# **Control of Nonlinear Systems via Temporal Difference Learning Based Intelligent Controller and Context Reasoning**

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#### Abstract:

Modeling emotions has attracted much attention in recent years, both in cognitive psychology and design of artificial systems. Far from being a negative factor in decisionmaking, emotions have shown to be a strong faculty for making fast satisfying decisions. In this paper, we have adapted a computational model based on the limbic system in the mammalian brain for control engineering applications.

Learning in this model based on Temporal Difference Learning. We applied the proposed controller (termed BELBIC) for a simple model of a submarine. The model was supposed to reach the desired depth underwater. Our results demonstrate excellent control action, disturbance handling and system parameter robustness for TDBELBIC.

The proposal method, regarding the present conditions, the system action in the part and the controlling aims, can control the system in a way that these objectives are attained in the least amount of time and the best way.

#### MODELLING

Motivated by the success in functional modeling of emotions in control engineering applications [15,29,30], the main purpose of this research is to use a structural model based on the limbic system of mammalian brain, for decision making and control engineering applications. We have adopted a network model developed by Moren and Balkenius [21], as a computational model that mimics amygdala, orbitofrontal cortex, thalamus, sensory input cortex and generally, those parts of the brain thought responsible for processing emotions. There are two approaches to intelligent and cognitive control. In the indirect approach, the intelligent system is utilized for tuning the parameters of the controller. We have adopted the second, so called direct approach, where the intelligent system, in our case the computational model termed TDBELBIC, is used as the controller block. The model is illustrated in figure 1. TDBELBIC is essentially an action generation mechanism based on sensory inputs and emotional cues. In general, these can be vector valued, although in the benchmarks discussed in this paper for the sake of illustration, one sensory input and one emotional signal (stress) have been considered. The emotional learning occurs mainly in amygdala. The learning rule of amygdala is given in formula (1).

$$\Delta G_a = k_1 . \max(0, EC - A) \tag{1}$$

where  $G_a$  is the gain in amygdala connection,  $k_1$  is the learning step in amygdala and *EC* and *A* are the values of emotional cue function and amygdala output at each time. The term max in the formula (1) is for making the learning changes monotonic, implying that

the amygdala gain can never be decreased. This rule is for modeling the incapability of unlearning the emotion signal (and consequently, emotional action), previously learned in the amygdala [21,23]. Similarly, the learning rule in orbitofrontal cortex is shown in formula (2).

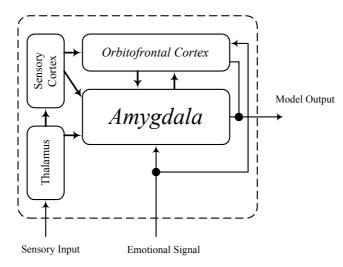


Figure 1- The abstract structure of TDBELBIC

$$\Delta G_o = k_2 .(MO - EC) \tag{2}$$

where  $G_o$  is the gain in orbitofrontal connection,  $k_2$  is the learning step in orbitofrontal cortex and *MO* is the output of the whole model, where it can be calculated as formula (3):

$$MO = A - O \tag{3}$$

in which, o represents the output of orbitofrontal cortex. In fact, by receiving the sensory inputs, the model calculates the internal signals of amygdala and orbitofrontal cortex by the relations in (4) and (5) and eventually yields the output.

$$A = G_a S \tag{4}$$

$$Q = G_a S \tag{5}$$

Since amygdala does not have the capability to unlearn any emotional response that it ever learned, inhibition of any inappropriate response is the duty of orbitofrontal cortex.

#### **IMPLEMENTAION**

Controllers based on emotional learning have shown very good robustness and uncertainty handling properties [29,30], while being simple and easily implementable. To utilize our version of the Moren-Balkenius model as a controller, we note that it essentially converts two sets of inputs into the decision signal as its output. We have implemented a closed loop configuration using this block (termed TDBELBIC) in the feed forward loop of the total system in an appropriate manner so that the input signals have the proper interpretations. The block implicitly implemented the critic, the learning algorithm and the action selection mechanism used in functional implementations of emotionally based (or generally reinforcement learning based) controllers, all at the same time [15,29,30]. The structure of the control circuit we implemented in our study is illustrated in figure 2. The functions we used in emotional cue and sensory input blocks are given in (6) and (7),

$$EC = W_1.e + W_2.CO \tag{6}$$

$$SI = W_3 \cdot PO + W_4 \cdot PO \tag{7}$$

where *EC*, *CO*, *SI* and *PO* are emotional cue, controller output, sensory input and plant output and the  $W_1$  through  $W_4$  are the gains must tuned for designing a satisfactory controller.

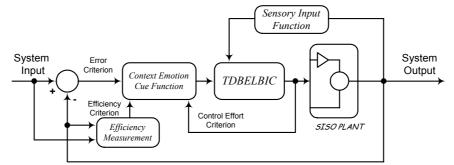


Figure 2 - Control system configuration using TDBELBIC

## SIMULATIONS

We confirmed the capability of TDBELBIC by performing some simulations. It must be mentioned that in the all simulations outlined below, we implemented the set-point control strategy with the desired value of 1. The descriptions of simulations are given below:

### LINEAR SISO SYSTEM: SUBMARINE MODEL

In this simulation, we considered a simple model of a submarine. The model was supposed to reach the desired depth underwater. The quantitative model is represented via (8).

$$G(s) = \frac{0.1(s+1)^2}{s(s^2+0.09)} = \frac{0.1s^2+0.2s+0.1}{s^3+0.09s}$$
(8)

We implemented the control circuits in MATLAB SIMULINK package. The output of the system with a simple feedback and the output of the system with a TDBELBIC controller are given in figure 3.

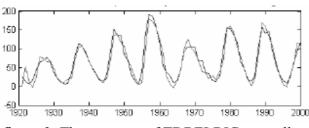


figure 3: The response of TDBELBIC controller

# $TD(\lambda)$ Learning

Most of new learning algorithms like reinforcement learning, Q-learning and the method of temporal differences are characterized by their fast computation and in some cases lower error in comparison with the classical learning methods. Fast training is a notable consideration in some control applications. However, in prediction applications, two more desired characteristics of a good predictor are accuracy and low computational complexity.

In reinforcement learning, there is no teacher available to give the correct output for each training example, which is called unsupervised Learning. The output produced by the learning agent is fed to the environment and a scalar reinforcement value (reward) is returned. The learning agent tries to adjust itself to maximize the reward. [1][2]

Often that the actions taken by the learning agent to produce an output will affect not only the immediate reward but also the subsequent ones. In this case, the immediate reward only reflects partial information about the action. It is called delayed-reward. [2][3]

Temporal difference (TD) learning is a type of reinforcement learning for solving delayed-reward prediction problems. Unlike supervised learning, which measures error between each prediction and target, TD uses the difference of two successive predictions to learn that is Multi Step Prediction. The advantage of TD learning is that it can update weights incrementally and converge to a solution faster. [4]

In a delay-reward prediction problem, the observation-outcome sequence has the form  $x_1, x_2, x_3, ..., x_m, z$  where each  $x_t$  is an observation vector available at time  $t, 1 \le t \le m$  and z is the outcome of the sequence. For each observation, the learning agent makes a prediction of z, forming a sequence:  $P_1, P_2, P_3, ..., P_m$ .

Assuming the learning agent is an artificial neural network, update for a weight w of the network with the classical gradient descent update rule for supervised learning is:

$$\Delta w = -\alpha \nabla_w E = -\alpha \sum_{t=1}^m (P_t - z) \nabla_w P_t \qquad (9)$$

Where  $\alpha$  is the learning rate and  $\nabla_w E$  is the gradient vector,  $\frac{\partial E}{\partial w}$  of the mean square error

function:

$$E = \frac{1}{2} \sum_{t=1}^{m} \left( P_t - z \right)^2$$
(10)

In [3], Sutton derived the incremental updating rule for equation (9):

$$\Delta w_t = \alpha (P_{t+1} - P_t) \sum_{k=1}^t \nabla_w P_k$$
(11)

For 
$$t = 1, 2, ..., m$$
 where  $P_{m+1} = z$ 

To emphasize more recent predictions, an exponential factor  $\lambda$  is multiplied to the gradient term:

$$\Delta w_t = \alpha (P_{t+1} - P_t) \sum_{k=1}^t \lambda^{t-k} \nabla_w P_k \qquad (12)$$

Where  $0 \le \lambda \le 1$ 

This results in a family of learning rules,  $TD(\lambda)$ , with constant values of  $\lambda$ . But there are 2 special cases:

First, when  $\lambda = 1$ , Eq. (12) falls back to Eq. (11), which produces the same training result as the supervised learning in Eq. (9). Second, when  $\lambda = 0$ , since  $0^0 = 1$ , Eq. (12) becomes

$$\Delta w_t = \alpha (P_{t+1} - P_t) \nabla_w P_k \tag{13}$$

I can extended the Eq. (13) for BELBIC and made Eq. (14) for TDBELBIC.  $\Delta G_{\Omega t} = \alpha (z - P_t) \nabla G_{\Omega} P_t \qquad (14)$ 

Which has a similar form as Eq. (9). So the same training algorithm for supervised learning can be used for TD(0).

## **Conclusion:**

In figure (3), you can observe the results of simulating the diagram block figure (2). The results, based on temporal difference learning, are compared to Orbitofrontal Cortex learning in a shared TDBELBIC structure. The outcomes suggest that temporal difference based learning in faster than Orbitofrontal Cortex learning. But faster learning is increased for maximum overshoot. Both of the learning is increase rates represent their memory output signals are presented in figure (4), (5). The increase rates represent their learning speed.

Paying attention to the achievements in the emotional controls founded a computational model, based on the Limbic system, for mammals' brain via time series learning. The paper tried to develop this method for answering more complicated issues and achieving difficult goals.

To do this, the ability of the learning module the emotional controller, was increased achieving based a brain computational model means of temporal difference learning for credit assignment. Temporal difference learning, has easier computations because of using it's own experience. The methods resemble human behavioral learning.

BEBIC Output	TDBEBIC Output
BELBIC Emotional Signal	TDBELBIC Emotional Signal
Amygdala BELBIC Output	Amygdala TDBELBIC Output

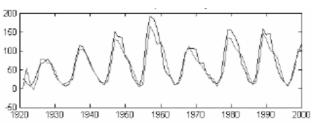


Figure (4): Comparison of BELBIC and OFC Learning with BELBIC and TD Learning

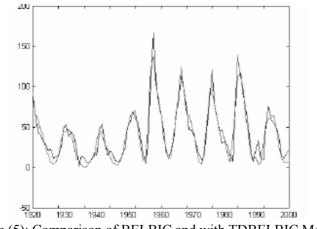


Figure (5): Comparison of BELBIC and with TDBELBIC Memory

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