 F_4 F_5 \vee F_1 F_2 F_4 \]

covers all rows of the fault detection table according with definition, so addition of any zero row transforms function F to zero without fail. So, correct solution that corresponds to the experimental validation vector must take into account zero coordinates of the vector V. Subject to the stated above it is necessary to eliminate the term \( F_3 \vee F_4 \vee F_5 \) from expression (7) on CNF forming stage

\[ F = (F_1 \vee F_4)(F_2 \vee F_3)(F_1 \vee F_5)(F_2 \vee F_5 \vee F_6) = \]

\[ = (F_1 \vee F_4)(F_2 \vee F_3)(F_3 \vee F_4 \vee F_5)(F_1 \vee F_5) = \]

(8)

The result represents all possible solutions, which make a device reaction, determined given experimental validation vector:

\[ F = F_1 F_2 \vee F_1 F_5 \vee F_2 F_3 F_4 \vee F_2 F_4 F_5 \]

Additional simulation of last Boolean function gives final solution in the form of two faults combination:

\[ F = F_1 F_2 \vee F_1 F_5 \vee F_2 F_3 F_4 \vee F_2 F_4 F_5 | F_3 \vee F_4 \vee F_5 = 0 \]

Algebra-logical method can be formally considered by an example of the following fault detection table \( M_1 \) and it can be represented by five algorithm items.

<table>
<thead>
<tr>
<th>T1</th>
<th>F1</th>
<th>F2</th>
<th>F3</th>
<th>F4</th>
<th>F5</th>
<th>F6</th>
<th>V</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>T2</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>T3</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>T4</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>T5</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

1. Detection of all rows, which correspond to zero values of the experimental validation vector for nulling of all 1-coordinates of found rows. In this case it is the row T5.

2. Detection of all columns, which have zero values of rows coordinates with zero state of the vector V. Nulling of unit values of found columns. In this case it is F2, F5, F6.
3. Removal the rows and the columns, which have only zero coordinate values (found in items 1 and 2), from the fault detection table.

\[
M_1 = \begin{vmatrix}
T_1 & F_1 & F_2 & F_3 & F_4 & F_5 & V \\
T_1 & 1 & 1 & 1 & 1 & 1 \\
T_2 & 0 & 0 & 1 & 0 & 1 \\
T_3 & 1 & 1 & 0 & 1 & 0 \\
T_4 & 1 & 1 & 1 & 1 & 0 \\
T_5 & 0 & 0 & 0 & 0 & 0
\end{vmatrix}
\]

4. Making CNF by unit values of the experimental validation vector:

\[
F = (F_1 \lor F_4) \land (F_3 \lor F_4) \land (F_1 \lor F_3) =
= (F_1 F_3 \lor F_3 F_4 \lor F_1 F_4 \lor F_4 F_4) \land (F_1 \lor F_3) =
= F_1 F_3 F_3 F_4 F_4 F_4 F_4 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \\
= F_1 F_3 \lor F_1 F_4 \lor F_1 F_3 F_4 \lor F_1 F_3 F_4 \lor F_3 F_4 \lor F_3 F_4 \lor F_3 F_4 \lor F_3 F_4 \lor F_3 F_4 \lor F_3 F_4
\]

5. Transformation CNF to DNF with subsequent minimization of the function. In this case it brings to gaining of sought-for result in the fault combination form:

\[
F = F_1 F_3 \lor F_1 F_4 \lor F_3 F_4.
\]

The proposed algorithm is oriented on preliminary analysis of the fault detection table to decrease its size and amount of subsequent computing related to DNF making that forms all solutions of SoC functionalities diagnosis. Further refinement of a diagnosis is possible by application of the multiprobe on basis of the boundary scan register [10].

3 Algebra-Logical Diagnosis Model

The structure of I-IP service modules for fault diagnosis in F-IP functional blocks is represented in Fig. 6. Comparator (⊕) analyses output reactions of a model and a real device on input test vectors, entering from a test generator. Discrepancy between model and experimental reactions on a test forms unit coordinates of the experimental validation vector \(V(T) = (V_1, V_2, ..., V_i, ..., V_n)\) for every input pattern. Communication between the vector V and the fault detection table (\(T = [T_{ij}], t = 1, p; r = 1, q + n\) of dimension \(p \times n\), \(p\) is a number of test-vectors, \(n\) is a number of stages of the boundary scan register) and circuit structure gives a set of lines and elements, which are suspected as faulty on a current test-vector. To organize of computational processes, which result in exact diagnosis, it is important metrics or initial information representation form.
In compliance with quantity of units in the experimental validation vector $V$ a number of disjunctive terms $CNF$ that is equal to 4 is formed. Every term is line-by-line writing of faults by logic operation OR which influence on distortion of functional output signals. Then $CNF$ is transformed to $DNF$ on basis of the Boolean algebra rules. It enables to get result:

$$F = (F_4 \lor F_{10}) \lor (F_5 \lor F_8) \lor (F_4) (F_5 \lor F_9) \lor (F_4 F_8) \lor (F_5 F_{10}) =$$

$$= (F_5 \lor F_8) (F_4) (F_5 \lor F_9) \lor (F_4 F_8) \lor (F_5 F_{10}) =$$

and

$$=(F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8).$$

The result

$$F = (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8) \quad (11)$$

contains the fault $F_4$ in all terms, it means that the fault is present in SoC functionality without fail. If to put forward hypothesis about existence of single fault or minimal quantity of multiple faults, the solution determinate by third term $F = F_4 F_8$ is preferable (in a circuit there exist two faults, which form the experimental validation vector that is equal to $V = (1001001001)$ on the outputs).

### 4 Sumulation for F-IP Diagnosis Refinement

Obtained disjunctive form (6) is basic model for defect finding. It does not always identify a functional fault definitely, so it needs in procedures, which improve a diagnosis. First of all it should be noted that all rows of the matrix $M = T \times F$, which were marked by zero values of the experimental validation vector, can be joined in a disjunction of faults (6), which can not be present in a circuit. The creation of form (5) from concerned fault detection table enables to determine all faults, which can not be present in a circuit.

Analysis of the expressions, represented by formulas (11) and (12) results in interesting conclusions: 1) Faults, which can not be present in a circuit, are determined in the $DNF$ terms, obtained by zero rows concerning the experimental validation vector; 2) Faults, which are in $DNF$ (14), must be removed from function (12); 3) In this case removal of the fault $F_5$ results in breakup of two terms $F_4 F_5 F_9 \lor F_4 F_8 F_{10}$, as far as without the fault $F_5$ every of them separately can not form given experimental validation vector; 4) So, it is make the sole conclusion – double fault that is determined by the term $F = (F_4 F_5)$ is present in a circuit; 5) Computational complexity of gaining of exact and full solution set is determined by expression

$$Q = 2^{m+1}(2m+1), \quad m \text{ is a number of faults.}$$

If to designate absence of the concrete fault $0 F_i = 0$, it can to form input conditions for $DNF$ (11) for subsequent simulation of the function on the following initial conditions:

$$F = (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8) \quad (12)$$

Then simulation result of the function $F = (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8)$ is equal to $F = (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8) = F_4 F_8$.

Really, if the faults $(F_4, F_5, F_6, F_7, F_8)$, which are verified on the test patterns theoretically, give the negative result (don’t distort the output states), it means they are absent in a circuit. Support of this fact is corroborated by the following proof.

**Lemma 1.** Full set of all possible fault combinations, which are verified by the test $T$, is determined as $DNF$, and obtained by transformation of a conjunctive form

$$F = \bigwedge_{V_i = 1}^{i = 1} \bigvee_{M_{ij} = 1}^{j = 1} F_j \bigg( \bigwedge_{V_i = 1}^{i = 1} \bigvee_{M_{ij} = 1}^{j = 1} F_j \bigg),$$

every term of that is written by unit values of the fault detection table row [18] $M = T \times F$ corresponding to the experimental validation vector state $V_i = 1$.

Initial information, formed in compliance with unit values of the experimental validation vector, is full model of faulty behavior of a real object, which forms the experimental validation vector with fixed quantity of units (fault detection table rows) that is
equal to k. Every row forms a fault disjunction, written by OR. A number of such disjunctions is equal to k, they are logical multiplied and form full and consistent set of events (faults), which are present in a circuit simultaneously. By multiplication of elementary disjunctions with subsequent simplification of the expressions and using the axioms \((\forall a \vee b = b; \forall a \vee a = a)\) DNF that includes all possible combinations, written in the elementary conjunctions form, is turned out. Considering identity of made transformations the obtained function is equivalent to the initial CNF at logic and it is technological notation of all solutions (fault combinations), which are in a circuit, essentially.

Lemma 2. All faults, verified in the fault detection table rows \(M = T \times F\) and marked by zero values of the experimental validation vector \(V_l = 0\) are absent in a real object.

Really, the fault detection table \(M = T \times F\) has unit and zero rows concerning the experimental validation vector value:

\[M_p(0110) \rightarrow V_p = 1; M_q(0101) \rightarrow V_q = 0.\]

The row \(p\) detects presence of two faults \(F_2 \vee F_3\) in a circuit. The row \(q\) evidences of theoretical verification of the faults \(F_2 \vee F_4\) if the vector is equal to \(1: V_q = 1\). But practically the signal \(V_q = 0\) shows nonessentiality of the faults \(F_2 \vee F_4\) for distortion of circuit outputs. Or these faults are absent in a tested device. Put zero signals for \(F_2 \vee F_4\) in the function

\[F = F_2 \vee F_3\]

and obtain the result:

\[F = F_2 \vee F_3 | F_2 = F_4 = 0 = F_3.\]

Analogous, all faults which are determined in the rows, corresponding to zero values of the experimental validation vector, are absent in a circuit. But if it is true they must be removed from DNF, written by unit values of the vector \(V\). So, there are DNF terms and a fault set, which can not exist in a circuit for given experimental validation vector and the procedure of substitution of zero signals in the variables of elementary conjunctions of DNF function can be carried out. But, in consideration of the fact \(0 \land a \land b \land c \ldots = 0\) the result of substitution and subsequent transformations to obtain minimal function will have only the terms, which don’t have variables (faults) with zero signal value. It means that the faults which concern to zero fault detection table rows (concerning the vector \(V\)), will be removed from DNF.

Theorem 1. Minimal set of all possible fault combinations, which are determined by the fault detection table \(M = T \times F\), is computed by DNF simulation on an initial conditions set

\[F = \bigvee_{i=1}^{2^m} \bigwedge_{j=1}^{m} k_j F_j ,\]

specified by zero values of all verified faults, which correspond to zero signals of the experimental validation vector.

In compliance with lemma 1 full set of all possible fault combinations, verified by a test, is determined in DNF form

\[F = \bigvee_{i=1}^{2^m} \bigwedge_{j=1}^{m} k_j F_j ,\]

that forms all solutions, which satisfy to unit values of the experimental validation vector \(V_q = 1\). It can be decreased by removal of the faults, which are verified by a test theoretically, but really they don’t distort the output states on the test patterns, that mean complete absence of them in a real circuit. So, they can be removed from DNF terms, which are a full set of all possible combinations. The removal mechanism, according to lemma 2, is substitution of zero variable values to DNF terms and subsequent simulation (simplification) of the function. If a term has zero-component one of the variables \(F_i\), according to the algebra of logic whole term is turned into 0, that means removal of it from DNF. So, after minimization subject to the condition of lemma 2 the minimal DNF is turned out that contains the minimal quantity of possible fault combinations (single and multiple ones) that can not be decreased without additional diagnostic information incoming from the multiprobe on basis of boundary scan register.

So, proposed algebra-logical diagnosis method uses Boolean calculus as the basic apparatus for solving of the covering task by getting of the disjunctive form that then is minimized by removal of the terms, which have fault variables, relating to the rows with zero values of the vector \(V\). For little quantity of faults in SoC the computational complexity enables to realize fault finding in real time.

5 Conditional Diagnosis of F-IP by DNF

To decrease of precautionary faults field essentially the half-division method is used [10], it is based on use of an interactive procedure of internal check point flexing that provides the obtained fault DNF by additional information to decrease a fault set. In this case as such tester the boundary scan register can be used that is able to determine an internal line state for fault removal or its confirmation. The
check point choice strategy is oriented on approximately half-division of precautionary set (removal of half faults by simulation on every step) and simplification of the initial DNF. The essence of the half-division method on disjunctive normal form that represents all possible fault combinations in a circuit can be demonstrated by the following example:

\[ F = (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8). \]

Choice of the first check point \( F_9 = 0 \) turns the Boolean function into reduced expression:

\[
\begin{align*}
F_9 = 0 & \rightarrow (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8) = F_2 F_3 F_{10} \lor F_4 F_8; \\
F_9 = 1 & \rightarrow (F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8) = F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8.
\end{align*}
\]

If \( F_9 = 1 \), it means confirmation of a line fault and decrease of DNF size do not happen. It is necessary to orient the check point choice algorithm on maximal decrease of the initial DNF after definition of the initial conditions \( F_j = \{0,1\} \) for simulation.

Weights of DNF powers, obtained in the process of simulation the both verification states, can be used as the check point choice criterion.

Check point choice rules are regulated by the following assertions.

Assertion 1. If \( F_j \) is present in all DNF terms, there exists given fault in a circuit without fail and it is not necessary to test it. Otherwise, if to suppose that verification result is zero, all terms is turned into zero and this fact contradicts to the existence condition of nonzero values of the experimental validation vector \( V \).

Assertion 2. There is a single fault combination in a circuit that is determined by a single DNF term. If it is found one confirmed solution in the DNF term it is necessary to choose the variables with minimal weight as check points, which will turn the terms into zero. So the first and second check points are \((F_3, F_6)\), they have minimal weight:

\[ F = (F_3 F_4 F_5 F_9 \lor F_2 F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_2 F_4 F_8 F_9 \lor F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_4 F_5 F_8 F_9 \lor F_4 F_5 F_8 F_9 \lor F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_4 F_5 F_8 F_9 \lor F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_4 F_5 F_{10}). \]

The verification \( F \) gives the following results of after probe simulation of two function variants:

\[ F = \begin{cases} 
F_5 = 0 \rightarrow F_4 F_8; \\
F_5 = 1 \rightarrow F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8.
\end{cases} \]

Then, after \((F_5 = 1)\), two verifications from three ones \((F_6, F_9, F_{10})\) should be carried out, they remove all terms except one that defines a solution:

\[ F = \begin{cases} 
F_9 = 0 \rightarrow F_4 F_5 F_9; \\
F_9 = 1 \rightarrow F_4 F_5 F_{10}.
\end{cases} \]

The finishing diagnosis procedure criterion is obtained of one DNF term that identifies the presence of a multiple fault in SoC functionality.

Below it is proposed one more example of carrying out the interactive diagnosis procedure on basis of DNF analysis:

There is a multiple fault \( F = F_1 F_2 F_8 F_{10} \) in a device.

1) Weight count of every variable that is a part of DNF is carried out:

\[
\begin{array}{cccccccc}
F_1 & F_2 & F_3 & F_4 & F_5 & F_6 & F_7 & F_8 & F_9 & F_{10} \\
W(F_1) & 2 & 2 & 1 & 4 & 2 & 1 & 3 & 3 & 2
\end{array}
\]

2) Fault presence probability in a circuit is correlated with their weighting coefficients. So, to get a single solution in the DNF term it is necessary to choose the variables with minimal weight as check points, which will turn the terms into zero. So the first and second check points are \((F_3, F_6)\), they have minimal weight:

\[ F = (F_3 F_4 F_5 F_9 \lor F_2 F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_2 F_4 F_8 F_9 \lor F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_4 F_5 F_8 F_9 \lor F_4 F_5 F_8 F_9 \lor F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_4 F_5 F_{10} \lor F_1 F_4 F_8 F_9 \lor F_4 F_5 F_{10}). \]

The verification \( F \) gives the following result of after probe simulation of two function variants:

\[ F = \begin{cases} 
F_5 = 0 \rightarrow F_4 F_8; \\
F_5 = 1 \rightarrow F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8.
\end{cases} \]

Then, after \((F_5 = 1)\), two verifications from three ones \((F_6, F_9, F_{10})\) should be carried out, they remove all terms except one that defines a solution:

\[ F = \begin{cases} 
F_9 = 0 \rightarrow F_4 F_5 F_9; \\
F_9 = 1 \rightarrow F_4 F_5 F_{10}.
\end{cases} \]

The verification \( F \) gives the following result of after probe simulation of two function variants:

\[ F = \begin{cases} 
F_5 = 0 \rightarrow F_4 F_8; \\
F_5 = 1 \rightarrow F_4 F_5 F_9 \lor F_4 F_5 F_{10} \lor F_4 F_8.
\end{cases} \]

Then, after \((F_5 = 1)\), two verifications from three ones \((F_6, F_9, F_{10})\) should be carried out, they remove all terms except one that defines a solution:

\[ F = \begin{cases} 
F_9 = 0 \rightarrow F_4 F_5 F_9; \\
F_9 = 1 \rightarrow F_4 F_5 F_{10}.
\end{cases} \]
F = (F_1 F_4 F_5 F_9 \lor F_2 F_4 F_5 F_6) \lor (F_1 F_4 F_6 F_{10}) \mid (F_2 = 0) = 
\quad = F_1 F_4 F_6 F_9 \lor F_1 F_4 F_8 F_{10}.

Coefficients re-calculation:

<table>
<thead>
<tr>
<th>F_1</th>
<th>F_2</th>
<th>F_3</th>
<th>F_4</th>
<th>F_5</th>
<th>F_6</th>
<th>F_7</th>
<th>F_8</th>
<th>F_9</th>
<th>F_{10}</th>
</tr>
</thead>
<tbody>
<tr>
<td>W(F_1)</td>
<td>2</td>
<td>-</td>
<td>-</td>
<td>2</td>
<td>-</td>
<td>-</td>
<td>2</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

makes provision for presence of the faults (F_1, F_4, F_5) in a circuit and additional verification of one in the lines (F_6, F_{10}): 

F = (F_1 F_4 F_8 F_9 \lor F_1 F_4 F_8 F_{10}) \mid (F_9 = 0) = F_1 F_4 F_8 F_{10}.

So, in the process of carrying out of four flexing, which are represented by the lines (F_3, F_6, F_2, F_9), the exact diagnosis was obtained: there is the multiple fault F = (F_1, F_4, F_8, F_{10}) in a circuit.

### 6 Examples of the use of diagnosis methods

**Example 1.**

F = F_1 F_2 F_4 F_5 \lor F_3 F_5 F_7 F_{10} \lor F_1 F_3 F_8 F_9 \lor 
\quad \lor F_1 F_2 F_7 F_{10} \lor F_5 F_6 F_9 F_{10}.

There is the multiple fault F_2 F_7 F_{10} in a device.

1. Sequential probing of terms in test points.

Counting of the weight for every variable that is part of DNF is carried out:

<table>
<thead>
<tr>
<th>F_1</th>
<th>F_2</th>
<th>F_3</th>
<th>F_4</th>
<th>F_5</th>
<th>F_6</th>
<th>F_7</th>
<th>F_8</th>
<th>F_9</th>
<th>F_{10}</th>
</tr>
</thead>
<tbody>
<tr>
<td>W(F_i)</td>
<td>3</td>
<td>2</td>
<td>2</td>
<td>1</td>
<td>3</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

Fault probability in a circuit depends on their weight coefficients. To obtain a single solution in the form of DNF term it is necessary to select such variables for test points, which have minimal weight and invert the terms to zero. So, first three points are F_4, F_5, F_8. After every step the weight coefficient re-calculation is performed. It enables to revise next steps.

F = (F_1 F_2 F_4 F_5 \lor F_3 F_5 F_7 F_{10} \lor F_1 F_3 F_8 F_9 \lor 
\quad \lor F_1 F_2 F_7 F_{10} \lor F_5 F_6 F_9 F_{10}) \mid (F_4 = 0) = 
\quad = F_3 F_5 F_7 F_{10} \lor F_1 F_3 F_8 F_9 \lor 
\quad \lor F_1 F_2 F_7 F_{10} \lor F_5 F_6 F_9 F_{10}.

The weight coefficients of variables, which are parts of the term under probing, are decreased by 1.

<table>
<thead>
<tr>
<th>F_1</th>
<th>F_2</th>
<th>F_3</th>
<th>F_4</th>
<th>F_5</th>
<th>F_6</th>
<th>F_7</th>
<th>F_8</th>
<th>F_9</th>
<th>F_{10}</th>
</tr>
</thead>
<tbody>
<tr>
<td>W(F_i)</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>-</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

The next term probing results in the obtainment of a DNF term.

F = (F_3 F_5 F_7 F_{10} \lor F_1 F_3 F_8 F_9 \lor F_1 F_2 F_7 F_{10} \lor F_5 F_6 F_9 F_{10}) \mid (F_6 = 0) = 
\quad = F_3 F_5 F_7 F_{10} \lor F_1 F_3 F_8 F_9 \lor F_1 F_2 F_7 F_{10}.

2. Parallel probing of several test points.

At parallel probing of several terms in various test points it is convenient to make the cover table for given function:

<table>
<thead>
<tr>
<th>F_1</th>
<th>F_2</th>
<th>F_3</th>
<th>F_4</th>
<th>F_5</th>
<th>F_6</th>
<th>F_7</th>
<th>F_8</th>
<th>F_9</th>
<th>F_{10}</th>
</tr>
</thead>
<tbody>
<tr>
<td>F_1 F_2 F_8 F_9</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>F_3 F_5 F_7 F_{10}</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>F_2 F_7 F_{10}</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>F_3 F_5 F_7 F_{10}</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

The test points F_4, F_6, F_8 don’t correspond to assertion 1 and have minimal weight coefficients, so a few terms (with elements F_4, F_6, F_8) can be probed simultaneously. The initial table is

<table>
<thead>
<tr>
<th>F_1</th>
<th>F_2</th>
<th>F_3</th>
<th>F_4</th>
<th>F_5</th>
<th>F_7</th>
<th>F_{10}</th>
</tr>
</thead>
<tbody>
<tr>
<td>F_3 F_5 F_7 F_{10}</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>F_1 F_2 F_7 F_{10}</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

The points F_3 or F_5 can be used for further probing. Using the point F_3 a single term F_1 F_2 F_7 F_{10} identifies functionality faults of a digital system. Simplification of initial DNF enables to show that there is the multiple fault F_1 F_2 F_7 F_{10} in a circuit. Using the parallel probing method it is realized by less quantity of steps.

### 7 Conclusion

Scientific novelty and practical importance of the research: 1) Algebra-logical method and algorithm of fault embedded diagnosis in functional blocks of...
SoC that uses preliminary analysis of the fault detection table for decrease of its size and the volume of subsequent calculations, related with DNF forming, which determines all solutions of SoC functionalities, diagnosis are proposed. 2) It is proposed the reduced SoC Functional Intellectual Property Infrastructure that is characterized by minimal set of the embedded diagnosis processes in real time and enables to realize the services: testing of the nominal functions on basis of generable input patterns (Automated Test Pattern Generator) and analysis of output reactions; fault diagnosis with given resolution of fault location by means of utilization of the IEEE 1500 multiprobe; fault simulation to provide of realization of the first two procedures on basis of the fault detection table. 3) It is represented the mapping model of the deductive structure synthesis process that differs by utilization of the deductive component library, covering all standardized functional elements, it enables to create the SoC functionality deductive model in computer-aided mode. 4) The mapping-model of fault synthesis that differs by utilization of the embedded test generators library for DSP functionality of SoC is proposed, it enables to decrease the time of test construction essentially, at that tests are designed for functional and fault verification.

The algebra-logical representation of the covering problem has appeal that is directed on optimal solution of all synthesis and analysis problems of complex systems, where the mapping problem exists: 1) a specification — a set of library components; 2) faults — test patterns; 3) functionalities — Testbench; 4) faulty elements — reserved ones; 5) object states — surveillance lines.

To decrease the dimension of the mapping problem it is necessary to structure of the initial model by means of the hierarchy making that is typical and use everywhere in computer-aided design of systems (ESL-, TLM-technologies).

A priori definition of the fault detection table in the Boolean function form is attractive by its compactness that on a concrete experimental validation vector is transformed to compact form, which determines DNF terms as all possible solutions of faulty repairable components.

Further research is oriented on development of testability structure of the system and hardware BIRA module for embedded repair of whatever components in appearance of faults on production and operating stages.

Yervant Zorian (EWDTS’ 2007, Yerevan): “Now the main problem of system on a chip repair is development of technologies and methods of on-chip repair of the logic that occupies no more than 10% of chip area”.

References: