# **Steady State Modeling of Isolated Induction Generators**

K.S. SANDHU Professor, Electrical Engineering Department National Institute Of Technology, Kurukshetra-136119 Haryana, India

*Abstract* – Isolated induction generators usually called self-excited induction generators seem to be most suitable machines for wind energy conversion in remote and windy areas. Estimation of steady state performances for such machines is must to encounter the problems, which may appear under real operating conditions. In this paper, a new and simple modeling approach, including a unique equivalent developed by the author, is adopted to analyze the steady state performance of a self-excited induction generator (SEIG). The study reveals that the performance of self-excited induction generator is greatly influenced by the operating speed and excitation capacitance. This gives an opportunity for proper handling of these parameters to obtain the required performance characteristics. Constant frequency and iterative models have been proposed for the analysis and control of SEIG. Simulated results as obtained have been compared with experimental results on a test machine and found to be in close agreement.

Key-words –Isolated Induction Generator, Renewable Generation, Steady State Analysis (SSA), Self- Excited Induction Generator, Wind Energy Generation,

#### NOMENCLATURE

- *a* per unit frequency*b* per unit speed
- *C* excitation capacitance per phase
- $E_1$  air gap voltage per phase at rated frequency
- $E_2$  rotor emf per phase referred to stator
- $E_a$  air gap voltage per phase=  $aE_1$
- f rated frequency
- $I_1$  stator current per phase
- $I_2$  rotor current per phase, referred to stator
- *I*<sub>L</sub> load current per phase
- $I_m$  magnetizing current per phase
- Pout output power
- *R* load resistance per phase
- $R_1$  stator resistance per phase
- $R_2$  rotor resistance per phase, referred to stator

V	terminal voltage per phase
$X_1$	stator reactance per phase
$X_2$	rotor reactance per phase, referred to stator
X <sub>c</sub>	capacitive reactance due to $C$ at rated frequency
$X_m$	magnetizing reactance per phase at rated frequency

### 1. Introduction

generator slip

It is found that self-excited induction generators (SEIG) are most suitable for many applications including wind and small hydroelectric energy conversion systems. Such generators may also be used for lighting or cooking purpose to minimize the requirement of conventional fuels in the remote areas. SEIG has many advantages such as brushless construction (squirrel-cage rotor), reduced size, absence of DC power supply for excitation as in conventional generators, reduced maintenance cost, self short-circuit protection capability and no synchronizing problem.

Proper circuit representation and accurate mathematical modeling is must to evaluate the steady-state performance of a SEIG for different operating conditions. In order to estimate the performance of a SEIG, researchers have made use of the conventional equivalent circuit of an induction motor. Some of the researchers [1-7] used the impedance model, and a few [8-11] used the admittance-based model for such computations. However it has been felt that the old conventional equivalent circuit model, in the absence of an active source, does not effectively correspond to generator operation. Therefore [10-12] suggested a new circuit model for the representation of induction generator. Further it is found that most of the researchers uses the modeling, which results in to a single polynomial equation of higher order in unknown generated frequency and magnetizing reactance.

This paper is an attempt to present two techniques (with new equivalent circuit model developed by the author) to analyze the steady state operation of a self-excited induction generator (SEIG). Proposed analysis needs only the solution of quadratic equation, irrespective of operating conditions. Computed results using proposed methodology have been compared with experimental results. The closeness between experimental and computed results confirms the validity of the proposed modeling.

### 2. Steady State Equivalent Circuit Model

The steady-state operation of the self-excited generator may be analyzed by using a new equivalent circuit [Appendix-1] representation as shown in Fig. 1.

Further, this network may be modified to a more practical format as given by Fig. 2, wherein  $E_a(1+s)$  represent source voltage corresponding to mechanical power transformed to electrical power through rotor.



Fig. 1. Per phase equivalent circuit representation for self-excited induction generator.



Fig. 2. Modified per phase equivalent circuit representation for self-excited induction generator.

Where,

$$R_{L} = \frac{RX_{c}^{2}}{a^{2}R^{2} + X_{c}^{2}}$$

$$X_{L} = \frac{aR^{2}X_{c}}{a^{2}R^{2} + X_{c}^{2}}$$
(1)

### 3. Constant Frequency Model

Circuit analysis of Fig. 2 results in to the following;

$$A_2 s^2 + A_1 s + A_0 = 0 (2)$$

Where,

$$A_{2} = a^{2} X_{2}^{2} R_{IL}$$

$$A_{I} = -R_{2} \left( R_{IL}^{2} + X_{IL}^{2} \right)$$

$$A_{0} = R_{IL} R_{2}^{2}$$

$$R_{IL} = R_{I} + R_{L}$$

$$X_{IL} = a X_{I} - X_{L}$$
&

X

$$\mathbf{b} = \mathbf{a} \, (1+s) \tag{3}$$

It is observed that equation (2) in terms of slip always comes to be quadratic expression irrespective of nature of load. Equation (2) & (3) may be used to determine the operating speed to generate a particular frequency for given value of excitation capacitance and load resistance. This gives an opportunity to control the generated frequency. Further following expression as obtained from the analysis may be used to determine the saturated value of magnetizing reactance.

$$X_{m} = \left[\frac{-R_{2}\left(R_{1L}^{2} + X_{1L}^{2}\right)}{sa^{2}X_{2}R_{1L} + aR_{2}X_{1L}}\right]$$
(4)

 $X_m$  as obtained may be used to determine the value of air gap voltage'  $E_1$ ' using Appendix-2.

### 4. Iteration Model

Approximate equivalent circuit representation of induction generator, after omitting stator impedance and rotor reactance, results in the operating slip as;

$$s = \frac{R_2}{R} \qquad (5)$$

Where generated frequency is

$$a = \frac{b}{1+s} \tag{6}$$

Equation (5) and (6) may be used to compute the initial value of frequency  $a_0$  (to start the iteration process) as;

5th WSEAS Int. Conf. on ENVIRONMENT, ECOSYSTEMS and DEVELOPMENT, Tenerife, Spain, December 14-16, 2007 422

$$a_0 = \frac{b}{1 + \frac{R_2}{R}} \tag{7}$$

Once the initial value for generated frequency is known, the iteration process may be carried out using the following steps;

- 1. Computations of initial value of frequency  $a_0$  from (7).
- 2. Estimation of the value of *s* from (2) after substituting the value of *a* as  $a_0$ .
- 3. Finding of the new value of generated frequency *a'* using the computed value of slip obtained in step 2, from (6).
- 4. Comparison of the new value of frequency a' with previous frequency used in step 2 i.e.  $a_0$ .

If  $|a'-a_0|\langle \varepsilon$ 

Where  $\varepsilon = 0.00000001$ 

Then a' may be treated as generated frequency, other wise process may be repeated by replacing  $a_0$  with a' until difference in the successive values for generated frequency comes out to be  $\varepsilon$ .

Proposed modeling may be used to estimate the generated frequency of SEIG. Further  $X_m$  may be obtained using (4), which gives the value of air gap voltage using magnetization curve. Once air gap voltage ' $E_1$ ' at rated frequency is known, then the performance of the machine may be obtained using equivalent circuit representations as given by Fig. 1 and Fig. 2.

#### 5. Operating Limits

Equation (2) & (3) gives the expression for operating slip as

$$s = \frac{R_2(R_{IL}^2 + X_{IL}^2) \pm R_2 \sqrt{(R_{IL}^2 + X_{IL}^2)^2 - 4a^2 R_{IL}^2 X_2^2}}{2a^2 X_2^2 R_{IL}}$$
(8)

The above equation gives two possible values of slip to which the stipulated operating conditions confirm too. But only the lower of the two values is relevant for generating mode.

This slip will be real only if

$$R_{1L}^{2} + X_{1L}^{2} \ge 2a R_{1L} X_{2}$$
(9)

If the limiting value (minimum) of  $(R_{1L}^2 + X_{1L}^2)$  given by equation (9) is substituted in equation (8), it gives the maximum possible value of operating slip for a given combination of exciting capacitance and rotor speed as

$$s_{\max} = \frac{R_2}{a X_2} \tag{10}$$

But it is to be noted that for the limiting value given by equation (10), the load on the machine becomes so large that the operation as generator fails. Further equation (9) gives

$$\frac{R_{1L}}{R_{1L}^2 + X_{1L}^2} < \frac{1}{2aX_2}$$
(11)

Modification of equation (11) with the assumption that  $(saX_2)^2 \ll (R_2)^2$  which is true for low operating slips, gives;

$$s < \frac{R_2}{2aX_2} \tag{12}$$

The above equation gives the limiting value of slip for the generator operation. Thus limiting value of the operating slip in terms of  $s_{max}$  is;

$$s < \frac{s_{max}}{2} \tag{13}$$

This implies that generator operation is not possible up to  $S_{\mbox{\scriptsize max}}.$ 

### 6. Identification of Control Parameters

In self-excited induction generator, terminal voltage and frequency varies with operating conditions. However these may be controlled by proper control of operating parameters such as excitation capacitance, speed etc.

#### **6.1 Excitation Capacitance**

It is well known that a SEIG always operates at a leading power factor. To meet this condition ' $X_{1L}$ ' as defined in section 3 must be negative.

$$R > \sqrt{\frac{X_1 X_c^2}{X_c - a^2 X_1}}$$
(14)

In this, *R* will be real and positive only when  $X_c \ge a^2 X_l$ 

If  $X_c = a^2 X_1$ , then,  $R \to \infty$ ,

Hence machine is not in a position to deliver the load under such conditions. Excitation shall meet only the VAr requirement of stator, where as in case of induction generator the capacitance must be sufficient to meet the total VAr requirements of the machine.

In case  $X_c >> a^2 X_1$ , then

$$R > (X_I X_C)^{1/2}$$

This is the load capability of the machine up to which a selfexcited induction generator may be loaded for a given value of excitation capacitance.

As  $X_c$  is inversely proportional to *C*, increase in the value of capacitor will reduce the value of  $X_c$ , thus decreasing the effective value of load resistance. This implies that the load capacity of the machine increases with an increase in the value of excitation capacitance.

### **6.2 Operating Speed**

It has been observed that the operating speed of machine is almost linearly related to generated frequency for a given set of operating conditions. Thus any change in the speed affects the generated frequency and plays an important role to control it.

Further any change in generated frequency affects the effective value of excitation reactance. The effective value of excitation reactance decreases with any increase in the frequency, which in turn increases with an increase in the operating speed. Thus any increase in the speed will result in to a reduction in the excitation reactance. This in turn is equivalent to the effect due to an increase in the capacitance. Therefore an increase in the operating speed with constant excitation capacitance and load resistance will result in to an increase in the terminal voltage.

### 5. Results & Discussions

Constant frequency and iteration model as discussed above, were applied on test machine (Appendix-2). Table 1 and Table 2 give a comparison of computed and experimental results on test machine. These are found to be in good agreement, and so confirm the validity of the proposed modeling.

Table1. Experimental verification of constant frequency model

Speed(rpm)	Computed Values		Experimental Values			
	Frequency(Hz)	Voltage(V)	Frequency(Hz)	Voltage(V)		
C=36μF,R=160 Ω						
1467	48.3	158.6	48.3	158		
1498	49.3	178.3	49.35	176		
1516	49.9	188.1	49.92	189		
1543	50.76	201.9	50.74	203		
$C=36 \mu F, R=220 \Omega$						
1467	48.43	173.8	48.28	171		
1496	49.4	190.3	49.24	188		
1540	50.8	213.1	50.78	210		

Table2. Experimental verification of iteration model

Snood(mm)	Computed Values		Experimental Values				
Speeu(Ipili)	Frequency(Hz)	Voltage(V)	Frequency(Hz)	Voltage(V)			
C=36 $\mu$ F,R=160 $\Omega$							
1467	48.29	158.4	48.3	158			
1498	49.3	178.4	49.35	176			
1516	49.89	188.1	49.92	189			
1543	50.78	202.4	50.74	203			
C=36 $\mu$ F, R=220 $\Omega$							
1467	48.44	174.5	48.28	171			
1496	49.39	190.3	49.24	188			
1540	50.84	213.8	50.78	210			

Fig. 3 to Fig. 5 shows the variation of terminal voltage, magnetizing reactance and frequency with excitation capacitance as simulated results on test machine. Here the operating speed of the machine is kept constant as 1 pu. It is felt that any change in the excitation capacitance affects the terminal voltage, magnetizing reactance, generated frequency and load delivered by the machine. Thus the load carrying capacity of the machine may be controlled by change of excitation capacitance and it may act as a control parameter in case of self-excited induction generator.



Fig. 3 Variation of voltage with excitation capacitance, b=1pu



Fig. 4 Variation of magnetizing reactance with excitation capacitance, b=1pu



Fig. 5 Variation of frequency with excitation capacitance, b=1pu



Fig. 6 Variation of voltage with operating speed, C=1pu

Fig. 6 to Fig. 7 gives the variation in the terminal voltage and generated frequency with the operating speed as simulated results on test machine, under given operating condition. It is found that any change in the operating speed effects terminal voltage as well as generated frequency Therefore similar to excitation capacitance operating speed becomes another control variable.



Fig. 7 Variation of frequency with operating speed, C=1pu

## 7. Conclusion

In this paper an attempt has been made to propose new and simple models for the steady state analysis of self-excited induction generator. Closeness between computed and experimental results proves the validity of proposed analysis. Proposed modelling results in the solution of a quadratic equation in contrast to higher order polynomial as obtained by other research person. It has been extended to estimate the operating zone of induction generator. Further controlled parameters have been identified which may be helpful in maintaining the terminal conditions of the generator. As observed from results, constant frequency and iteration model both may be adopted for complete analysis and control.

### Appendix-1

The usual equivalent circuit representation for a threephase induction motor is shown in Fig. 8 (a). This circuit may be redrawn as shown in Fig. 8 (b) and 8 (c). In Fig. 8(c) the sink voltage is given by  $E_2(1-s)$ ;  $E_2$  being equal to  $I_2(R_2/s + jX_2)$ . In case of generator operation, the sink voltage becomes source voltage with slip as negative. The corresponding equivalent circuit is shown in Fig. 8 (d).



Fig. 8 (a)



Fig. 8 (b)



Fig. 8 (c)



Fig. 8 (d)

Fig. 8 Equivalent circuit representation for induction generator

### Appendix-2

The details of the Induction Machine used to obtain the experimental results are;

Specifications

3-phase, 4-pole, 50 Hz, delta connected, squirrel cage induction machine

2.2kW/3HP, 230 V, 8.6 A

• Parameters

The equivalent circuit parameters for the machine in pu are  $R_1 = 0.0723$ ,  $R_2 = 0.0379$ ,  $X_1 = X_2 = 0.1047$ .

Base values

Base voltage =230 V

Base current =4.96 A

Base Impedance=46.32  $\Omega$ 

Base frequency=50 Hz

Base speed=1500rpm

Base capacitance= 68.71µ F

• Air gap voltage

The variation of magnetizing reactance with air gap voltage at rated frequency for the induction machine is as given below.

$X_m < 82.292$	$E_1 = 344.411 - 1.61X_m$
$95.569 > X_m \ge 82.292$	$E_1 = 465.12 - 3.077 X_m$
$108.00 > X_m \ge 95.569$	$E_1 = 579.897 - 4.278X_m$
$X_m \ge 108.00$	$E_1 = 0$

### References

- S. S. Murthy, O. P. Malik, and A.K.Tandon, "Analysis of self-excited induction generators," *Proc. IEE*,vol. 129,pt. C, no. 6,1982, pp. 260-265.
- [2] G. Raina and O. P. Malik, "Wind energy conversion using a selfexcited induction generator," *IEEE Trans. Power Apparatus and Systems*, vol. PAS-102, no. 12,1983,pp. 3933-3936.
- [3] A. K. Tandon, S. S. Murthy and C. S. Jha, "New method of computing steady-state response of capacitor self-excited induction generator," *IE(I) Journal-EL*, vol. 65,1985, pp. 196-201.
- [4] N. H. Malik and S. E. Haque, "Steady-state analysis and performance of an isolated self-excited induction generator," *IEEE Trans. Energy Conversion*,vol.EC-1,no.3, 1986,pp.134-139.
- [5] N. H. Malik and A. H. Al-Bahrani, "Influence of the terminal capacitor on the performance characteristics of a self-excited induction generator," *Proc. IEE*, vol.137,pt.C, no. 2, 1990, pp.168-173.
- [6] L. Shridhar, B. Singh, and C. S. Jha, "A step towards improvements in the characteristics of self-excited induction generator," *IEEE Trans. Energy Conversion*, vol. 8, no. 1,1993, pp. 40-46.
- [7] T. F. Chan, "Steady-state analysis of self-excited induction generators," *IEEE Trans. Energy Conversion*, vol. 9, no. 2,1994, pp.288-296.
- [8] L.Quazene and G. McPherson, "Analysis of the isolated induction generator," *IEEE Trans. Power Apparatus and Systems*, vol. PAS-102, no. 8, 1983, pp. 2793-2798.
- [9] T. F. Chan, "Analysis of self-excited induction generators using an iterative method," *IEEE Trans. Energy Conversion*, vol. 10 no. 3,1995,pp. 502-507.
- [10] K. S. Sandhu and S. K. Jain, "Operational aspects of self-excited induction generator using a new model", *Electric Machines and Power Systems*, vol. 27, no. 2,1999, pp. 169-180.
- [11] I. A. M. Abdel-Halim, M. A. Al-Ahmar, and M. Z. El-Sherif, "A novel approach for the analysis of self-excited induction generator," *Electric Machines and Power Systems*, vol. 27,1999, pp. 879-888.
- [12] K. S. Sandhu, "Iterative model for the analysis of self-excited induction generators," *Electric Power Components and Systems*, vol. 31, no. 10, 2003, pp. 925-939.