Program Optimization Using Abstract State Machines

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Abstract: Usually the result code of source code by a compiler is not necessary the best one, and can be improved to run faster or to use less memory. This kind of improvement is done in compiling phase after parsing. Some good techniques in optimization are in folding the constants, elimination of dead code, or improvement of the loops. Here it is considered the runtime overhead and present how can this be improved. The source is specific for object oriented languages with late binding, where a name of method to be called is bound to method dynamically. It increases the computation time by a cost of traversing the class hierarchy each time a method is called.

Keywords: Optimization, Abstract State Machine (Evolving Algebras), Annotation Class

1. Introduction in optimization

Usually the result code made by a compiler is not necessary the best one, and can be improved to run faster or to use less memory. This kind of improvement is done in compiling phase after parsing. Some good techniques in optimization are in folding the constants, elimination of dead code, or improvement of the loops. Details about these methods can be found in [2]

In this paper it is considered one source of runtime overhead and how to eliminate it. The source is specific for high level programming languages (object-oriented) with late-binding, where a name of method to be called is bound to the method dynamically.

In this way the computation time will increase for parsing the class hierarchy each time this method is called.

In 3 the algebra will be transformed in a form that can be used by a modified version of R to run the program faster by statically binding a name of method with method.

2. Collecting information

The optimization method that will be discussed needs an collection of receivers’ classes, which are used as an additional input for optimization. Will call this receivers’ class, a annotation class.

In general, the problems to determine the class of a given expression for a given program and input are undecidable.

Different methods for finding an approximation of an annotation class were proposed. Graver and Johnson designed a type system. Their solution needs manual type declaration of methods, and than type of expressions can be reconstructed.

Completely different approach was suggested by Agesen and Hölze in [1]. Their method, named feedback, extracts receivers’ possible classes of a program from a previous execution of P. The optimization of P is divided into two phases. In the first phase P is run and if some message expression of P is computed, then the class of the receiver of this expression is stored in memory. The second phase optimizes P using information stored in the previous run of P. In [1] a comparison between type reconstruction and feedback is discussed.

In this section will be defined an algebra $C_0$ obtained from algebra $B_0$ by adding a new universe CLASS_LIST, and three functions $TypeOf$, $First$ and $Method$.

Elements of universe CLASS_LIST represents the annotation class as a list of elements from universe CLASSES. The first element of such a list is given by the function:

$$First : CLASS \_ LIST \rightarrow CLASSES$$

Suppose that for each element from universe EXPRESSIONS an annotation class is given, e.g. as a result of one of methods mentioned above.
For each $e \in EXPRESSIONS$ the annotation class of $e$ is given by the function value
LISTSCLASS SEXPRESSION

TypesOf : EXPRESSIONS → CLASS _LISTS

If, for e ∈ EXPRESSIONS representing the message expression a class of its receiver is determined uniquely, i.e. the list TypeOf (REceiver(e)) has only one element, than it is possible to determine, which method should be invoked if e is evaluated. For such e a function:

Method : EXPRESSIONS → METHODS

it is defined. In section 2.1 will give a definition of the value of Method.

In addition, will be defined the transition rule R2 for C0, that is a modified version of transition rule R1.

Semantics defined by < B0, R1 > is equivalent with semantics defined by < C0, R2 > in the sense that for some programs P, < B0, R1 > defines the semantics for P, than < C0, R2 > defines, also, an equivalent semantics of P.

3. Static dispatch

3.1 Methods transformation

In this section the algebra B0 will be modified to be possible to use the information stored by TypeOf function.

Suppose that for one element e from universe EXPRESSIONS, the length of list TypeOf(e) is 1, i.e. the expression class e is uniquely determined. Suppose, also that e represents a receiver of method expression, i.e. exists e′ ∈ EXPRESSIONS such that

REceiver(e′) = e

Than it is easy to determine which method will be called if computation comes to e′: it is a value of the term Method (Name(e′), First (TypeOf(e))) or, if no method with the name Name(e′) is in class TypesOf(e), than a suitable method is search in class Superclass (TypeOf(e)), than in Superclass (Superclass (TypeOf(e))), etc. If a method is found in class C, than the value of term Method (Name(e′), C) will be assigned to the term Method(e′). Otherwise, if no method is found, then the program is not correct.

Such a transformation performed for each element from universe EXPRESSIONS makes that transformed programs to run faster.

3.2 Program improvements

We can define now a rule R2 that uses the functions defined in algebra C0.

Definition of R2 is obtained from definition of R1 by doing some modifications.

It is defined a new rule MODIFIED_LOOKUP. In R2 the rule EXPRESSION_EVALUATION differs from rule EXPRESSION_EVALUATION from R1, since MODIFIED_LOOKUP is used instead of METHOD_LOOKUP.

Rule MODIFIED_LOOKUP

if Method (CurrExp) ≠ undef then
    Method := Method (CurrExp)
    Receiver := Expression_value (Receiver (CurrExp), Current_state)
else
    METHOD_LOOKUP
endif

EndRule

Rule EXPRESSION_EVALUATION

if is not method then
    PRIMARY_EVALUATION
elseif Expression_value (Receiver (CurrExp), Current_state) = undef then
    CurrExp := Receiver (CurrExp)
elseif First_argument (CurrExp) = undef then
    MODIFIED_LOOKUP
elseif Expression_value (First_argument (CurrExp), Current_state) = undef then
    CurrExp := First_argument (CurrExp)
else
    MODIFIED_LOOKUP
endif

EndRule

3.3 Equivalence of semantics

In this section we study the equivalence of the continuation semantics previously given, and also, its optimized version with static dispatch from section 3.1. We will demonstrate that the results given by both semantics are equivalent.

Let P be e program, and let be an algebra B0 defined for P, and let C0 be the algebra defined for P. R1 and R2 are transition rules. The pairs < B0, R1 > and < C0, R2 > defines two operational semantics of P.

Recall definition of equivalence:

Let P be a program, and b and c two elements from B0, respectively C0 are equivalents b ≡ c if and only if b and c represents the same name, either
the same list of names, either the same object, either the same variable, either the same method, expression or state from P.

Let \( \Sigma \) be a signature included in signatures \( \Sigma _{B} \) and \( \Sigma _{C} \), of \( B_{i} \) and \( C_{j} \). We shall write that \( B_{i} \) and \( C_{j} \) are equivalent up to \( \Sigma \). Notice that each set of applicable rules \( R_{1} \) and \( R_{2} \) consists of most one rule \( \text{extend} \), such that the definition of equivalence between elements can be extended for the new created elements (see definition 3.2).

Definition 3.2 Let \( C \) and \( D \) be algebras such that:

\[
C \equiv _{\Sigma } D
\]

Let be \( R \) a set of update rules over \( \Sigma \) including one extend rule. Let \( c \) and \( d \) be elements created by applying \( R \) in \( C \) and \( D \). We have

\[
c \equiv d
\]

then results of applying \( R \) to \( C \) and \( D \) are also equivalent up to \( \Sigma \).

Definition of \( C_{0} \) is derived from definition of \( B_{0} \), by adding an additional function \( \text{Method} \). So, if \( \Sigma _{B} \) denotes the signature of \( B_{0} \) then

\[
B_{0} \equiv _{\Sigma _{B}} C_{0}
\]

Let \( R_{1} *(B_{0}) \) be the computation

\[
R_{1} *(B_{0}) = B_{0}, B_{1}, B_{2}, ..., B_{m}, ...
\]
determined by the pair \( <B_{0}, R_{1}> \).

Let \( R_{2} *(C_{0}) \) be the computation

\[
R_{2} *(C_{0}) = C_{0}, C_{1}, C_{2}, ..., C_{n}, ...
\]
determined by the pair \( <C_{0}, R_{2}> \).

Since \( R_{1} \) differs from \( R_{2} \), the evaluations \( R_{1} *(B_{0}) \) and \( R_{2} *(C_{0}) \) can be different.

Bellow we consider these differences between \( R_{1} *(B_{0}) \) and \( R_{2} *(C_{0}) \).

Suppose that \( B_{i} \) and \( C_{j} \) such that

\[
B_{i} \equiv _{\Sigma } C_{j}
\]

but

\[
R_{1} (B_{i}) \equiv _{\Sigma } R_{2} (C_{j})
\]
does not hold. This implies that two different set of rules have been applied, i.e. set of applicable rules \( E_{B_{i}} (R_{1}) \) and \( E_{C_{j}} (R_{2}) \) are different. Notice that exists only one difference between \( R_{1} \) and \( R_{2} \), in \( R_{2} \) LOOKUP_METHOD is replaced by MODIFIED LOOKUP. So, if

\[
B_{i} \equiv _{\Sigma } C_{j}
\]

and METHOD_LOOKUP is applied to \( B_{i} \) and MODIFIED_LOOKUP is applied to \( C_{j} \), than

- \( B_{i} |= \text{Receiver}(\text{Current_expression}(\text{Current_state})) \neq \text{undefined} \)
- \( C_{j} |= \text{Receiver}(\text{Current_expression}(\text{Current_state})) \neq \text{undefined} \)
- \( C_{j} |= \text{Method}(\text{Current_expression}(\text{Current_state})) \neq \text{undefined} \)

In such case the values of term \( \text{Current_expression}(\text{Current_state}) \) from \( B_{i} \) and \( C_{j} \) corresponds to the message expression \( \text{exp} \) from \( P \). Moreover, the method being called by \( \text{exp} \), can be uniquely determined, and the element \( m \) corresponding to this method is the value of term \( \text{Method}(\text{Current_expression}(\text{Current_state})) \) from \( C_{j} \).

Rules METHOD_LOOKUP and MODIFIED_LOOKUP compute a value of constant method \( \text{Method} \), which corresponds to the method that will be called.

METHOD_LOOKUP (from \( R_{1} \)) computed \( \text{Method} \) in different steps by parsing the class hierarchy. These steps forms a subset of \( R_{1} *(B_{0}) \)

\[
B_{i}, B_{i+1}, ..., B_{i_{k}}
\]

For each \( n,i \leq n \leq i_{k} \) we have

\[
B_{n} |= \text{Method} = \text{undefined}
\]

and

\[
B_{i_{k}} |= \text{Method} \neq \text{undefined}
\]

Notice that METHOD_LOOKUP applied to \( B_{n},i \leq n \leq i_{k} \) changes only the value of the constant \( \text{Class} \). This implies, that for each \( n \) such that \( i \leq n \leq i_{k} \)

\[
B_{n} \equiv _{\Theta } C_{j}
\]

where \( \Theta = \Sigma _{B} / \{ \text{Class} \} \).

In the final step \( B_{i_{k}} \), a value is assigned to \( \text{Method} \) by METHOD_LOOKUP. In \( R_{2}(C_{0}) \), a value of \( \text{Method} \) is determined in one step, and is already computed in \( R_{2}(C_{j}) \) by evaluating the term \( \text{Method}(\text{Current_expression}(\text{Current_state})) \), and assigning its value to \( \text{Method} \). If function \( \text{Method} \) is determined correctly, then the values of the constant \( \text{Method} \) from \( B_{i_{k}} \) and \( R_{2}(C_{j}) \) should be equivalent, hence

\[
B_{i_{k}} \equiv _{\Sigma } R_{2}(C_{j})
\]
We know that
\[ B_0 \equiv_{\Sigma_B} (C_0) \]
so two computations: \( R_1^* (B_0) \) and \( R_2^* (C_0) \),
begin from two equivalent algebras.
Moreover, if
\[ B_i \equiv_{\Sigma_B} C_j \]
then, if the set of applicable rules \( E_{B_i}(R_i) \) and
\( E_{C_j}(R_j) \) are equals, than
\[ R_i(B_i) \equiv_{\Sigma_B} R_j(C_j) \]
Notice that if \( E_{B_i}(R_i) \) and \( E_{C_j}(R_j) \) are equals than
all terms from \( E_{B_i}(R_i) \) and \( E_{C_j}(R_j) \) are built over
\( \Sigma_B \). If these sets of applicable rules are not equals,
than \( R_i(B_i) \) and \( R_j(C_j) \) are not equivalent over
\( \Sigma_B \). However, in this case exists \( k \) nonnegative such
that
\[ R_i^{(k)} (B_i) \equiv_{\Sigma_B} R_j(C_j) \]
So, the computations \( R_1^* (B_0) \) and \( R_2^* (C_0) \)
become equivalent again from \( R_i^{(k)} (B_i) \) and \( R_j(C_j) \).

Theorem 1 The computation \( R_1^* (B_0) \) is finite if and
only if the computation \( R_2^* (C_0) \) is finite.

Theorem 2 Let computations \( R_1^* (B_0) \) and
\( R_2^* (C_0) \) be finite. Let \( R_i^{(x)} (B_0) \) be the last algebra
of \( R_1^* (B_0) \), let \( R_j^{(x)} (C_0) \) be the last algebra of
\( R_2^* (C_0) \). Then
\[ R_i^{(x)} (B_0) \equiv_{\Sigma_B} R_j^{(x)} (C_0) \]
Theorem 2 implies that the final value of the constant \( \text{Last_value} \),
that represents the value if program \( P \), has equivalent interpretations in \( R_i^{(x)} (B_0) \)
and \( R_j^{(x)} (B_0) \).

4. Conclusions
In this paper we have presented an optimization
method of the programs by applying operational
semantics of an object-oriented programming
language.
The problem with late binding, where a name
of method to be called is bound to method
dynamically, it increases the computation time by a
cost of traversing the class hierarchy each time a
method is called it, it is solved by the transformed
algebra in a form that can be used by a modified
version of \( R \) to run the program faster by statically
binding a name of method with method.

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