

# Experience with SSFR Test for Synchronous Generator Model Identification Using Hook-Jeeves Optimization Method

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*Abstract:* Accurate generator modeling allows for more precise calculation of power system control and stability limits. In this paper a procedure using a set of measured data from Standstill Frequency Response (SSFR) test on MontazerGhaem gas power plant's synchronous generator is used to obtain synchronous machine. A novel approach is used to find d-axis which is different from standard SSFR scheme which can save the time in doing SSFR tests. Hook-Jeeves method is used for optimization purpose. The test procedure and identification results are reported.

*Keywords:* SSFR, Synchronous generator, Parameter identification

## 1- Introduction

Stability analysis is one of the most important tasks in power system operations and planning. Synchronous generators play a very important role in this way. A valid model for synchronous generators is essential for a reliable analysis of stability and dynamic performance. Almost three quarters of a century after the first publications in modeling synchronous generators, this subject is still a challenging and attractive research topic.

Two axis equivalent circuits are commonly used to represent the behavior of synchronous machines. The direct determination of circuit parameters from design data is very difficult due to intricate geometry and nonlinear constituent parts of machines. So several tests have been developed which indirectly obtain the parameter values of equivalent circuits.

The stand still Frequency Response (SSFR) test has been widely accepted for extraction synchronous machine parameters. The following advantages can credit to the SSFR method:

- 1) It is easy to implement at the factory or during outages for routine maintenance without risk to the machine, since the tests involve very little power.
- 2) The ready availability of powerful computer tools have eased the data logging and analysis procedures.
- 3) Unlike the ANSI-standardized short-circuit test, the SSFR approach can simultaneously provide

the equivalent circuits for both direct and quadrature axes, and at the present time, seems the most appropriate for modeling the machine behavior for stability analysis.

Frequency response testing of electrical machines as a means of determining their parameters was introduced by [2] but the main thrust for the current work stems from the comprehensive study of the problem initiated by EPRI which culminated in the workshop in 1981 [3].

In [4] presented results of frequency response tests carried out on a 555MVA machine, with limited frequency range of 0.01 to 10 Hz but this was sufficient to identify a third order model for the machine. In [5] presented results for third order models for several machines introducing the concept of unequal mutual in the direct axis. In [6] proposed a new third order model claiming it as an improvement on the limited second order model. In [7] offered a recursive least squares algorithm with a frequency dependent weighting function to accentuate particular frequency ranges as an aid to the identification of the time constants. Numerical curve-fitting methods were used in all of the above papers.

In this paper an experience with SSFR test on MontazerGhaem gas unit generator has been presented and used Hook and Jeeves optimization method for curve fitting purpose.

## 2- MACHINE MODELING

The structure of the synchronous machine model used

in this study is a standard second order model with one damper in the d-axis and two dampers in the q-axis given in Fig. 1 [8]. Degree of the applied model is selected based on synchronous generator type, rotor structure and IEEE-Std-1110 considerations. The equations of generators are as stated in [2]. Some relations between parameters are listed in Appendix.

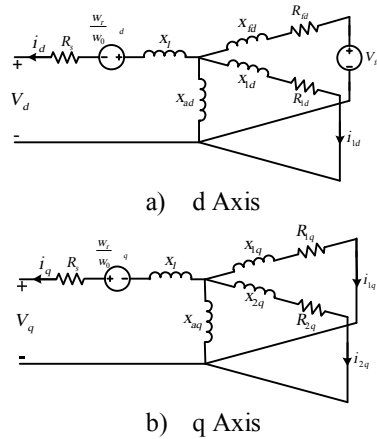


Fig.1) Synchronous Machine Equivalent Circuits According to 2-2 Model of IEEE Std 1110

### 3- TEST PROCEDURE

The SSFR test is categorized in off-line tests so machine shall be shut down, disconnected from its turning gear and electrically isolated. Also all connection to the field should be taken off, this can be done by removing the brush gear or, in the case of a brushless exciter, electrically disconnecting the complete exciter from the generator field winding. This test consists of two steps, one for d-axis and another for q-axis. For each step, by positioning the rotor align with d or q axis and temporarily connecting the power amplifier as in table (1) the tests are performed.

Reducing or eliminating the effect of contact resistances is very important to the accuracy of the measurements, particularly for the armature winding.

The armature current metering shunt should be bolted directly to the conductor in the isolated phase bus, as close to the generator terminals as possible, also conducting grease should be used to enhance the contact.

For aligning the rotor with the q-axis, a power amplifier is temporarily connected as in Fig 3. A signal generator tuned on 100 Hz and 10 amps drives the amplifier. Then the induced field voltage is measured with an oscilloscope. The

generator rotor is slowly turned until a null induced field voltage is achieved.

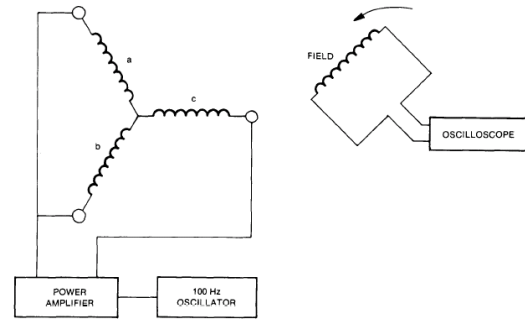


Fig.2) Positioning rotor align with q-axis tests

This situation indicates quadrature-axis of the synchronous machine.

In this paper a novel approach is used to obtain d-axis which is different from standard SSFR scheme [1]. For this purpose, after finding q-axis, by keeping rotor position the armature phase winding connection is changed as illustrated in table(1). In this situation the rotor is aligned with d-axis. With using this novel method, the d-axis could be found as precisely as q-axis without additional work.

For performing SSFR tests, considering the test circuits illustrated in table (1), the following tests are carried out.

One test for q-axis corresponding to the test circuit no.1, and two tests for d-axis corresponding to test circuits no. 2 & 3. No test has been done with respect to test circuit no.4.

For each test, the frequency of the provided sin wave signal by the signal generator is changed over the range of .01Hz to 1000 Hz. Then for each frequency, the magnitude and phase of  $\Delta e_q, \Delta i_q, \Delta e_d, \Delta i_d, \Delta e_{fd}$  and  $\Delta i_{fd}$  are measured.

Approximately 10 test points, logarithmically spaced per decade of frequency, is a satisfactory measurement density.

### 4- IDENTIFICATION PROCEDURES

The procedure for extracting d and q-axes parameters from SSFR tests can be summarized as follows [10]:

- 1) Use the best available estimation for armature leakage inductance  $L_l$ ; it could be valued supplied by manufacturer.
- 2) Using the measured values, by means of Fourier transform the RMS value of the main wave associated with each measured quantities and corresponding to each frequency are obtained.
- 3) Based on the equations for  $Z_d$  and  $Z_q$  mentioned in table(1) and using RMS values

Table (1) Standstill Frequency Response Test

No.	Measurement	Test Diagram	Measured Value	Relationships
1	q-Axis operational Impedance $Z_q(s)$		$U_{stator}$ $I_{stator}$ $U_{rotor(about\ 0)}$	$Z_q(s) = -\frac{\Delta e_q(s)}{\Delta i_d(s)} \Big _{\Delta e_{fd}=0}$
2	d-Axis operational Impedance $Z_d(s)$		$U_{stator}$ $I_{stator}$ $U_{rotor(max)}$	$Z_d(s) = -\frac{\Delta e_d(s)}{\Delta i_d(s)} \Big _{\Delta e_{fd}=0}$
3	Standstill armature to field transfer function $sG(s)$		$U_{stator}$ $I_{stator}$ $I_{rotor}$	$sG(s) = -\frac{\Delta i_{fd}(s)}{\Delta i_d(s)} \Big _{\Delta e_{fd}=0}$
4	Standstill armature to field transfer impedance $Z_{af0}$		$U_{rotor}$ $I_{stator}$ $I_{rotor(about\ 0)}$	$Z_{af0}(s) = -\frac{\Delta e_{fd}(s)}{\Delta i_d(s)} \Big _{\Delta i_{fd}=0}$

for the measured quantities, the value for  $Z_d$ ,  $Z_q$  and  $G(s)$  are obtained corresponding to each

- Obtain  $L_d(0)$  and  $L_q(0)$  which are low-frequency limit of  $L_d(s)$  and  $L_q(s)$  and then determine

$$L_{ad}(0) = L_d(0) - L_l$$

$$L_{aq}(0) = L_q(0) - L_l$$

- find the field to armature turns ratio  $N_{fd}/N_a$  using the armature to field transfer impedance  $Z_{af0}(s)$

$$N_{af}(0) = \frac{1}{sL_{ad}(0)} = \lim_{s \rightarrow 0} \left[ \frac{\Delta e_{fd}(s)}{\Delta i_d(s)} \right]$$

- Calculate the field resistance referred to armature winding.

$$R_{fd} = \frac{sL_{ad}(0)}{\lim_{s \rightarrow 0} \left[ \frac{\Delta i_{fd}(s)}{\Delta i_d(s)} \frac{2}{3} N_{af}(0) \right]}$$

- Define an equivalent circuit structure for the d and q axes.
- Use the Hook-Jeeves optimization technique to find the best value for generator parameters

which provide the best fits for  $L_d(s)$  and  $L_q(s)$  and  $sG(s)$

- Measure the fields winding resistance, convert it to the desired operating temperature, and refer it to the stator

$$R_{fd-\theta} = \left[ \frac{234.5 + \theta}{234.5 + T_f} \right] R_{fd} \times \frac{3}{2} \left[ \frac{1}{N_{af}(0)} \right]^2$$

### 5-HOOK AND JEEVES OPTIMIZATION METHOD

The pattern search method of Hook and Jeeves is a sequential technique in which each step consists of two kinds of moves, one called exploratory move and another called as pattern move. The first move is to explore the local behavior of the objective function and the second move is to take advantage of the pattern direction. The general procedure can be described by the following steps [11].

- Start with an arbitrarily initial point  $X_1 = [x_1 \ x_2 \ \dots \ x_n]^T$ , called the starting base point and prescribed step lengths  $\Delta x_i$  in each of the coordinate directions  $u_i$ ,  $i = 1, 2, \dots, n$ . set  $k=1$ .
- Compute  $f_k = f(X_k)$ . Set  $i=1$  and define new variable with initial value set as,  $Y_{k0} = X_k$  and start the exploratory move as stated in step 3.
- The variable  $x_i$  is perturbed about the current temporary base point  $Y_{k,i-1}$  to obtain the new temporary base point as follows:

$$Y_{k,i} \begin{cases} Y_{k,i-1} + \Delta x_i u_i & \text{if } f^+ = f(Y_{k,i-1} + \Delta x_i u_i) \\ & < f = f(Y_{k,i-1}) \\ Y_{k,i-1} - \Delta x_i u_i & \text{if } f^- = f(Y_{k,i-1} - \Delta x_i u_i) \\ & < f = f(Y_{k,i-1}) \\ & < f^+ = f(Y_{k,i-1} + \Delta x_i u_i) \\ Y_{k,i-1} & \text{if } f = f(Y_{k,i-1}) < \min(f^+, f^-) \end{cases}$$

This process of finding the new temporary base point is continued for  $i=1,2, \dots$ . Until  $x_n$  is perturbed to find  $Y_{k,n}$ .

4- If the point  $Y_{k,n}$  remains same as the  $X_k$ , reduce the step lengths  $\Delta x_i$  (say by a factor of two), set  $i=1$  and go to step 3.

If  $Y_{k,n}$  is different from  $X_k$ , obtain the new base point as

$$X_{k+1} = Y_{k,n}$$

and go to step 5.

5- With the help of the base points  $X_k$  and  $X_{k+1}$  establish a pattern direction  $S$  as

$$S = X_{k+1} - X_k$$

and find a point  $Y_{k+1,0}$  as

$$Y_{k+1,0} = X_{k+1} + \lambda S$$

The point  $Y_{kj}$  indicates the temporary base point obtained from the base point  $X_k$  by perturbing the  $j^{\text{th}}$  component of  $X_k$ .

Where  $\lambda$  is the step length which can be taken as 1 for simplicity.

6- set  $k=k+1$ ,  $f_k = f(Y_{k0}), i=1$  and repeat step 3, if at the end of step 3,  $f(Y_{k,n}) < f(X_k)$ , we take the new base point as  $X_{k+1} = Y_{k,n}$ , and go to step 5. On the other hand if  $f(Y_{k,n}) \geq f(X_k)$ , set  $X_{k+1} = X_k$ , reduce the step length  $\Delta x_i$ , set  $k = k+1$  and go to step 2.

7- The process is assumed to be converged whenever the step lengths fall below a small quantity  $\epsilon$ . thus the process is terminated if

$$\max_i (\Delta x_i) < \epsilon$$

## 6- CARRY OUT SSFR TEST AND PARAMETER EXTRACTION

SSFR tests were performed on MontazaerGhaem rated 147.8 MVA, 13.8KV, 50 Hz, gas Generator. Leakage reactance is extracted from design data and equals to 0.095 p.u. Armature and field resistances are taken as  $R = 0.00141 \Omega$   $R_f = 0.1015 \Omega$  from generator technical document. Temperature during tests was

measured as 27 °C, while operating temperature is supposed to be 100 °C.

The rotor position was changed by means of rotor lifting pump which made it easy to rotate the rotor with the use of proper pulling tools. During positioning of the rotor, zero voltage on the field winding could not be precisely achieved, so the final position was decided by achieving the minimum induced field voltage. During measurements, signals became noisier as the frequency was decreased below 0.1 Hz.

During the test instantaneous value of measured current and voltage are recorded by transient recorder in each scanning frequency. Using Fourier transform, from the instantaneous measured values, RMS values are extracted by which operational impedances  $Z_d, Z_q$  and  $G(s)$  (both magnitudes and angles) are calculated for the whole range of scanning frequency. The magnitudes and phase angles of  $Z_d$  and  $Z_q$  are illustrated in fig (4), (5) respectively.

$R_d, R_q$  are obtained by extrapolating operational impedances  $Z_d, Z_q$  at zero frequency as illustrated in Fig.6. Using operational impedances  $Z_d, Z_q$  and  $R_d, R_q$ , the d and q axes impedances are calculated and depicted as Fig. for finding  $L_d(0)$  and  $L_q(0)$  is used from a fictitious quadrate rational function.(Fig.7)

For fitting  $L_d$  and  $L_q$  to obtain equivalent circuit parameters we used the Hook-Jeeves optimization technique [13]. All data processing was done in actual units and at the end p.u values was calculated relevantly. Curve fitting for finding  $L_d$  and  $L_q$  magnitude and phase using Hook-Jeeves method is illustrated in Fig.8 – Fig. 11.

Field resistance is modified according to operating temperature and actual value obtained from manufacturer.  $L_{ad}$  and  $L_{aq}$  are modified for operating flux density using linear equation of [2]. The final result for d and q axis is summarized in table (2) and table (3) respectively. The manufacturer parameter for d-axis and q-axis is shown in table (4).

## 7-CONCLUSION

It has been demonstrated here that the problem of the synchronous machine's parameters identification. From the results of frequency response tests can be done by an essentially analytical process. The parameters are estimated using Hook-Jeeves pattern search method. Simulation and experimental results show that the parameters of model for a synchronous generator can be identified successfully and have good accuracy with parameters presented by manufacturer. Model can then be used for studying low frequency oscillations and design and tuning power system stabilizers.

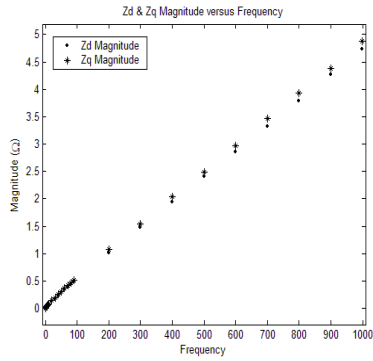


Fig.3)  $Z_d$  and  $Z_q$  magnitudes obtained by SSFR test

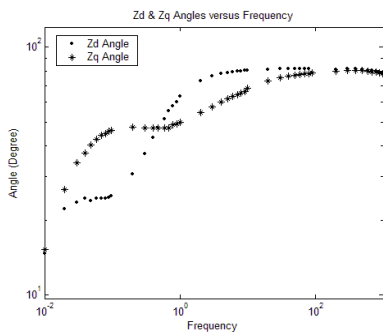


Fig.4)  $Z_d$  and  $Z_q$  phase angles obtained by SSFR test

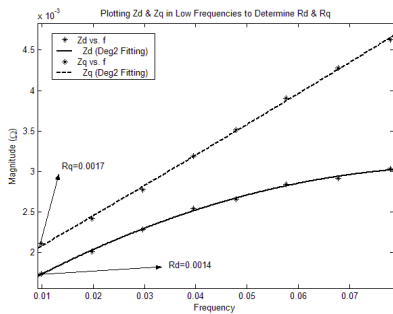


Fig.5) Extended window for Low frequency magnitudes of  $Z_d$  and  $Z_q$  to obtain  $R_d$  and  $R_q$

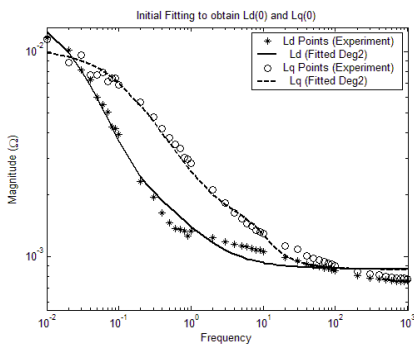


Fig.6) Finding  $L_d(0)$  and  $L_q(0)$  using a fictitious quadratic rational function

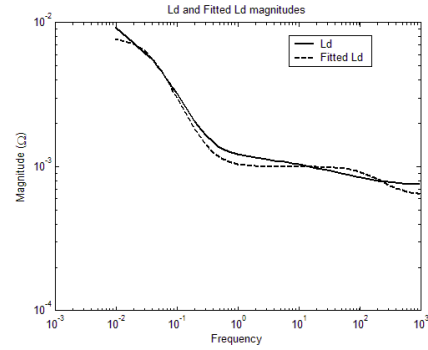


Fig.7)  $L_d$  magnitude fitting to obtain parameters, a second order model

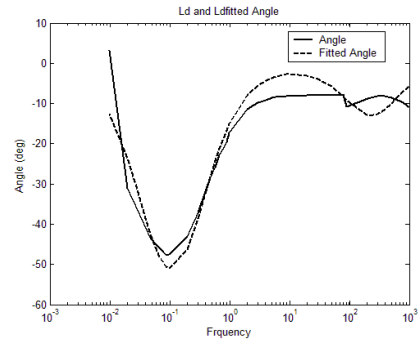


Fig.8) Angle of  $L_d$  and fitted quad rational function, second order model

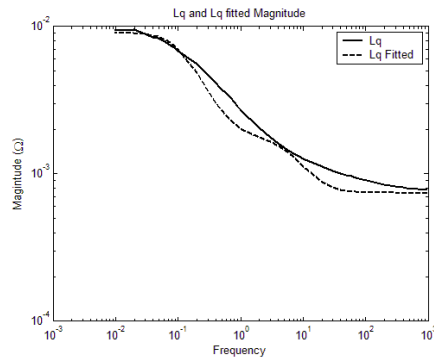


Fig.9)  $L_q$  magnitude fitting to obtain parameters, a second order model

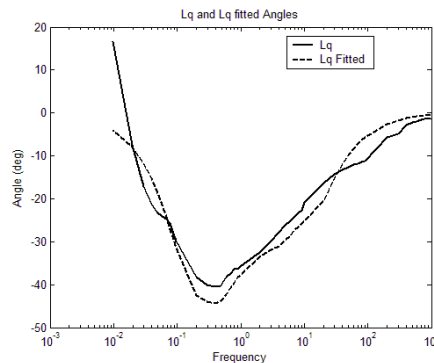


Fig.10) Angle of  $L_q$  and fitted quad rational function, second order model

Table(2) D-axes results

Rfd (pu)	Lfd (pu)	Rd1 (pu)	Ld1 (pu)	Ladu(Test) (pu)	Ladu(mod) (pu)	Ll (pu)	Ra (pu)	X"d (pu)	T"d (s)	X'd (pu)	T'd (s)	Xd (pu)
0.001018	0.18182	0.96219	0.11716	2.22088	2.19300	0.095	0.001094	0.16401	0.0190	0.2629	0.8526	2.2880

Table (3) Q-axes results

Rq2 (pu)	Lq2 (pu)	Rq1 (pu)	Lq1 (pu)	Laqu (Test) (pu)	Laqu (mod) (pu)	Ll (pu)	Ra (pu)	X"q (pu)	T"q (s)	X'q (pu)	T'q (s)	Xq (pu)
0.051411	0.098088	0.007403	0.379834	2.098992696	2.0726421	0.095	0.001094	0.17013	0.020612	0.4160	0.2023	2.16764

Table (4) Manufacturer provided data

X"d (pu)	T"d (s)	X'd (pu)	T'd (s)	Xd (pu)	X"q (pu)	T"q (s)	X'q (pu)	T'q (s)	Xq (pu)
0.19	0.021	0.28	0.88	2.29	0.19	0.021	0.39	0.15	2.12

### ACKNOWLEDGEMENT

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#### APPENDIX

Some relations between operational parameters and dynamical parameters are presented here.

$$X_d = x_l + x_{ad}$$

$$X_q = x_l + x_{aq}$$

$$X'_d = x_l + x_{ad} \parallel x_{fd} = x_l + \frac{X_{ad} X_{fd}}{X_{ad} + X_{fd}}$$

$$X'_q = x_l + x_{aq} \parallel x_{1q} = x_l + \frac{X_{aq} X_{1q}}{X_{aq} + X_{1q}}$$

$$X''_d = x_l + x_{ad} \parallel x_{fd} \parallel x_{1d} = x_l + \frac{X_{ad} X_{fd} X_{1d}}{X_{ad} X_{fd} + X_{ad} X_{1d} + X_{fd} X_{1d}}$$

$$X''_q = x_l + x_{aq} \parallel x_{1q} \parallel x_{2q} = x_l + \frac{X_{aq} X_{1q} X_{2q}}{X_{aq} X_{1q} + X_{aq} X_{2q} + X_{1q} X_{2q}}$$

$$T'_{do} = \frac{1}{\omega_0 R_{fd}} (x_{fd} + x_{ad})$$

$$T'_{qo} = \frac{1}{\omega_0 R_{1q}} (x_{1q} + x_{aq})$$

$$T''_{do} = \frac{1}{\omega_0 R_{1d}} (x_{1d} + x_{fd} \parallel x_{ad}) = \frac{1}{\omega_0 R_{1d}} \left( x_{1d} + \frac{X_{fd} X_{ad}}{X_{fd} + X_{ad}} \right)$$

$$T''_{qo} = \frac{1}{\omega_0 R_{2q}} (x_{2q} + x_{1q} \parallel x_{aq}) = \frac{1}{\omega_0 R_{2q}} \left( x_{2q} + \frac{X_{1q} X_{aq}}{X_{1q} + X_{aq}} \right)$$