

Gear noise detection. An integrated method using Fourier and Wavelet approach

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Abstract: - This work deals with the objective measurement of the gear noise, in particular with the analysis of the gear whine which represents transmission noises resulting from gears engaged in the torque flow, *i.e.* teeth engagement noise.

In this paper we present results obtained by our basic noise research on the vibration of gears using a "traditional" Fourier's approach compared with an "innovative" Wavelet's approach.

Key-Words: - Signal processing, Gear noise, Wavelet Transform, Multiresolution analysis.

1 Introduction

Noise and vibration properties of cars have become important criteria in the competition between automotive manufacturers and together with new legislation are an important reason to reduce noise and vibrations.

Moreover, noise and vibrations are seen as indicators of the quality of the product: noisy products create a "cheap" impression while silent products gives the impression of quality. Moreover, car manufacturers' demands, on one hand, to reduce the total vehicle weight and on the other hand, to increase power at lower speed. As a consequence noise due to the gearbox is expected to increase and to be less masked by the engine noise.

The most common method for gear noise assessment is subjective evaluations. Evaluators either drive the vehicle or listen to the tape on which the noise data was recorded to rank the noise. The subjective evaluations have some drawbacks. First of all, the subjective ratings are not consistent and may change from time to time. Secondly, the resolution of the ratings is limited by the auditor's ability to distinguish small difference in the gear noises. Additionally, the cost for conducting a subjective evaluation is much higher than for an objective one. Subjective evaluation often requires more people to be involved.

For this reason, this work deals with the objective measurement of the gear noise, in particular with the analysis of the gear whine which represents transmission noises resulting from gears engaged in the torque flow, *i.e.* teeth engagement noise.

In this paper we present results obtained by our basic noise research on the vibration of gears using a "traditional" Fourier approach compared to an "innovative" Wavelet approach.

2 Problem Statement

Many vehicle manufacturers, research and academic institutions have focused their attention on vehicle acoustic design. Noise emissions produced by the transmission play a significant role. In fact, transmission acoustic rating is one of the customer's acceptance criterion.

The most maddening vibrations are induced by the engagement impulse ($f = nz / 60$, n is the speed and z is the number of teeth). The greater the load, the more important the entity of this impulse is. The angular speed of the mating gears has a relevant influence too. Acoustic optimization has to find solutions that minimize such impulses.

Our research activities therefore have been planned according to the following development roadmap:

- 1st phase: noise generation *i.e.* teeth engagement

- 2nd phase: noise transfer *i.e.* gearbox housing and bearings
- 3rd phase: noise emission *i.e.* the transmission housing to the human perception.

Typically, to reduce the gear whine noise, two options are possible:

- optimization of the gear's macro-geometry *e.g.* using high contact ratio gears that leads to minor noise emissions in conjunction with higher transmitted power levels
- optimization of the gear's micro-geometry *e.g.* by trying to balance load-induced teeth deflections with profile corrections which generally leads to less noisy transmission effects. This is not a suitable solution for an overall working range; therefore profile corrections must be determined statistically to take into account manufacturing deviations which will overlap their effect.

This paper focused on the 1st phase. The goal is to find a method to process the data in order to find the teeth engagement discontinuity during the torque transmission which caused noise.

All the experimental activities are performed in Elasis using the Virtual Engine Simulator described in the next paragraph.

3 Virtual Engine Simulator

The ELASIS Virtual Engine Simulator (VES) is the latest tool for automotive transmissions NVH testing. A view of a VES setup for testing and evaluating the gear noise is shown in Fig. 1.



Fig. 1. Virtual engine simulator

The major benefit of using VES in gear noise testing is its ability to reproduce engine output irregularities, therefore, gearboxes can be objectively evaluated and tested without the need to build their associated engines. This capability is extremely important in reducing the product time to market.

Since VES can accurately reproduce mean value of both speed and combustion and inertia forces, car manufactures are able, in this way, to test prototype gearbox earlier in the process, before prototype engines are available.

Fig. 2 shows a schematic diagram of the virtual engine simulator. As shown in this figure, unlike conventional test rigs, this particular virtual engine simulator has a mechanical coupling between the input dynamometer and a high performance dynamic pulse generator.

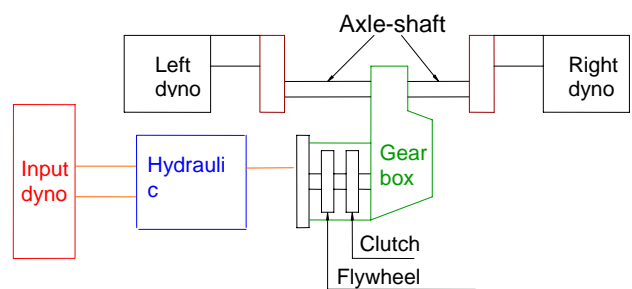


Fig. 2. Virtual engine simulator: schematics

In order to load the gearbox output shafts, each half-shaft is equipped with additional dynamometers to simulate road loads. The output dynamometers are sized to cover a wide range of vehicle speeds and torques. In addition to the simulated road loads, flywheels are installed on the output dynamometer to represent vehicle inertias. The virtual engine simulator can be controlled by providing excitation time histories generated either by computer software (synthesized) or measured on a real vehicle.

4 Experimental testing

As shown in Figure 3, the test-rig is installed in a semi anechoic chamber where dynamometers are soundproofed inside enclosures. In the same way, in order to achieve appropriate background conditions for gear noise measurements, the floor is covered with soundproofing material.

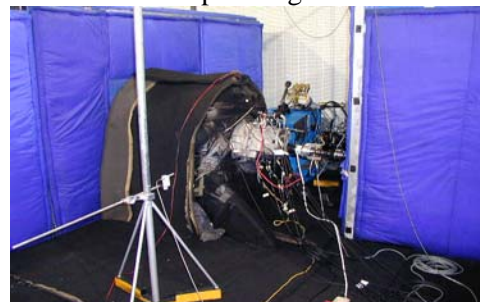


Fig. 3. Virtual engine simulator settled in semi anechoic chamber

Such a set-up, unlike what happens on the vehicle or in a power train test-cell, uncouples the noise generated by the gearbox from the other noises present on the vehicle or generated by the engine. For this reason, the noise problem is pronounced and consequently, noise investigation becomes easier and more objective.

The test rig is equipped with the following signals:

- engine shaft velocity fluctuation measured by magnetic sensors at the flywheel and at the primary shaft
- sound pressure level (SPL) measured by using capacitive microphones (sensitivity 0.051 V/Pa), located at one meter far from transmission housing
- piezoelectric accelerometers (sensitivity 1pC/ms⁻²) placed on the gearbox housings.

The gearbox oil temperature is also monitored because of the strong influence of the gear whine with the oil viscosity. All the tests are performed at 70°C.

A five-speed manual shifted transmission is used for the analysis presented in this paper. The time history acquired on the car is first recorded, during a wide-open throttle condition with the 2th gear engaged, and then it is reproduced on the test rig. The 2th gear is selected because it leads to very audible gear whine noise inside the vehicle cabin, especially up to 5500 rpm.

5 Data processing and results

5.1 Traditional Fourier's method

The accelerometer used in this test has been placed on the gearbox housing (Fig. 4), in correspondence of the contact point of gears.



Fig. 4. Acceleration measure point

Fig. 5 shows the time history of the 2th gear for the engine speed (green, red) and accelerometer vibrations (blue).

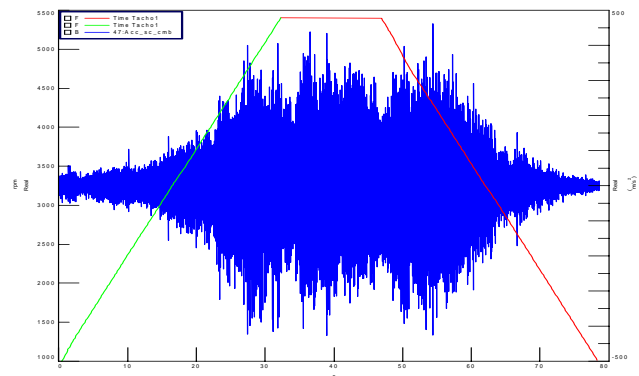


Fig. 5. Time history and vibrations

Duration of signals is roughly 80 seconds and it consists of one slow acceleration in 33 seconds, a stationary phase (12 seconds) and then a deceleration in 33 seconds.

The conversion from time-domain data to frequency domain is performed using the Fast Fourier Transform (FFT) [1] technique. In this application, where the engine speed is steadily increasing and decreasing (engine run up & run down case respectively), a family of FFT operations is obtained to scan the range of the engine speed of interest. Thus, two Campbell diagrams [2] have been created, one for the acceleration phase and the other for the deceleration phase.

Acquired signal has been processed with a sampling frequency of 51200 hz, using Hanning windowing [3] and a resolution of 25 rpm (round per minute).

Fig. 6-7 show the contribution in frequency according to engine speed. In order to indicate the signal amplitude a chromatic scale is used.

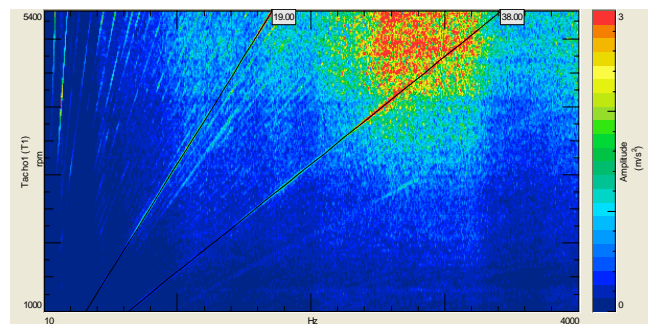


Fig. 6. Campbell diagram during acceleration phase

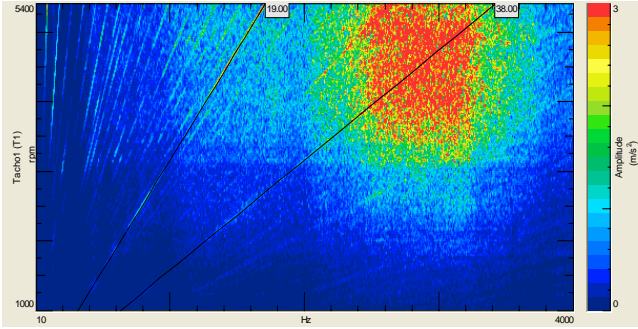


Fig. 7. Campbell diagram during deceleration phase

Spectral content is calculated to extract the overall levels and engagement orders for both run up and run down maneuvers.

The engagement orders are referred to:

- the gear order (order 19) and its first harmonic (order 38)
- the final reduction order (order 7.4) and its first harmonic (order 14.8).

Fig. 8 reports the order analysis for both acceleration and deceleration phase.

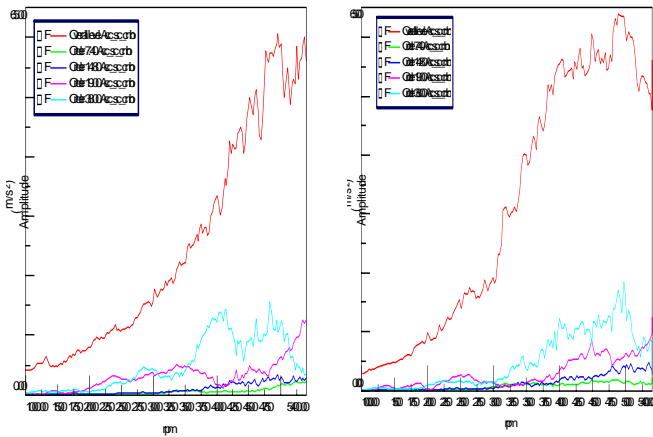


Fig. 8. overall level and engagement orders

5.2 Wavelet Transform

The word wavelet is used in mathematics to denote a kind of orthonormal bases in L^2 with remarkable approximation properties.

Wavelets allow to simplify the description of a complicated function in terms of small number of coefficients. Often there are less coefficients necessary than in the classical Fourier analysis. Wavelets are adapted to local properties of functions to a larger extent than the Fourier basis. The adaptation is done automatically in view of the existence of a second degree of freedom: the localization in time (or space, if multivariate functions are considered).

The vertical axis in the next graphs denotes always the level, i.e., the partition of the time axis into finer and finer resolutions. The advantage of this “multiresolution analysis” is that we can see immediately local properties of data and thereby influence our further analysis. There were attempts in the past to modify the Fourier analysis by partitioning the time domain into pieces and applying different Fourier expansions on different pieces. But the partitioning is always subjective. Wavelets provide an elegant and mathematically consistent realization of this intuitive idea [4].

In summary, wavelets offer a frequency/time representation of data that allows us time (respectively, space) adaptive filtering, reconstruction and smoothing.

Recall that a mother wavelet ψ is a function of zero h -th moment (e.g. see [5], [6], [7], [8])

$$\int_{-\infty}^{+\infty} x^h \psi(x) dx = 0, \quad h \in \mathbf{N}. \quad (1)$$

From this definition, it follows that, if ψ is a wavelet whose all moments are zero, also the function $\psi_{jk}(x) = 2^{j/2} \psi(2^j x - k)$ is a wavelet.

Now consider a wavelet ψ and a function φ such that $\{\{\varphi_{j,k}\}, \{\psi_{j,k}\}, k \in \mathbf{Z}, j = 0, 1, 2, \dots\}$ is a complete orthonormal system. In this case, a given signal $s(t)$, decomposed by wavelet (i.e., CWT) is represented in the following detail function coefficients

$$d_{jk} = \int_{-\infty}^{+\infty} s(\tau) \cdot \frac{1}{\sqrt{2^j}} \psi\left(\frac{\tau - k}{2^j}\right) d\tau \quad (2)$$

and in the approximating scaling coefficients as follows

$$a_{j_0k} = \int_{-\infty}^{+\infty} s(\tau) \cdot \varphi(\tau - k) d\tau \quad (3)$$

Note that, for any j , d_{jk} can be regarded, as a function of k . Consequently, if the signal $s(t)$ is a smooth function, then the relative details are zero, since, as said before, a wavelet has zero moments (for a detailed argumentation see [5]).

The sequence of spaces $\{V_j, j \in \mathbf{Z}\}$, generated by φ is called a multiresolution analysis (MRA) of $L^2(R)$ if it satisfies the following properties

$$V_j \subset V_{j+1}, j \in \mathbf{Z} \text{ and } \bigcup_{j \geq 0} V_j \text{ is dense in } L^2(R).$$

It follows that if $\{V_j, j \in \mathbf{Z}\}$, is a MRA of $L^2(R)$, we say that the function φ generates a MRA of $L^2(R)$, and we call φ the father wavelet.

Besides, based on Parseval theorem, for any $s \in L^2(R)$, it follows that

$$h_0^2 + h_1^2 + h_2^2 + h_3^2 = 1$$

$$h_0 h_2 + h_1 h_3 = 0$$

and the ‘‘approximation condition of $p = L/2 = 2$ order’’

$$g_0 + g_1 + g_2 + g_3 = 0$$

$$0g_0 + 1g_1 + 2g_2 + 3g_3 = 0$$

In the present work (i.e., $L = 4$) the solution of condition is [5]

$$h_0 = \frac{1 + \sqrt{3}}{4\sqrt{2}}$$

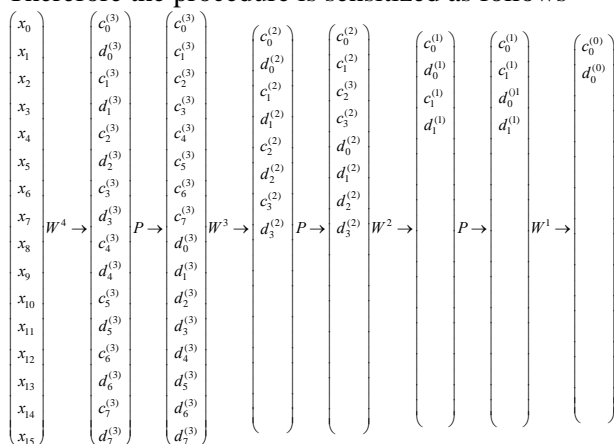
$$h_1 = \frac{3 + \sqrt{3}}{4\sqrt{2}}$$

$$h_2 = \frac{3 - \sqrt{3}}{4\sqrt{2}}$$

$$h_3 = \frac{1 - \sqrt{3}}{4\sqrt{2}}$$

The DWT consists in applying the W^j matrix in hierarchical way to the vector $x(W^j)$ of length $N = 2^j$, then to the *coarse* vector obtained by the convolution of x with the low-pass filter h (of $N/2 = 2^{j-1}$ length, with the W^{j-1} matrix), therefore still to the vector of $N/4$ length obtained from the next convolution with the filter h , and so on until to a prefixed level J_0 or when the convolution with the low-pass filter supplies a single element. The last procedure takes the name of pyramidal algorithm. In order to explain the procedure let us consider the case $N = 16 = 2^4$.

Therefore the procedure is sensitized as follows



where P is a permutation matrix of elements of vector x which orders all the coefficients of type ‘‘ c ’’ (i.e., *coarse* coefficients) and type ‘‘ d ’’ (i.e., *detail* coefficients). Practically the W^j matrix of order j acts on *coarse* coefficients of j level, while

the *detail* coefficients of the same level are unchanged. Therefore at the end the wavelet transform vector will be formed as following

$$(c_0^{(0)} d_0^{(0)} d_1^{(1)} d_0^{(2)} d_1^{(2)} d_2^{(2)} d_3^{(2)} d_0^{(3)} d_1^{(3)} d_3^{(3)} d_4^{(3)} d_5^{(3)} d_6^{(3)} d_7^{(3)})^T$$

where $c_0^{(0)}$ means the *coarse* coefficient obtained at the fourth step of wavelet transform, $d_0^{(0)}$ indicates the *detail* coefficient obtained on the same step, $d_0^{(1)}, d_1^{(1)}$ are the *detail* coefficients obtained at the third step of transform, the $d_k^{(2)}, k = 0, \dots, 3$ represent the *detail* coefficients obtained at the second step and finally $d_k^{(1)}, k = 0, \dots, 7$ the *detail* coefficients obtained at the first step of transform. Since the procedure is based on orthogonal linear operations equally the WT will show the same feature.

For the calculation of the inverse transform, it will be sufficient to repeat the steps of the transform in the inverse order.

The performance of the WT algorithm is evaluated for real data. In this first experiment, we considered the real data shown in Fig. 5 as the input signal and applied the DWT to each signal decomposition level. The Fig. 9 below shows two singularities at 5th and 6th decomposition level.

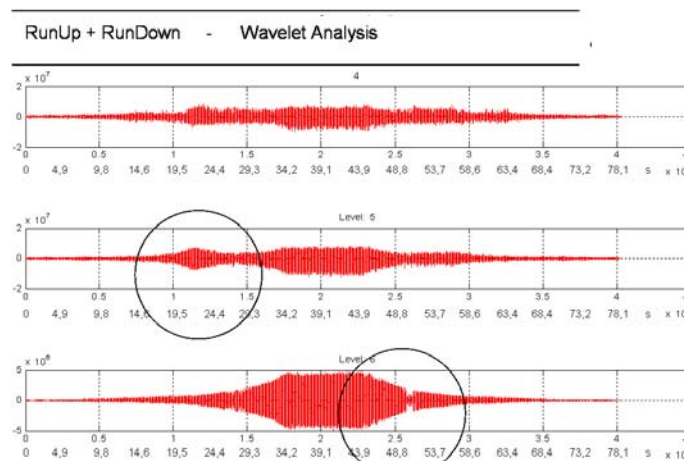


Fig. 9 RunUp + RunDown – Wavelet Analysis

6 Conclusions

This paper presents a new gearbox noise detection algorithm based on analyzing singular points of vibration signals using the Wavelet Transform. The proposed algorithm is compared with a previously-developed algorithm associated with

the Fourier decomposition using Hanning windowing. Simulation carried on real data demonstrate that the WT algorithm achieves a comparable accuracy while having a lower computational cost. This makes the WT algorithm an appropriate candidate for fast processing of noise gear box.

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