A Numerical Evaluation of Damages Caused by Asynchronous Motors to the Environment

FRANCESCO MUZI, LUIGI PASSACANTANDO
Department of Electrical Engineering and Computer Science
University of L’Aquila
Monteluco di Roio, L’Aquila 67100
ITALY
muzi@ing.univaq.it     luigi.passacantando@tiscali.it

Abstract: - In recent years a slow but progressive increase in the world’s temperatures has been consistently recorded. To oppose this global warming trend, two especially important actions are the monitoring and reduction of greenhouse emissions, in large quantity caused by global electric energy production. To this regard an algorithm is proposed to estimate the particles released into the atmosphere as a consequence of the electric energy produced for the operation of asynchronous motors, which in industrialized countries absorb as much as 60 % of the total electric energy generated. The described procedure can also help to evaluate the possibility to supply motors with electric energy produced from renewable sources instead of from thermal power plants supplying traditional public networks, which would of course reduce the environmental impact of motors to almost zero. Emissions linked to electric energy generation were evaluated on the basis of statistics collected from the main electric utilities. The proposed algorithm was validated by means of laboratory tests performed on a single asynchronous motor working under different operating conditions.

Key-words: - Electric motor operation and consumption, Emissions and pollution, Environmental sustainability.

1 Introduction
In the specialized literature a number of works have dealt with motor energy consumption and efficiency, addressing the geographical distribution and consumption of different kinds of motors as well [1]. In order to improve motor efficiency, many different solutions were proposed, with the basic aim to reduce electric energy absorption while meeting construction constraints and assuring the required performance threshold [2], [12]. Even more so than in the past, attention was recently addressed to digital control strategies and the use of power electronics devices. In this context, particularly successful procedures were adopted, such as the Vector Control (VC) and Scalar Control (HVAC) [3].

On the other hand, also different algorithms were implemented with an aim to increase motor efficiency, following two main research approaches. The former was directed to improve the motor construction features [4], whereas the latter was based on the implementation of control procedures to improve the motor operating performances [5]. In addition, a number of studies were published addressing the errors made in estimating motor efficiency; in this context, the approaches proposed were mainly the Maximum Estimated Error (MEE), the Worst Case Estimated Error (WCEE), and the Realistic Estimated Error (REE) [6].

2 The problem formulation
The issue here was to estimate the amount of emissions into the environment associated to the electric energy drawn by an asynchronous motor. The first step of the proposed procedure is the estimation of the $P_m$ mechanical power on the motor shaft:

$$P_m = C_m \cdot \omega_m \quad [W]$$

where $\omega_m$ is the rotor speed and $C_m$ the electromagnetic torque. $C_m$ can be determined from the dynamic equilibrium equation:

$$C_m - C_r - C_a = J_T \frac{d\omega_m}{dt} \quad [N \cdot m]$$

$$C_m = C_r + C_a + J_T \frac{d\omega_m}{dt} \quad [N \cdot m]$$

The quantities $C_r$, $C_a$ and $J_T$ are the load torque, the friction torque and the moment of inertia, respectively; all of them are known quantities. $\omega_m$ is an unknown and can be estimated with the algorithm illustrated in Section 4. From the knowledge of $\omega_m$, Eq. (3) allows the evaluation of:
\[ \hat{C}_m = C_r + C_a + J_r \frac{d\hat{\omega}_m}{dt} \quad [N \cdot m] \quad (4) \]

The value of \( \hat{C}_m \) introduced in Eq. (1) allows the computation of \( \hat{P}_m \):

\[ \hat{P}_m = \hat{C}_m \cdot \hat{\omega}_m \quad [W] \quad (5) \]

Finally, the electric power drawn by the motor can be estimated from the knowledge of the \( \eta \) motor efficiency:

\[ \hat{P}_e = \frac{\hat{P}_m}{\eta} \quad [W] \quad (6) \]

\( \eta \) can be read from the motor label or evaluated with laboratory tests. It can also be estimated for an equivalent asynchronous load [10], [11].

The \( E_e \) energy supplied by the electrical system can be computed by the following integral:

\[ E_e = \int_0^t P_e \, dt \quad [W \cdot s] \quad (7) \]

If the \( t \) time is assumed (as a reference) as 1 h, the value obtained from Eq. (7) can be easily expressed in kWh. On the other hand, electricity companies are obliged to write an annual report of their emissions on the basis of 1 kWh of produced energy.

The knowledge of the energy required by a single machine for a given industrial working cycle may help to decide how to supply the motor, that is choosing either the external public network or renewable sources available on the premises. Both solutions are shown in Fig. 1.

Recently, increasing energy production from renewable sources [8], [9], [18] is coming from photovoltaic plants. These generation systems can be subdivided into two main categories:

1. Systems connected to a distribution network (grid-connected systems);
2. Systems completely isolated from the grid (stand-alone systems).

The former system type is shown in Fig. 2.

In this case, the electric energy is first converted to the rated frequency and then used to supply the consumer load and/or directly put onto the grid in accordance to a predefined interchange regime [16], [17].

The latter system type is shown in Fig. 3.

In this case, the generated energy supplies directly a load while the surplus energy is generally transferred and stored into appropriate batteries.

Fig.1 Example of different arrangements that can be used to supply motors.

Fig.2 Photovoltaic grid-connected system.

Fig.3 Photovoltaic stand-alone system.
that in their turn will supply the load in absence of solar radiation.

Generally speaking, the main components of a photovoltaic system are: a photovoltaic generator (or photovoltaic field for high-power plants), a power controller and conditioner system and an energy storage system (for stand-alone systems).

The conversion efficiency of the system takes into account the efficiencies of each component such as: the single photovoltaic cell (solar mono-crystal silicon cells having high purity level are able to transform over 23% of solar energy), solar module, power control and conversion system, and eventually the storage system in the stand-alone plants.

In normal conditions, the energy generated by a photovoltaic generator flows to the load and battery simultaneously. When a battery is in discharged condition and the energy required by the load overcomes the generated energy, the photovoltaic generator is connected to a further complementary source that supplies the energy deficit as shown in Fig. 4.

![Fig.4 System with a complementary source.](image)

A photovoltaic stand-alone system does not have complementary sources to fill the energy deficit. In this case information is required about the nature and amount of energy needs to be satisfied on a daily basis, in different seasons or in one whole year. In such conditions, the proposed algorithm may be very helpful in identifying the best possible solutions.

### 3 Emissions compared to electric energy production

The emissions reported in the following are those released by a traditional thermal power plant. In this case, the emitted pollution can be primarily classified as solid, liquid and gas. Another frequently used classification subdivides the generated pollution as follows:

- emissions into the atmosphere;
- avoided CO$_2$ emissions;
- outlet water;
- hazardous waste.

Emissions into the atmosphere include pollutant particles and greenhouse gases. The former category comprises:

- Sulphur dioxide (SO$_2$);
- Nitrogen oxides (NO$_x$);
- Powders.

The latter category comprises:

- Carbon dioxide (CO$_2$);
- Sulphur hexafluoride (SF$_6$);
- Methane (CH$_4$).

SO$_2$ and NO$_x$ come from a combustion process and are consequently produced by thermal power plants. In recent years SO$_2$ and NO$_x$ emissions have been drastically reduced by means of advanced combustion processes and the use of desulphurators, deoxidizers and molecular sieves. As concerns the Italian situation, Fig. 5 shows SO$_2$ and NO$_x$ emissions due to electric energy production from thermal power plants.

![Fig.5 SO$_2$ and NO$_x$ emissions due to electric energy generation.](image)

Of course, also CO$_2$ emissions depend on combustion. Fig. 6 shows CO$_2$ emissions from thermal power plants.

![Fig.6 CO$_2$ emissions.](image)
As shown in Fig. 6, in the last few years also CO\(_2\) emissions (as SO\(_2\) and NO\(_x\) emissions) have been reduced in Italy. Avoided CO\(_2\) emissions can be viewed as a useful indicator in quantifying the penetration level of renewable energy sources. Emissions are often expressed more significantly in [g/kWh] as shown by the diagrams in Figs. 7 and 8.

\[ \text{SO}_2 \text{ [g/kWh]} \quad \text{NO}_x \text{ [g/kWh]} \]

![Fig.7 SO\(_2\) and NO\(_x\) specific emissions.](image)

![Fig.8 CO\(_2\) specific emissions [g/kWh].](image)

### 4 The algorithm for motor speed estimation

The procedure proposed to estimate the \( \hat{\theta} \) motor rotor speed is shown in Fig. 9. The estimate is based on the knowledge of the \( \Delta \theta \) rotor position variation.

The rotor \( \hat{\theta}(t) \) position, \( \omega_r(t) \) speed and \( a_r(t) \) acceleration are linked by the following relations:

\[
\begin{align*}
\frac{d}{dt} \hat{\theta}(t) &= \omega_r(t) \\
\frac{d}{dt} \omega_r(t) &= a_r(t) \\
\frac{d}{dt} a_r(t) &= 0
\end{align*}
\]  

where \( \frac{d}{dt} a(t) \) is an additional estimate equation defining acceleration as a state quantity. In order to implement the model on a DSC (Digital Signal Controller), a discretization of the (8) differential system must be made. Fig. 10 shows a discretization of an \( a_r(t)=\ddot{a} \) constant acceleration inside the \( \Delta t=t-t_0 \) sampling step.

\[ \begin{align*}
\vartheta_r(k) &= \vartheta_r(k-1) + \omega_r(k-1)(\Delta T) + \ddot{a} (\Delta T)^2 \\
\omega_r(k) &= \omega_r(k-1) + \ddot{a} \Delta T \\
a_r(k) &= a_r(k-1) = \dddot{a}
\end{align*} \]

where \( k \) and \( k-1 \) refer to the current and the previous state, respectively.

Equations (9), (10) and (11) can be written in a matrix form as:

\[
\begin{bmatrix}
\vartheta_r(k) \\
\omega_r(k) \\
a_r(k)
\end{bmatrix} = 
\begin{bmatrix}
1 & \Delta T & \frac{\Delta T^2}{2} \\
0 & 1 & \Delta T \\
0 & 0 & 1
\end{bmatrix} 
\begin{bmatrix}
\vartheta_r(k-1) \\
\omega_r(k-1) \\
a_r(k-1)
\end{bmatrix}
\]

Let us define the performed error of the estimate at step \( k \) as:

\[
\varepsilon(k) = a_r(k) - \dddot{a} \rightarrow a_r(k) = \varepsilon(k) + \dddot{a}
\]
Therefore the following relation can be written:

\[ a_i(k-1) = \varepsilon(k-1) + \bar{a} . \]

Finally, relation (12) can be modified as:

\[
\begin{bmatrix}
\varphi_i(k) \\
\omega_i(k) \\
\varepsilon_i(k)
\end{bmatrix} =
\begin{bmatrix}
0 \\
0 \\
0
\end{bmatrix} +
\begin{bmatrix}
1 & \Delta T & \frac{\Delta T^2}{2} \\
0 & 1 & \Delta T \\
0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
\varphi_i(k-1) \\
\omega_i(k-1) \\
\varepsilon_i(k-1)
\end{bmatrix}
\]

\[ a_i(k-1) = \varphi_i(k-1) + \frac{\Delta T^2}{2} \Delta T \]

Finally, relation (12) can be modified as:

\[
\begin{bmatrix}
\Delta \varphi_i(k) \\
\Delta \omega_i(k) \\
\Delta \varepsilon_i(k)
\end{bmatrix} =
\begin{bmatrix}
0 & \Delta T & \frac{\Delta T^2}{2} \\
0 & 1 & \Delta T \\
0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
\varphi_i(k-1) \\
\omega_i(k-1) \\
\varepsilon_i(k-1)
\end{bmatrix}
\]

In order to obtain relations in compact form, the following positions are established:

\[ \bar{x}(k) = \begin{bmatrix} \varphi_i(k) \\ \omega_i(k) \\ \varepsilon_i(k) \end{bmatrix} ; \]

\[ A = \begin{bmatrix} 1 & \Delta T & \frac{\Delta T^2}{2} \\ 0 & 1 & \Delta T \\ 0 & 0 & 1 \end{bmatrix} ; \]

\[ \bar{x}(k-1) = \begin{bmatrix} \varphi_i(k-1) \\ \omega_i(k-1) \\ \varepsilon_i(k-1) \end{bmatrix} ; \]

\[ b = \begin{bmatrix} \frac{\Delta T^2}{2} \\ \frac{\Delta T}{2} \\ 0 \end{bmatrix} ; \quad u = \bar{a} . \]

Finally, the model in a compact form can be written as follows:

\[ x(k) = [A] \cdot \bar{x}(k-1) + b \cdot u \quad \text{State equation (17)} \]

\[ y(k) = [\Delta \varphi(k)] \quad \text{Output equation (18)} \]

The above model is linear and time-invariant since the matrix coefficients are constant.

On the basis of the previous model, an observer based on the Kalman filter can be implemented [13, 17]. Actually, the following non-linear and time-invariant system can be written:

\[
\begin{cases}
\dot{x}_k = f(x_{k-1}, u_k, k) + w_k \\
y_k = h(x_k, u_k, k) + v_k
\end{cases}
\]

where:
- \( x_k \) is the state equation;
- \( y_k \) is the output equation;
- \( f \) and \( h \) are generic equations;
- \( u_k \) is the input of the system;
- \( k \) is the sampling step;
- \( w_k \) is the noise produced by both disturbances and model accuracies;
- \( v_k \) is the noise on the output that is linked to the measurement process.

Noises are assumed to be Gaussian with zero mean.

The implemented algorithm, which is based on the EKF (Extended Kalman Filter), requires two separate processes:

1. Prediction

\[ \tilde{x}_k = A \tilde{x}_{k-1} + b \bar{a}_k \]  

2. Correction

\[ \hat{x}_k = \tilde{x}_k + g \left( y_k - c^T \tilde{x}_k \right) \]  

where “\( g \)” is the gain vector that is assumed as:

\[ g = \begin{bmatrix} g_1 \\ g_2 \\ g_3 \end{bmatrix} \quad \text{and} \quad c^T = [1 \ 0 \ 0] . \]

The proposed procedure assumes the \( \Delta \varphi(k) = \varphi(k) - \varphi(k-1) \) position change instead of
the \( \varphi(k) \) position as output. In this case, the dynamic equation becomes:

\[
\varphi_j(k) = \varphi_j(k-1) + \omega_j(k-1)(\Delta T) + \frac{\Delta \varphi_j(k-1)}{2} + \frac{\Delta \varphi_j(k-1)}{2}
\]

(22)

\[
\varphi_j(k) - \varphi_j(k-1) = \omega_j(k-1)(\Delta T) + \frac{\Delta \varphi_j(k-1)}{2} + \frac{\Delta \varphi_j(k-1)}{2}
\]

(23)

\[
\Delta \varphi_j(k) = \varphi_j(k) - \varphi_j(k-1) = \omega_j(k-1)(\Delta T) + \frac{\Delta \varphi_j(k-1)}{2} + \frac{\Delta \varphi_j(k-1)}{2}
\]

(24)

On the other hand, the dynamic equations of speed and acceleration remain unchanged. Consequently the discrete complete model of the position-variation, speed and acceleration can be written as:

\[
\begin{bmatrix}
\Delta \varphi_j(k) \\
\omega_j(k) \\
\epsilon_j(k)
\end{bmatrix} =
\begin{bmatrix}
0 & \Delta T & \frac{\Delta T^2}{2} \\
0 & 1 & \frac{\Delta T}{2} \\
0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
\Delta \varphi_j(k-1) \\
\omega_j(k-1) \\
\epsilon_j(k-1)
\end{bmatrix} +
\begin{bmatrix}
\Delta \varphi_j(k-1) \\
\omega_j(k-1) \\
\epsilon_j(k-1)
\end{bmatrix}
\]

(25)

Variations will be present only on the state vector of the \([A]\) matrix:

\[
\tilde{x}_k = \bar{x}(k) =
\begin{bmatrix}
\Delta \varphi_j(k) \\
\omega_j(k) \\
\epsilon_j(k)
\end{bmatrix}
\]

Finally, the discrete model becomes:

\[
\bar{x}(k) = [A] \cdot \bar{x}(k-1) + b \cdot u
\]

(26)

\[
y(k) = \Delta \varphi(k)
\]

(27)

where the output measured quantity corresponds to the position-variation.

For the discrete, linear and time-invariant model defined by the (25) matrix equation to be implemented on a DSC, a per unit (p.u.) transformation of the real quantities is required. Therefore equations (20) and (21) can be written in the following form:

Fig. 11 shows a flow-chart of the implemented algorithm.

![Flow-chart of the implemented algorithm](image)

**5 Experimental validation of the model**

Fig. 12 shows the configuration of a laboratory monitoring system that can be adopted to estimate the quantity of emissions released into the environment in consequence of 1kWh energy consumption of one single motor, with data acquisition at the mechanical load side [14]. In laboratory tests the motor speed is measured while in normal cases the speed is estimated using the algorithm of Fig. 11. In order to easily obtain the consumed electric energy in kWh, the operation time of the motor is established as 1h. For certain established \( \omega_m \) speeds, Tables 1 and 2 compare data either measured or estimated by a computation based on the implemented speed-estimate algorithm.
A validation procedure was performed also on the behavior of the algorithm of Fig. 11. In this case the (9) equation model was implemented on a DSC with quantities expressed per units. Fig. 13 compares the speeds estimated by the algorithm and those obtained from laboratory measurements. The saw-tooth function in the figure represents the normalized pulses counted by the encoder whereas the horizontal line consists of two overlapping straight lines representing the measured and estimated speeds, respectively.

As an example, Figs. 14, 15, 16, 17, 18, 19, 20, 21, 22 show the results supplied by the estimate algorithm concerning the particles released into the atmosphere for different load torques and mechanical speeds of the tested motor.

The adoption of an environment management system allows a census of the pollutant emissions which are mainly metals and compounds, nitrogen and compounds, phosphorus and compounds, and in lower quantities the COD (Chemical Oxygen Demand) and BOD (Biochemical Oxygen Demand) parameters.

Table 1 Measured data.

<table>
<thead>
<tr>
<th>Pe[W]</th>
<th>Pm[W]</th>
<th>( \omega_m )[rpm]</th>
<th>( \omega_m )[rad/s]</th>
<th>C+Ca[Nm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>3334.59</td>
<td>2734.36</td>
<td>1274.0</td>
<td>133.459</td>
<td>20.49</td>
</tr>
<tr>
<td>3401.58</td>
<td>2789.30</td>
<td>1300.0</td>
<td>136.137</td>
<td>20.49</td>
</tr>
<tr>
<td>3532.25</td>
<td>2896.45</td>
<td>1350.0</td>
<td>141.373</td>
<td>20.49</td>
</tr>
<tr>
<td>3270.65</td>
<td>2681.93</td>
<td>1250.0</td>
<td>130.900</td>
<td>20.49</td>
</tr>
<tr>
<td>3138.46</td>
<td>2573.54</td>
<td>1200.0</td>
<td>125.664</td>
<td>20.49</td>
</tr>
<tr>
<td>3009.03</td>
<td>2467.40</td>
<td>1150.0</td>
<td>120.428</td>
<td>20.49</td>
</tr>
</tbody>
</table>

Table 2 Estimated data.

<table>
<thead>
<tr>
<th>( \omega_m )[rpm]</th>
<th>( \omega_m )[rad/s]</th>
<th>Pm</th>
<th>Pe</th>
</tr>
</thead>
<tbody>
<tr>
<td>1274.527</td>
<td>133.468</td>
<td>2734.763</td>
<td>3335.08</td>
</tr>
<tr>
<td>1299.921</td>
<td>136.127</td>
<td>2789.251</td>
<td>3401.53</td>
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<tr>
<td>1350.196</td>
<td>141.392</td>
<td>2897.127</td>
<td>3533.08</td>
</tr>
<tr>
<td>1249.613</td>
<td>130.859</td>
<td>2681.306</td>
<td>3269.88</td>
</tr>
<tr>
<td>1200.036</td>
<td>125.667</td>
<td>2574.926</td>
<td>3140.16</td>
</tr>
<tr>
<td>1150.112</td>
<td>120.439</td>
<td>2467.806</td>
<td>3009.52</td>
</tr>
</tbody>
</table>

Tables 3 and 4 show the amount of estimated particles released into the atmosphere as a consequence of the energy drawn and consumed by the tested motor.

Table 3 Estimate of the emitted particles.

<table>
<thead>
<tr>
<th>Pe[W]</th>
<th>( \text{SO}_2[g] )</th>
<th>( \text{NO}_x[g] )</th>
<th>Powders[g]</th>
<th>( \text{CO}_2[g] )</th>
<th>SF6[g]</th>
<th>( \text{H}_2[S]_g )</th>
</tr>
</thead>
<tbody>
<tr>
<td>3532.25</td>
<td>3.2858</td>
<td>3.2859</td>
<td>1.02459</td>
<td>1752.409</td>
<td>3.1798</td>
<td>14.132</td>
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<tr>
<td>3270.65</td>
<td>3.0409</td>
<td>3.0409</td>
<td>.094827</td>
<td>1621.863</td>
<td>2.9429</td>
<td>13.079</td>
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<tr>
<td>3138.46</td>
<td>2.9203</td>
<td>2.9203</td>
<td>.091064</td>
<td>1557.516</td>
<td>2.8261</td>
<td>12.561</td>
</tr>
<tr>
<td>3009.03</td>
<td>2.7988</td>
<td>2.7988</td>
<td>.087276</td>
<td>1492.722</td>
<td>2.7086</td>
<td>12.038</td>
</tr>
</tbody>
</table>

Table 4 Estimate of other emitted particles.

<table>
<thead>
<tr>
<th>Pe[W]</th>
<th>Cells pollutant load[g]</th>
<th>Metals[g]</th>
<th>Nitrogen<a href="total">g</a></th>
<th>Phosphorus<a href="total">g</a></th>
<th>COD[g]</th>
</tr>
</thead>
<tbody>
<tr>
<td>3334.59</td>
<td>1247.319</td>
<td>13340.3</td>
<td>4.002092</td>
<td>0.43356</td>
<td>17.342</td>
</tr>
<tr>
<td>3401.58</td>
<td>1272.171</td>
<td>13606.1</td>
<td>4.081831</td>
<td>0.442198</td>
<td>17.687</td>
</tr>
<tr>
<td>3532.25</td>
<td>1321.373</td>
<td>14123.3</td>
<td>4.236998</td>
<td>0.459301</td>
<td>18.372</td>
</tr>
<tr>
<td>3270.65</td>
<td>1222.937</td>
<td>130795</td>
<td>3.923863</td>
<td>0.425085</td>
<td>17.003</td>
</tr>
<tr>
<td>3138.46</td>
<td>1174.418</td>
<td>125606</td>
<td>3.768185</td>
<td>0.40822</td>
<td>16.328</td>
</tr>
<tr>
<td>3009.03</td>
<td>1125.56</td>
<td>120381</td>
<td>3.611424</td>
<td>0.391238</td>
<td>15.649</td>
</tr>
</tbody>
</table>

Fig. 13 Estimated and measured speeds vs. time as shown by a measurement oscilloscope; a) \( \dot{\omega}_{\text{rpm}} = 0.5 \text{p.u.} \) b) \( \dot{\omega}_{\text{rpm}} = 1 \text{p.u.} \)
Fig. 14 Example of the estimated emissions for constant load torque (18 N m) and constant speed (1498 rpm).

Fig. 15 Example of other estimated emissions for constant load torque (18 N m) and constant speed (1498 rpm).

Fig. 16 Example of other estimated emissions for constant load torque (18 N m) and constant speed (1498 rpm).

Fig. 17 Example of the estimated emissions for constant load torque (18 N m) and constant speed (749 rpm).

Fig. 18 Example of the estimated emissions for constant load torque (18 N m) and constant speed (749 rpm).

Fig. 19 Example of other estimated emissions for constant load torque (18 N m) and constant speed (749 rpm).
6. Conclusions

A method was proposed to estimate the amount of polluting emissions due to the production of electric energy required and consumed by asynchronous motors. Since the reduction of atmospheric pollutants is a mandatory issue in national and international directives, a number of measures are constantly being enacted to improve the efficiency of both electric generation and electric end-uses. The method introduced in this paper is based on the Kalman filter estimate and can be used for monitoring purposes as well as to define the best actions targeted at reducing polluting emissions. Moreover, the method allows also to establish when a motor may be supplied by an internal renewable source instead of an external traditional network. The procedure and the suggested algorithm, implemented on a DSC TMS320F2812 from Texas Instrument, were validated by means of laboratory experimental tests.

References


