# MATLAB program for Simulation and Control of the Continuous Stirred Tank Reactor

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Abstract—The paper shows advantages of the computer technology for the simulation of the technological system's behaviour and control. The technological process here is represented by the Continuous Stirred Tank Reactor (CSTR) as a typical member of a nonlinear lumped-parameters system widely used in the industry. The computer simulation has great importance nowadays with the decreasing value of the computer components together with the growing computer speed. The adaptive control used here fulfils all basic control requirements and it can be used for the systems with nonlinear behaviour. The benefit of this paper can be found in the simulation program made in mathematical software MATLAB with the use of Graphical User Interface (GUI) that provides user possibilities to examine simulations without changing of the program code.

**Keywords**—Matlab, modeling, simulation, adaptive control, recursive identification.

# I. INTRODUCTION

THE most of processes in the real world, not only in the industry has nonlinear behaviour. On the other hand, chemical reactors belong to the most often equipments in the chemical and biochemical industry and that is why this paper is focused on one particular member of this family – the Continuous Stirred Tank Reactor (CSTR) with exothermic reaction inside.

Specific design of the controller is usually precede by few very important steps. Not every property of the controlled system is known before we start and that is why we perform simulation experiments on the system. There are two main types of the investigating of the system's behaviour - (1) experiment on the real model and (2) computer simulation. Computer simulation is very often used at present as it has many advantages over an experiment on a real system, which is not feasible and can be dangerous, or time and money demanding.

Simulation and modelling possibilities rise with the increasing impact of the digital technology and especially with the

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computer technology which grows exponentially every moment.

The mathematical model of this particular CSTR is described by the set of two nonlinear Ordinary Differential Equations (ODEs) which are constructed with the use of material and heat balances inside. Examples for deriving such mathematical models can be found in [1]. The steady-state analysis investigates behaviour of the system in the steady-state which from the mathematical point of view means numerical solving of the set of nonlinear algebraic methods. The simple iteration method [2] was used in this case because the system fulfills the convergence condition. The next step is the dynamic analysis which practically means numerical solving of the nonlinear set of ODEs. A lot of numerical solution methods have been developed, especially for the ODE, such as Euler's method or Taylor's method [3]. Runge-Kutta's methods are very popular because of their simplicity and easy programmability [4].

The basic idea of adaptive control is that parameters or the structure of the controller are adapted to parameters of the controlled plant according to the selected criterion [5]. The adaptive approach in this work is based on choosing an *external linear model* (ELM) of the original nonlinear system whose parameters are recursively identified during the control. Parameters of the resulted continuous controller are recomputed in every step from the estimated parameters of the ELM.

The polynomial method introduced by Kucera [6] used for designing of the controller here together with the pole-placement method ensures basic control requirements such as stability, reference signal tracking and disturbance attenuation. The basic control system configurations with one degree-of-freedom (1DOF) and two degrees-of-freedom have been used. The proposed controller is hybrid because polynomial synthesis is made for continuous-time but recursive identification runs on the  $\delta$ -model, which belongs to the class of discrete-time models.

The MATLAB (MATrix LABoratory) is mathematical software often used for computation and simulation [7]. Although this software has it own programming language, it also provides the tool for creating window-like programs which can be used for testing and simulation without changing of the program and knowledge about this programming language. This tool called GUIDE was used here for creating of the simulation program as a practical output of this contribution.

This program is available for free. If you are interested, please contact author on his email address – vojtesek@fai.utb.cz.

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#### II. MODEL OF THE PLANT

The proposed control strategy was tested on the mathematical model of Continuous Stirred Tank Reactor (CSTR). This model has simple exothermic reaction inside the tank which is cooled via cooling coil – see Fig. 1.

Mathematically speaking, this plant is represented by the mathematical model which describes all quantities is of course very complex and we need to introduce some simplifications. First, we expect that reactant is perfectly mixed. Then, we also assume that volume, heat capacities and densities do not change rapidly during the control.

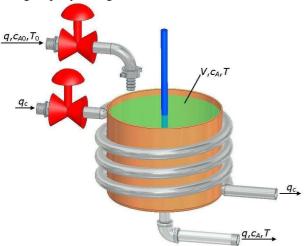


Fig. 1 The schematic representation of CSTR

These assumptions results in the mathematical model represented by the set of two Ordinary Differential Equations (ODE) [8] which are derived from the material and heat balances of the reactant and cooling, i. e.

$$\frac{dT}{dt} = a_1 \cdot (T_0 - T) + a_2 \cdot k_1 \cdot c_A + a_3 \cdot q_c \cdot \left(1 - e^{\frac{a_4}{q_c}}\right) \cdot (T_{c0} - T) \tag{1}$$

$$\frac{dc_A}{dt} = a_1 \cdot (c_{A0} - c_A) - k_1 \cdot c_A$$

where  $a_{1-4}$  are constants computed as

$$a_1 = \frac{q}{V}; a_2 = \frac{-\Delta H}{\rho \cdot c_p}; a_3 = \frac{\rho_c \cdot c_{pc}}{\rho \cdot c_p \cdot V}; a_4 = \frac{-h_a}{\rho_c \cdot c_{pc}}$$
(2)

The fixed values of the system are shown in Table 1.

FIXED PARAMETERS OF THE REACTOR

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Quantity	Symbol and value
Reactor's volume	$V = 100 \ l$
Reaction rate constant	$k_0 = 7.2 \cdot 10^{10} \ min^{-1}$
Activation energy to R	$E/R = 1 \cdot 10^4 K$
Reactant's feed temperature	$T_0 = 350 \ K$
Inlet coolant temperature	$T_{\rm c0} = 350 \ K$
Reaction heat	$\Delta H = -2 \cdot 10^5 \ cal.mol^{-1}$
Specific heat of the reactant	$c_p = 1 \ cal.g^{-1}.K^{-1}$
Specific heat of the cooling	$c_{pc} = 1 \ cal.g^{-1}.K^{-1}$
Density of the reactant	$\rho = 1.10^3 \ g.l^{-1}$
Density of the cooling	$\rho_c = 1.10^3  g.t^1$
Feed concentration	$c_{A0} = 1 \ mol.l^{-1}$
Heat transfer coefficient	$h_a = 7.10^5 \ cal.min^{-1}.K^{-1}$

The nonlinearity of the model is hidden mainly in the computation of the reaction rate,  $k_1$ , which is nonlinear function of the temperature, T, and it is computed from Arrhenius law:

$$k_1 = k_0 \cdot e^{\frac{-E}{RT}} \tag{3}$$

#### III. STEADY-STATE AND DYNAMIC ANALYSES

The pre-control simulation often includes steady state and dynamic analyses which help us with the understanding, how system works in different states and behaves after various changes on the input.

## A. Steady-state Analysis

The steady-state analysis shows behaviour of the system in the steady-state, i.e. in  $t \to \infty$  and results in optimal working point in the sense of maximal effectiveness and concentration yield. Mathematical meaning of the steady-state is that derivatives with respect to time variable are equal to zero,  $d(\cdot)/dt = 0$ .

The previous studies [9] have shown interesting steady-state feature of this reactor. It is clear, that the reactant and cooling heat must be equal in the steady-state, i.e.  $Q_r = Q_c$ , which means that the equation (1) in steady-state is rewritten to:

$$a_{1} \cdot (T_{0} - T) + a_{2} \cdot k_{1} \cdot c_{A} + a_{3} \cdot q_{c} \cdot \left(1 - e^{\frac{a_{4}}{q_{c}}}\right) \cdot (T_{c0} - T) = 0$$

$$(4)$$

and results in relations for these heats  $Q_r$  and  $Q_c$ :

$$Q_r = a_2 \cdot k_1 \cdot c_A^s$$

$$Q_c = \begin{bmatrix} a_1 + a_3 \cdot q_c \cdot \begin{pmatrix} \frac{a_4}{q_c} \\ 1 - e^{\frac{q_c}{q_c}} \end{bmatrix} \cdot T^s - \begin{bmatrix} a_1 \cdot T_0 + a_3 \cdot q_c \cdot \begin{pmatrix} \frac{a_4}{q_c} \\ 1 - e^{\frac{q_c}{q_c}} \end{bmatrix} \end{bmatrix}$$
(5)

If we compute  $Q_r$  and  $Q_c$  for various values of the temperature  $T = \langle 300, 500 \rangle$  K for working point  $q = 100 \ l.min^{-1}$  and  $q_c = 80 \ l.min^{-1}$ , we obtain three steady-states – see Fig. 2.

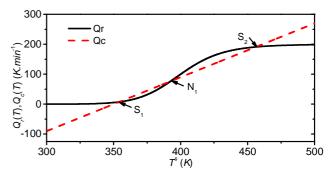


Fig. 2 Heat balance inside the reactor

As you can clearly see, this system has two stable steady-states ( $S_1$  and  $S_2$ ) and one unstable steady state ( $N_1$ ). The steady-state values of the state variables in these points are:

$$S_1: T^s = 354.23 K c_A^s = 0.9620 \text{ mol.} I^{-1}$$
  
 $N_1: T^s = 392.45 K c_A^s = 0.6180 \text{ mol.} I^{-1}$   
 $S_2: T^s = 456.25 K c_A^s = 0.0439 \text{ mol.} I^{-1}$ 

$$(6)$$

It is clear, that the second operating point  $S_2$  has better efficiency (95.6 % reacts) for the same input settings than on the point  $S_1$  (3.8 % reacts).

So the steady-state model is finally described by the set of nonlinear functions

$$T^{s} = \frac{a_{1} \cdot T_{0} + a_{2} \cdot k_{1} \cdot c_{A}^{s} + a_{3} \cdot q_{c} \cdot T_{0} \cdot \left(1 - e^{\frac{a_{4}}{q_{c}}}\right)}{a_{1} + a_{3} \cdot q_{c} \cdot \left(1 - e^{\frac{a_{4}}{q_{c}}}\right)}$$
(7)

$$c_A^s = \frac{a_1 \cdot c_{A0}}{a_1 + k_1}$$

which are easily solved numerically by the simple iteration method.

## B. Dynamic Analysis

This analysis means that we observe course of the state variables in time after the step change of some input variable. The step changes of volumetric flow rates q and  $q_c$  are input variables in our case and the steady-state values in Equation (6) are initial conditions for the set of ODE (1). The Runge-Kutta's fourth order method was used for numerical solving of the set of ODE.

#### IV. ADAPTIVE CONTROL

There could be used several so called "modern" techniques to control of this process such as robust control, predictive control, fuzzy control etc. In our case, the adaptive control was used mainly because of its strong theoretical background and usability for such kind of processes.

The Adaptive control is based on the quality of real organisms which can change behavior according to environmental conditions. This process is usually called "adaptation". There are several ways of use of the adaptation. It can be done for example by the modification of the controller's parameters by the change of the controller's structure or by generating an appropriate input signal, which is called "adaptation by the input signal".

The adaptive approach in this work is based on choosing an external linear model (ELM) of the original nonlinear system whose parameters are recursively identified during the control. Parameters of the resulted continuous controller are recomputed in every step from the estimated parameters of the ELM. The advantage of this method is that we do not care about the system nonlinearity. First we do the dynamic analysis that shows us the dynamic behavior of the output variable which is then used for the choice of the ELM which describes the output in the most accurate way. The possible change of the ELM parameters is taken into account by the recursive identification of ELM during the control.

## A. External Linear Model (ELM)

The ELM could be generally described by the transfer function:

$$G(s) = \frac{Y(s)}{U(s)} = \frac{b(s)}{a(s)} \tag{8}$$

The presence of the variable s in the Equation (8) indicates continuous-time (CT) model. The online identification of such processes which is necessary in this case is not very easy.

One way, how we can overcome this problem is the use of so called  $\delta$ -model. These special types of models formally belong to discrete models but it was proofed for example in [10] that their parameters are close to the continuous ones for very small sampling period.

The  $\delta$ -model introduces a new complex variable  $\gamma$  ([11]):

$$\gamma = \frac{z - 1}{\beta \cdot T_{\nu} \cdot z + (1 - \beta) \cdot T_{\nu}} \tag{9}$$

Where  $\beta$  is a parameter from the interval  $0 \le \beta \le 1$  and  $T_{\nu}$  means a sampling period. It is clear that we can obtain infinite number of  $\delta$ -models for various  $\beta$ . A so called *forward*  $\delta$ -model for  $\beta = 0$  was used and  $\gamma$  operator is then

$$\gamma = \frac{z - 1}{T_{\nu}} \tag{10}$$

The continuous model (8) is then rewritten to the form

$$a^{\delta}(\delta) y(t') = b^{\delta}(\delta) u(t') \tag{11}$$

where polynomials  $a^{\delta}(\delta)$  and  $b^{\delta}(\delta)$  are discrete polynomials and their coefficients are different, but for the small sampling period very close to those of the CT model a(s) and b(s).

These parameters identified recursively, which means that they are computed by the Recursive Least Squares (RLS) method from differential equation

$$y_{\delta}(k) = \boldsymbol{\theta}_{\delta}^{T}(k) \cdot \boldsymbol{\varphi}_{\delta}(k-1) + e(k)$$
(12)

Where  $\phi_{\delta}$  stands for known regression (data) vector,  $\theta_{\delta}$  represents vector of parameters and e(k) is a general random immeasurable component.

# B. Recursive Identification

As it is written above, the well known and easily programmable Recursive Least-Squares (RLS) method is used for the on-line identification. This method is usually modified with some kind of forgetting; exponential or directional [12] mainly due to specific features of the identified system like nonlinearity etc.

The basic RLS method is described by the set of equations:

$$\varepsilon(k) = y(k) - \boldsymbol{\varphi}^{T}(k) \cdot \hat{\boldsymbol{\theta}}(k-1)$$

$$\gamma(k) = \left[1 + \boldsymbol{\varphi}^{T}(k) \cdot \mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k)\right]^{-1}$$

$$\boldsymbol{L}(k) = \gamma(k) \cdot \mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k)$$

$$\mathbf{P}(k) = \frac{1}{\lambda_{1}(k-1)} \left[\mathbf{P}(k-1) - \frac{\mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k) \cdot \boldsymbol{\varphi}^{T}(k) \cdot \mathbf{P}(k-1)}{\lambda_{1}(k-1) + \boldsymbol{\varphi}^{T}(k) \cdot \mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k)}\right]$$

$$\hat{\boldsymbol{\theta}}(k) = \hat{\boldsymbol{\theta}}(k-1) + \boldsymbol{L}(k)\varepsilon(k)$$
(13)

Where the "forgetting" could be affected by the choice of the forgetting factor  $\lambda_1$ .

The identification methods used in the program are:

Without forgetting, e.g. no forgetting factor is inserted. Constant exponential forgetting is for  $\lambda_1 < 1$  and

Constant exponential forgetting is for  $\lambda_1 < 1$  and  $\lambda_2 = 1$ . The values of forgetting factor  $\lambda_1$  are from the range <0.95; 0.99>. Parameter  $\lambda_1$  influences gradual forgetting of

the old values and the most weight is put on the last values. This relation can be described by criterion

$$J = \sum_{i=1}^{k} \lambda^{k-i} \varepsilon_i^2 \tag{14}$$

This algorithm can be used for systems with changing

Increasing exponential forgetting has forgetting parameters  $\lambda_2 = 1$  and  $\lambda_1$  is computed from

$$\lambda_{1}(k) = \lambda_{0}\lambda_{1}(k-1) + 1 - \lambda_{0} \tag{15}$$

Typical values of the forgetting parameters are  $\lambda_1(0) = \lambda_0 \in \langle 0.95, 0.99 \rangle$ . The value of this forgetting factor is asymptotically approaching to 1, which means that the old data is forgotten.

Changing exponential forgetting has again the value of forgetting parameter  $\lambda_2 = 1$  and exponential forgetting  $\lambda_1$  is recomputed in every step as

$$\lambda_{1}(k) = 1 - K \cdot \gamma(k) \cdot \varepsilon^{2}(k) \tag{16}$$

where K is a very small value (e.g. 0.001).

Directional forgetting. This algorithm forgets information only in the direction from which it comes. General description of this method can be formulated by the following equations:

$$r(k-1) = \boldsymbol{\varphi}^{T}(k) \cdot \mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k)$$

$$L(k) = \frac{\mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k)}{1 + r(k-1)}$$

$$\beta(k-1) = \begin{cases} \lambda_1(k-1) - \frac{1 - \lambda_1(k-1)}{r(k-1)} & \text{for } r(k-1) > 0 \\ 1 & \text{for } r(k-1) = 0 \end{cases}$$

$$\mathbf{P}(k) = \mathbf{P}(k-1) - \frac{\mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k) \cdot \boldsymbol{\varphi}^T(k) \cdot \mathbf{P}(k-1)}{\beta^{-1}(k-1) + r(k-1)}$$

$$\mathbf{P}(k) = \mathbf{P}(k-1) - \frac{\mathbf{P}(k-1) \cdot \boldsymbol{\varphi}(k) \cdot \boldsymbol{\varphi}^{T}(k) \cdot \mathbf{P}(k-1)}{\beta^{-1}(k-1) + r(k-1)}$$

where  $\lambda_1$  can be chosen similarly as in exponential forgetting.

### C. Control System Synthesis

The control system configuration with one degree-of-freedom (1DOF) was used this work - see Fig. 3.

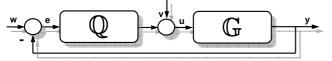


Fig. 3 1DOF control configuration

G in Fig. 3 denotes transfer function (8) of controlled plant, w is the reference signal (wanted value), v is disturbance, e is used for control error, u is control variable and y is a controlled output.

The feedback part of the controller are designed with the use of polynomial synthesis:

$$Q(s) = \frac{q(s)}{s \cdot p(s)} \tag{18}$$

where parameters of the polynomials p(s) and q(s) are computed by the Method of uncertain coefficients which

compares coefficients of individual s-powers from Diophantine equation [6]:

$$a(s) \cdot s \cdot p(s) + b(s) \cdot q(s) = d(s)$$
(19)

The resulted, so called "hybrid", controller works in the continuous time but parameters of the polynomials a(s) and b(s) are identified recursively in the sampling period  $T_v$ .

The feedback controller Q(s) ensures stability, disturbance attenuation for both configurations and asymptotic tracking.

The polynomial d(s) on the right side of (19) is an optional stable polynomial. Roots of this polynomial are called poles of the closed-loop and their position affects quality of the control. This polynomial could be designed for example with the use of Pole-placement method. The degree of the polynomial d(s) is in this case

$$\deg d(s) = \deg a(s) + \deg \tilde{p}(s) + 1 \tag{20}$$

A choice of the roots needs some a priory information about the system's behaviour. It is good to connect poles with the parameters of the system via spectral factorization. The polynomial d(s) then for our ELM (8) can be rewritten for aperiodical processes to the form

$$d(s) = n(s) \cdot (s + \alpha)^{\deg d - \deg n}$$
(21)

where  $\alpha > 0$  is an optional coefficient reflecting closed-loop poles and stable polynomial n(s) is obtained from the spectral factorization of the polynomial a(s)

$$n^*(s) \cdot n(s) = a^*(s) \cdot a(s) \tag{22}$$

## V. SIMULATION PROGRAM

The simulation program which deals with the simulation of the steady-state, dynamics and of course adaptive control of the CSTR was made in mathematical software MATLAB (MATrix LABoratory), version 7.0.1 from Mathworks [7] using Graphical User Interface (GUI). The use of this tools enable programmer to make program user-friendly and close to the users who do not know or do not like programming. They can use all features of Matlab as a simulation tool by just changing of the most important variables and pressing buttons for computing.

The program can be start by the typing the command go in the program's directory. It is divided into two main windows mainly because of the space. The first window (Fig. 4) involves simulation of the steady-state and dynamics of the system. The user can set the working point of the reactor which is defined by volumetric flow rates of the reactant and the cooling,  $q_r$  and  $q_c$ , input temperatures of the reactant and the cooling,  $T_{r0}$  and  $T_{c0}$ , and input concentration of the reactant,  $c_0$ . The next part gives user choice between two stable states S1 or S2 which closely described in chapter III.

The third part is dedicated to the steady-state analysis where two analyses could be done - the steady-state analysis for different volumetric flow rate of the reactant  $q_r$  and different volumetric flow rate of the coolant  $q_c$  where the starting and end values could be set in the edit boxes. The steady-state analysis for both input variables together is represented by the push-button "Compute 3D" and results in 3D graphs. The sample results of the steady-state analysis are shown in Fig. 5.

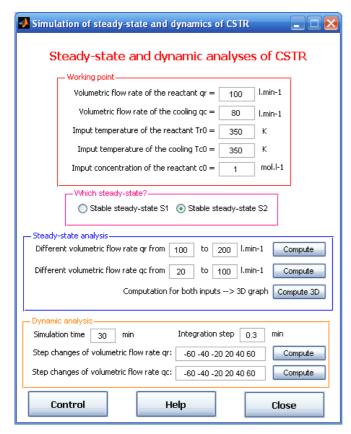


Fig. 4 GUI for the simulation of the steady-state and dynamics of CSTR

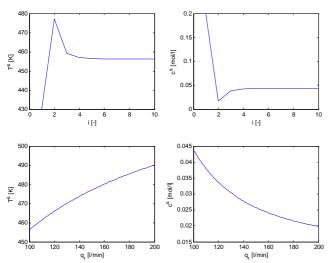


Fig. 5 Sample results of the steady-state analysis

The last part is focused on the dynamic analysis which could be done for step changes of both input variables  $q_r$  and  $q_c$ . Both dynamic analyses can be done for more step changes (e.g. six step changes -60, -40, -20, 20, 40 and 60 as it can be seen in Fig. 4). The simulation time and the integration step in Runge-Kutta's method could be set via appropriate edit boxes. Again, the sample results of the dynamic analysis are shown in Fig. 6.

The buttons in the bottom of the window used for opening the next window for control (push-button "Control"), displaying

the help to the program (push-button "Help") and closing of this window and all graphs (push-button "Close").

The second sub-program called by the pressing of the push-button "Control" or by the command <code>go\_control</code> from the Matlab's command window deals with the simulation of the adaptive control. The window is displayed in Fig. 7.

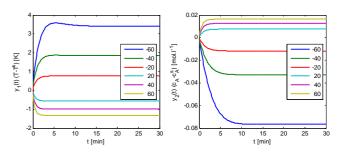


Fig. 6 Sample results of the dynamic analysis

The first two parts related to the working point and the choice of the steady-state are the same as in previous case. The new part here is the choice of the external linear model and settings for the control where the user could set the position of the root  $\alpha$ , sampling period  $T_{\nu}$ , definition of step changes of the reference signal w(t) which represents wanted value and time when they occur.

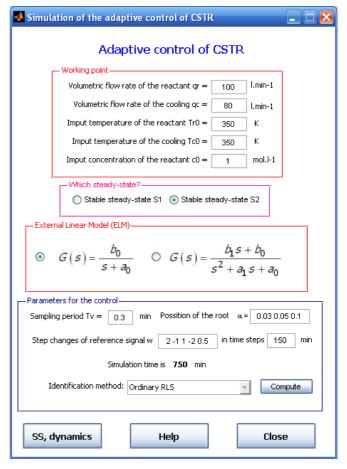


Fig. 7 GUI for the simulation of the adaptive control of CSTR

The final simulation time is recomputed according to the number of steps and time for each step. The last part in this sub-window is dedicated to the choice of recursive methods (see Fig. 8) for identification.

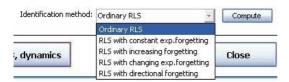


Fig. 8 The choice of the identification method

The buttons below has the same functions as in previous case except the first push-button on the left which will call the program for simulating of the steady-state and dynamics in this case. Simulation results of the adaptive control can be seen in Fig. 9.

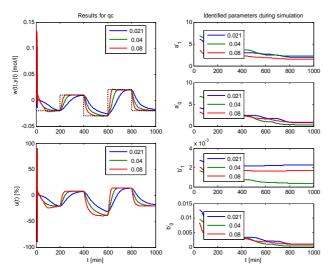


Fig. 9 Sample results of the adaptive control

As a result of the simulation, program shows the final value which indicates what computation was done and in which MAT-file are data saved in. The name of this file differs with the computation – see Fig. 10.



Fig. 10 GUI with the results of the computation

# VI. CONCLUSION

The main goal of this contribution is to show usability of the mathematical software MATLAB for creating simulation programs which could help users to investigate the behaviour of the nonlinear system represented by the CSTR. The resulting program has two main windows – the first provides the simulation of the steady-state and dynamics of the system

for different values of input quantities. Results are displayed in the separate figures and the data were also saved in the MAT-files. The second program deals with adaptive control of this system and user can again set different input variables and choose various computations. The benefit of this program can be found in the GUI which provides changing of the most important values by the edit windows instead of the change of the program code. The program is available also for free at the author email.

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