

# Problem-Based Learning In Calculus Course : Perception, Engagement And Performance

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**Abstract.** Calculus is an important subject for science and engineering students but phenomenally it is abstract, difficult and highly boring. Hence, problem-based learning (PBL) which adopted a student-centered and active learning approach can be used to improve students' participation, interests and performance in learning of calculus. This study is designed to investigate: (1) student's perception about PBL approach in calculus; (2) student's engagement during the acquisition of understanding of calculus and; (3) student's performance as a result of PBL learning experience. A group of 24 Foundation Year students was randomly selected to undergo the PBL approach in Basic Calculus course. A rubric-scoring assessment was used to evaluate students engagement level, a questionnaire with open ended question was used to assess students' perception of PBL learning, and a post-test to measure students' performance after undergoing PBL approach. This pedagogical approach has made the teaching and learning of calculus more interesting and effective. It is also able to develop the potential of individuals to be more creative, critical in their thinking and effective in problem solving.

**Key-Words:** Problem Based Learning, Calculus, Engagement in learning, Education Technology; Performance

## 1 Introduction

Calculus is most important subject for science and engineering students in university because its use is widespread in science, engineering, medicine, business, industry, and many other fields to understand and apply the concept of change and motion. However many students cannot achieve a deep understanding and find that calculus is very hard and abstract [1]. Students were forced to learn it to pass the examination. They often questioned and claimed, "What / Why am I going to do with this anyway? It is of no importance". Student may only memorize formulae and procedures that have been taught in the class to find the task has been assigned [2]. The task or problems presented during lessons seemed meaningless or do not have any "real" meaning for them [3]. Many students wonder why they should learn calculus and how calculus would be useful in their future work after graduation.

Generally, traditional approaches is teacher-centered where students are not actively involved in lectures but passively follow their teacher and are isolated from the real world in learning. Teacher plays a leading role in transferring information. They are the authority, expert, the main source of knowledge, and the focal point of all activity in the class [4]. Thus, teacher centered teaching does not provide an active learning environment for students. Teachers also should not only transmit knowledge but also cultivate some lifelong learning skills in their students [5].

Passive learning is relatively easy for both lecturers and students. Students passively involved in class will lack an understanding of the calculus ideas used to solve problems, and will be confused in their future study and work when they encounter problems that are not in textbooks. Sequentially to motivate students to become independent and active learners many faculties have

suggested ways to improve teaching and learning calculus by making better, more active and meaningful strategies in teaching [6]. Active learning will induce development of skills in “doing” mathematics rather than “knowing” mathematics. This type of students is capable of solving problems, building mathematical model, abstracting, inventing and providing [7].

In an effort to improve the teaching and learning in calculus, a reformed curriculum was introduced at some institutions, which makes use of multiple representations of calculus concepts and use of technology. This new curriculum move from teacher centered teaching to student centered learning that allowed students actively involved in teaching and learning as much as possible. Research shows that student success rate was dramatically improved due to the change of course structure and content delivery [8].

Underpinning with in constructivism theories, problem-based learning (PBL) is one of student centered and active learning strategies or approach which can be used to improve students’ interests and often lead to deep level understand hence acquiring the learning outcomes of a course. [9][5].

This pedagogical approach has made the teaching and learning of calculus more interesting and effective. It has potential to develop individuals to be more creative, critical in their thinking and effective in problem solving [10].

## 2 Problem Based Learning in Calculus

Problem based learning is defined in many ways but the most widely accepted definition of PBL is an instructional strategy whereby student are required to solve the ill structured problem (real world problem) in a collaborative environment by identifying facts related to it. Unlike traditional approach, which is often conducted in lecture format, teaching in PBL normally occurs within small discussion groups of students facilitated by a faculty tutor. The student brainstorms and hypothesizes about the underlying process of the problem and come up with possible solutions [11][12]. Problems were posed to students acting as triggers in this learning environment, thus they became skilled in problem solving, creative thinking, and critical thinking.

In PBL the problem may not be solvable, but nevertheless provides a rich environment for learning. This aim is to learn rather than to solve the problem. Work with real-world and practical problem cooperatively can make them interesting, because these problems may be related to their personal development and hobbies.

Implementation of PBL in calculus class would provide the students more opportunities to think

critically, represent their own creative ideas, and communicate with their peers mathematically [13]. A lot of researches show that PBL improved student learning and it widely use in educational settings. PBL can foster students’ intrinsic motivations and develop their self-learning skills because it provides a student-centered and self-oriented learning for students to seek solutions to real world problems proposed that those who undertook PBL are significantly better in the development of critical thinking dispositions than those who took lecture courses [9][14][15].

Numerous literatures had indicated that PBL positively influence learning outcomes along with learners’ higher order thinking skills such as creative thinking, problem solving, logical thinking and decision making. Elshafei found that students in PBL settings had higher levels of achievement and better solutions in Calculus compared to student in traditional setting [16]. Similar to above studies, several researchers claimed that PBL had a positive influence on problem solving and critical thinking skills [17][18]. However, there are very few studies on the effectiveness of PBL in calculus or mathematics. A study was conducted by Akinoglo and Tandogan to determine the effects of PBL in Introduction of Calculus-Physic on students’ academic achievement and concept found that PBL model had positive effect on academic achievement and attitudes [19]. It was also found that the application of PBL model affected students’ conceptual development positively.

## 3. Methodology

The general aim of this study is to determine the effect of PBL approach in enhancing students’ learning experience in calculus. Specifically, this study aimed to investigate student’s perception about PBL approach in learning calculus; student’s engagement during acquisition of knowledge via PBL; student’s performance in calculus after undergoing PBL.

This study was conducted using the quasi experimental design which comprised of two groups of students. Participants involved in this study were 44 students Foundation Year students in private university enrolled in Basic Calculus course. The students were from same program of studies and were randomly assigned to control group named as TRAD Group (n=24 student) and treatment group which was named as PBL Group (n=24 student). The learning sessions were based on the topic of derivative which is part of the Basic Calculus course. The duration of the experiment was two weeks. Group PBL were given a brief description and training about process of learning in PBL approach in the first class of experimental period. The rubric of

student engagement, questionnaire with open ended question and post test were used for data collection tool.

## 4 Result

### 4.1 Students Perception

Based on the questionnaire responses, more than half students (58%) preferred to learn in group and (40%) prefer to learn in pair. These students also preferred to engage in group or pair work (75%) rather than individual work (25%). In terms of study approach, most students preferred case study approach (75%) and project approach (25%). Half of this group preferred their lecturer to direct them on what to learn (50%) and do the classroom teaching (46%). Only small number (21%) is willing to have free hand to decide what they want to learn. This indicates that this group needs the lecturer to assist them to ensure that they were able to participate in the learning activities. In learning process, nearly half of students (48%) preferred to learn through exchanging of ideas with others.

Benefits of this approach perceived by the students included the ability to discuss, query and correct misunderstandings and the development of transferable skills. Students also mentioned that they felt more confident, independent and were therefore more willing to contribute to discussion. Almost all students (84%) stated that the PBL approach requires them to do a lot of self study and do a lot of research.

Seven (7) positive themes about PBL approach were categorized according to the open ended question in questionnaire "What is your comment/view about PBL approach in calculus?". The seven themes were as follows:

- (1) PBL enhance working in groups and increase interactivity. (eg: "We work together to solve the problem. Everybody must play the role to fulfill the requirement and nobody sleeps");
- (2) PBL encourage search for information. (eg: "I have the opportunity to state my opinion. I also need to know what I know and identify things that are needed to solve the problem");
- (3) PBL allow applying of interesting or relevant calculus concepts.(eg: "I will able to relate what I've been learning to the application in daily life. It's more interest");
- (4) PBL allows opportunity for hearing different perspectives within group and intergroup (eg: "Views and solutions form other group helped me better understand to solve the issue has submitted");
- (5) PBL stimulates thinking (eg : "Stimulate my mind to further outstanding certain topic or ideal

and boost our self to adhere independence in finding solution");

(6) PBL allows flexibility in time (eg: "It is good approach, so that student will be more independent and unstressed") and;

(7) PBL allows process of learn to learn (eg: "I learned to think critically in solving the problem and also learn to cooperate with other").

Clearly students in PBL approach enjoyed working in groups and recognize the scope for different perspectives within their group. This may suggest that both elements (engagement and thinking opportunity) are beneficial to students in their first semester at university in which they benefited from PBL experiences. Central to the effectiveness of PBL is the ability of students to work together to solve problems. The relevance of applying calculus concepts to an authentic situation or problem is largely attributable to the PBL nature of the exercise. Having flexibility in time and learning activity will open up more opportunities for the student to be independent learners and free to explore deeper learning.

### 4.2 Engagement

In this study, eleven (11) items were used in the rubric assessment to evaluate level of student engagement. For each item, students were given 3 point if they showed "Exemplary" engagement, 2 point for "Proficient" and 1 point for "Partially Proficient". According to the average rubric engagement score during learning process, 25% of the respondent can be classified as an Exemplary, (58.3%), 16.7% as Proficient and the rest of the students were Proficient Partially. Detail percentage frequency student in each engagement categories as in Table 1. Mean average rubric engagement score = 2.08, this indicated that this group maybe classified as Proficient in terms of collaborative and cooperative engagement during their PBL activity in the learning of calculus.

### 4.3 Performance

To investigate our hypothesis of association between Total Score Engagement Rubric and Calculus Achievement Test, a correlation was computed using Pearson correlation coefficient. Using Cohen's (1988) guidelines, there was a medium positive correlation between engagement scores and performance with an r of 0.45 [ $r(22) = 0.45, p < 0.05$ ]. These results indicated that high score in engagement during learning session are associated with high performance in Calculus Achievement Test.

An independent-samples t-test was conducted to compare the performance in Calculus Achievement Test between treatment group (PBL group) and control group

(TRAD group), to support the correlation analysis result. There was no significant difference in Calculus test achievement PBL group as table 2 (M= 78.44, SD = 13.49) and TRAD group (M= 78.23, SD = 15.23); t (46)

= 0.05, p = 0.960 > 0.05). The magnitude of the difference in the means was very small (eta = 0.007, eta squared = 0.00).

**Table 1 : Student Engagement**

No	Item [Exemplary - 3 point] [Proficient - 2 point] [Proficient Partially - 1 point]	Engagement Categories		
		Exemplary	Proficient	Proficient Partially
1.	Consistently stays focused on the task given and self directed.	29.2%	37.5%	33.3%
2.	As team member that who contributes encourages and supports the efforts of others in the group.	16.7%	50.0%	33.3%
3.	Follows through on assigned tasks independently and responsibility.	16.7%	58.3%	25.0%
4.	Asks insightful and challenging questions to help understanding and learning.	12.5%	54.2%	33.3%
5.	Demonstrates poise and confidence when answering questions.	25.0%	45.8%	29.2%
6.	Indicates signs of active listening and interest	16.7%	58.3%	25.0%
7.	Gathers research and shares useful ideas when participating in the group discussion.	20.8%	45.8%	33.3%
8.	Makes necessary compromises to accomplish a common goal and help keep the group working well together.	33.3%	33.3%	33.3%
9.	Has a positive attitude about the task(s) and the work of others.	20.8%	50.0%	29.2%
10.	Performed duties of assigned team role and contributed knowledge, opinions and skills to share with the team.	20.8%	50.0%	29.2%
11.	Has high value of acceptance and tolerance in encouraging diversity of ideas in the group.	16.7%	54.2%	29.2%

**Table 2 : Comparison of PBL group and TRAD group Performances**

Independent Samples T-Test										
Based	Group	N	Mean	Std. Deviation	t	df	Sig.(2-tailed)	Mean Diff	Eta	Eta <sup>2</sup>
Test1	PBL	24	78.44	13.49	0.05	46	<b>.960</b>	0.21	.007	.000
	Control	24	78.23	15.42						

## 5 Discussion and Conclusion

Problem-based learning as a constructivist teaching method often plays an important role during teaching and learning process. As a result, PBL can provide meaningful learning experiences hence effective learning. This pedagogical approach hopefully will be able to produce graduate in the 21st century who should be able to transfer the knowledge to solve a real problem, make a judgment individually, have a broad perspective and insights into his/her field, have imaginative and creative powers, communicate and cooperate with others, utilize new technology and ready for lifelong learning.

The study showed that the students have a positive perception towards implement of PBL approach in

calculus learning. It also increases their motivation to learn calculus and observe the applicability of calculus in real-life. According to the students, PBL approach is a group based which encourages them to gather information, take active role in lessons, hence increasing success and gaining self confidence amongst them. The main difference between PBL approach and teacher based method is to solve the problems in scenarios with the group and being forced to do research (learn to learn). Teacher based approach in calculus are boring, decreased attention, knowledge thought to be gained were easily forgotten. Whilst in PBL approach students were able to undergo searching of information, sharing the knowledge gained in the group and making discussions, increase interactivity and the success

motivated the students to improve their achievement and self confidence. PBL developed students to play an effective role during learning, thus as active learners students were lead to better performance by the end of the learning process. In conclusion, PBL in calculus will offer the advantages as it promotes collaborative and distributed learning; development of learners' critical thinking, evaluative and judgment/ decision making skills and enables new and inexperienced learners to access and learn from captured solutions of expert problem solvers.

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